

Name:	
Enrolment No:	

**UNIVERSITY OF PETROLEUM AND ENERGY STUDIES**  
**End Semester Examination, December 2022**

**Course: Quantum Mechanics and Applications**  
**Course Code: PHYS3001**  
**Programme: BSc Physics (H)**  
**Total pages: 2**

**Semester: V**  
  
**Max. Marks: 100**  
**Time: 03 hrs.**

**Instructions:**

- All questions are compulsory (Q8 and Q11 have internal choice)

**SECTION-A**

S. No.		Marks	CO
Q1.	For a given wavefunction, $\psi = \sqrt{2/L} \sin(\pi x/L)$ , calculate probability between 0 to L/2 (a)1, (b) 1/3, (c)1/2, (d) 1/5 (choose correct one)	4	CO1
Q2.	Choose correct difference between energy Eigen values of 1D harmonic oscillator for (n+1) <sup>th</sup> and n <sup>th</sup> states, (a) $\frac{\hbar\omega}{2}$ , (b) $2\hbar\omega$ , (c) $3\hbar\omega$ , (d) $\hbar\omega$ .	4	CO1
Q3.	The correct commutator relation is (a) $[x, p_x] = i\hbar$ , (b) $[L^2, L_x] = 0$ , (c) both are correct, (d) none.	4	CO2
Q4.	Kinetic energy of an electron whose de-Broglie wavelength, $\lambda = 0.1$ nm is (a)100 eV, (b)150 eV, (c)175 eV, (d)200 eV.	4	CO3
Q5.	Lande g factor for the state $3^2D_{5/2}$ is (a) 2/3, (b) 6/5, (c) 5/3, (d) 4/3 (choose correct one).	4	CO4

**SECTION-B**

Q6.	Prove that Eigen values of Hermitian operators are real.	10	CO1
Q7.	Evaluate most probable position for the state, $\psi(x) = Nxe^{-(\alpha^2 x^2/2)}$ , where $\alpha =$ constant, and N = normalization constant.	10	CO2

Q8.	Write short note on  (a) LS coupling  <b>OR</b>  (b) Paschen Back effect	<b>10</b>	<b>CO2</b>
Q9.	For a given wavefunction, $\Phi = Ae^{2i\varphi}$ , where A = constant, Calculate Eigen value of $L_z$ operator.	<b>10</b>	<b>CO3</b>

**SECTION-C**

Q10.	(a) What is spin-orbit interaction? Find the relation between <b>B</b> (magnetic field) and <b>L</b> (orbital angular momentum).  (b) Discuss Stern-Gerlach experiment for space quantization.	<b>10</b>  <b>10</b>	<b>CO3</b>  <b>CO3</b>
Q11.	(a) Sketch Zeeman transition levels neatly for the atomic transition, 3d→2p.  (b) What is space quantization? Calculate total angular momentum J and total magnetic moment $\mu_J$ for the state, $^2P_{3/2}$  <b>OR</b>  (a) Solve Schrodinger equation in spherical polar co-ordinates for radial part to obtain energy Eigen value of hydrogen atom of the form, $E_n = -\frac{me^4}{32\pi^2\epsilon_0^2\hbar^2n^2}$  (b) Find average radius ( $\langle r \rangle$ ) the ground state of hydrogen atom, $\psi_{100}(r) = \frac{1}{\sqrt{\pi a_0^3}} e^{-r/a_0}$	<b>10</b>  <b>10</b>  <b>10</b>  <b>10</b>	<b>CO4</b>  <b>CO4</b>  <b>CO4</b>  <b>CO4</b>

Physical constants:  $h = 6.63 \times 10^{-34} \text{ J-s}$ ,  $c = 3 \times 10^8 \text{ m/s}$ ,  $a_0 = \text{Bohr radius} = 0.53 \text{ \AA}$ ,  $\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$ ,  $\epsilon_0 = 8.854 \times 10^{-12} \text{ F/m}$ , mass of proton =  $1.6726 \times 10^{-27} \text{ Kg}$ , mass of electron =  $9.1 \times 10^{-31} \text{ Kg}$