


Name:			
Enrolment No:			
<div><div>UPES</div><div>End Semester Examination, May 2025</div><div>Course: Probability, Computing and Statistics</div><div>Semester: IV</div><div>Program: B-SC-CS</div><div>Course Code: CSEG2061</div><div>Time: 03 hrs.</div><div>Max. Marks: 100</div></div>			
Instructions: Use of non-programmable scientific calculators is allowed.			
<div>SECTION A</div> <div>(5Qx4M=20Marks)</div>			
S. No.		Marks	CO
Q 1	Define moment generating function.	04	CO1
Q 2	State two properties of cumulative distribution function.	04	CO2
Q 3	A sample of 36 students has an average height of 164 cm. The population mean is 160 cm with a standard deviation of 9 cm. At 5% significance level, test whether the sample mean is significantly different from the population mean.	04	CO4
Q 4	What is the principle of least squares?	04	CO3
Q 5	Explain Euler’s Method with formulas and steps.	04	CO5
<div>SECTION B</div> <div>(4Qx10M= 40 Marks)</div>			
Q 6	Let X be a random variable with the following probability function: xi: -5 -3 0 2 4 6 p(xi): n 0.2 n 0.1 3n 0.3 Determine: i. The constant n. ii. P(X ≤ 0). iii. P(-4 < X ≤ 5). iv. The mean of X. v. The standard deviation of X.	10	CO1
Q 7	Fit a straight line to the following data using least squares method: X: 1 2 3 4 5 Y: 2 4 5 4 5	10	CO3
Q 8	A random sample of 1000 items gave 400 defective. Can the sample be regarded as taken from a population in which 42% of the items are defective? Test at 5% level of significance.	10	CO4
Q 9	Find the eigenvalues of the matrix	10	CO5

	$A = \begin{bmatrix} 4 & 1 & 2 \\ 1 & 3 & 0 \\ 2 & 0 & 2 \end{bmatrix}$ <p style="text-align: center;">OR</p> <p>Solve the initial value problem using the Runge-Kutta method of order 2 method:</p> $\frac{dx}{dy} = x + 2y, \quad y(0) = 1$ <p>with step size h = 0.2, up to 3 iteration and find y(1).</p>												
<p style="text-align: center;">SECTION-C (2Qx20M=40 Marks)</p>													
Q 10	<p>Define Chi-Square Test, its Assumptions and Decision Criteria, and solve the following problem A beverage company claims that its four new drink flavors are equally popular among consumers. A random sample of 120 people gave the following preferences:</p> <table><tr><td>Flavor</td><td>Observed</td></tr><tr><td>Apple</td><td>28</td></tr><tr><td>Berry</td><td>30</td></tr><tr><td>Citrus</td><td>33</td></tr><tr><td>Guava</td><td>29</td></tr></table> <p>Test whether the company's claim is valid at 5% level of significance ($\alpha = 0.05$) using the Chi-Square Goodness of Fit Test. From Chi-Square table, at $\alpha=0.05$, $df=3$ is 7.815</p> <p style="text-align: center;">OR</p> <p>Write a short Introduction to ANOVA test and solve the following problem A researcher wants to test whether there is a significant difference in the mean productivity of workers trained using three different training programs. The productivity scores (in units produced per day) are given below:</p> <ul style="list-style-type: none">• Program A: 92, 95, 91• Program B: 88, 85, 87• Program C: 90, 89, 91 <p>Test at the 5% significance level whether the training program has a significant effect on productivity. Given $F_{0.05}(2,6) \approx 5.14$</p>	Flavor	Observed	Apple	28	Berry	30	Citrus	33	Guava	29	20	CO4
Flavor	Observed												
Apple	28												
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Q 11	<p>Explain Gauss-Jacobi Methode with formulas and steps, and solve the system:</p> $\begin{aligned} 10x_1 + 2x_2 - x_3 &= 27 \\ -3x_1 - 6x_2 + 2x_3 &= -61 \\ x_1 + x_2 + 5x_3 &= -21 \end{aligned}$ <p>using Gauss-Jacobi method with initial guess $x(0) = (0, 0, 0)$.</p>	20	CO5										