

Name:	
Enrolment No:	

UNIVERSITY OF PETROLEUM AND ENERGY STUDIES
End Semester Examination, May 2022

Course: Statistical Mechanics
Program: B. Sc (Honors) Physics
Course Code: PHYS 3004

Semester: VI
Time : 03 hrs.
Max. Marks: 100

Instructions: Draw a neat and clean diagram wherever it is needed.

SECTION A
(5Qx4M=20Marks)

S. No.	Question	Marks	CO
Q 1	Deduce the Wien's Law from the Planck's law of Blackbody radiation.	4	CO1
Q.2	Determine the wavelength corresponding to the maximum emissivity of a blackbody at a temperature equal to 300K. Take the Wien's constant equal to 2898 $\mu\text{m K}$.	4	CO2
Q.3	Define the following terms (a) Phase space (b) Macro and Micro states (c) Ensemble and types of ensemble	4	CO1
Q.4	Discuss the variation of the fermi probability function, $f(\epsilon)$ with energy, ϵ at different temperatures.	4	CO1
Q.5	Three distinguishable particle have to be accommodated in four available states. Find the number of ways in which this can be done if the particles obey M-B statistics.	4	CO1

SECTION B
(4Qx10M= 40 Marks)

Q.6	Consider a system of N particles and a phase space consisting of only two states with energies 0 and, ϵ . Calculate the partition function and the internal energy.	10	CO2
Q.7	Consider the system of N elements with two non-degenerate energy levels ϵ_1 and ϵ_2 where ϵ_2 is the excited state. Apply the classical approach to show that the heat capacity at constant volume, C_v is given by $C_v = N k_B \left(\frac{\Theta}{T} \right)^2 \frac{e^{\frac{\Theta}{T}}}{\left(1 + e^{\frac{\Theta}{T}} \right)^2}$ where, $\Theta = \frac{\epsilon}{k_B}$ is called characteristic temperature.	10	CO3
Q.8	Apply Bose-Einstein statistics to photon gas and derive the Planck's law for the spectral distribution of energy in black body radiation.	10	CO3
Q.9	Calculate the number of modes in a chamber of volume 1m^3 in the frequency range 0.6×10^{14} Hz to 0.61×10^{14} Hz.	10	CO2

SECTION-C
(2Qx20M=40 Marks)

Q.10	<p>Derive Sackur Tetrode equation for the entropy of an ideal gas. How does it resolve the Gibb's paradox?</p> <p style="text-align: center;">OR</p> <p>Consider the non-relativistic electron gas with electron density, n. Demonstrate that the total internal energy of a non-relativistic fermion system is greater than that predicted classically. Mention the reason behind it.</p>	20	CO4
Q.11	<p>(a) Explain the Bose-Einstein condensation. How does it differ from ordinary condensation? Obtain an expression for the critical temperature at which this phenomenon sets in.</p> <p>(b) Show that the distribution function of the Bosons for the most probable macrostate is given by $n_s = \frac{g_s}{e^{\alpha + \beta \epsilon_s} - 1}$ where α and β are the Lagrange multipliers.</p>	10 10	CO2 CO3