


<b>Name:</b>	
<b>Enrolment No:</b>	

## UNIVERSITY OF PETROLEUM AND ENERGY STUDIES

**End Semester Examination, December 2018**

<b>Programme Name:</b> B.Tech Mechanical Engineering	<b>Semester :</b> I
<b>Course Name :</b> Physics	<b>Time :</b> 03 hrs
<b>Course Code :</b> PHYS 1005	<b>Max. Marks:</b> 100
<b>Nos. of page(s) :</b> 02	

**Instructions:** 1. In section A, all questions are compulsory. In section B, questions 6, 7 and 8 are compulsory, while question 9 have choice. In section C, question 10 is compulsory while Q 11 have a choice.

2. All bold letters are vectors.

3. The value of constants are given in table.

Quantity	Values
Magnetic constant (vacuum permeability) ( $\mu_0$ )	$1.25 \times 10^{-6} \text{ N}\cdot\text{A}^{-2}$
Electric constant (vacuum permittivity) ( $\epsilon_0$ )	$8.85 \times 10^{-12} \text{ F}\cdot\text{M}^{-1}$
Elementary charge	$1.60 \times 10^{-19} \text{ C}$

### SECTION A

S. No.	Question	Ma rks	CO
Q 1	Let $\rho_v = (x+2y+3z) \frac{C}{m^3}$ in the cubical region $0 \leq x, y, z \leq 1\text{mm}$ and $\rho_v = 0$ outside the cube. What is the total charge contained within the cube.	4	CO2
Q 2	The temperature variation inside the earth can be assumed to be spherically symmetric and approximately described by the following equation: $T(r) = T_0 - \alpha r^2$ , where r is the distance measured from the center of the earth. Calculate the gradient of T?	4	CO1
Q 3	Write the Maxwell's Equations with their physical significance.	2+2 =4	CO4
Q 4	Define the Laplacian of a scalar field. Find the Laplacian of the scalar field. $U = \rho^2 z \cos\phi$	1+3 =4	CO2
Q 5	Explain the polarization in polar and nonpolar dielectrics	2+2 =4	CO3

### SECTION B

Q 6	(a) Let $V = x^2y^2z$ in a region ( $\epsilon = 2\epsilon_0$ ) defined by $-1 < x, y, z < 1$ . Find the charge density $\rho_v$ in the region.	5+5 =10	CO3
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	(b) If the charge travels at $10^4 \mathbf{a}_y$ m/s, determine the current crossing surface $0 < x, z < 0.5, y = 1$ .		
Q.7	State and prove the Poynting's theorem. Discuss the physical significance of each term in the resulting equation.	2+5 +3= 10	CO5
Q 8	Define the electric fields due to continuous charge distributions. Derive the expression for the electric field due to surface charge.	3+7 =10	CO3
Q 9	<p>What are boundary conditions? Prove that, in case of dielectric- dielectric medium, the tangential components of electric field is continuous and normal component of <math>\mathbf{E}</math> is discontinuous at the boundary</p> <p style="text-align: center;"><b>OR</b></p> <p>Region 1 (<math>z &lt; 0</math>) contains a dielectric for which <math>\epsilon_r = 2.5</math>, while region 2 (<math>z &gt; 0</math>) is characterized by <math>\epsilon_r = 4</math>. Let <math>\mathbf{E}_1 = -30\mathbf{a}_x + 50\mathbf{a}_y + 70\mathbf{a}_z</math> V/m and find: (a) <math>\mathbf{D}_2</math> (b) <math>\mathbf{P}_2</math> (c) the angle between <math>\mathbf{E}_1</math> and the normal to the surface.</p>	2+4 +4= 10	CO2
<b>SECTION C</b>			
Q. 10	<p>[i] State the Faraday's law. Explain the variation of flux with time in cases (a) by having a stationary loop in a time-varying B field (b) by having a time-varying loop area in a static B field.</p> <p>[ii] A parallel-plate capacitor with plate area of <math>5 \text{ cm}^2</math> and plate separation of 3 mm has a voltage <math>50 \sin 10^3 t</math> volt applied to its plates. Calculate the displacement current assuming <math>\epsilon = 2\epsilon_0</math>.</p>	2+4 +4= 10	CO4  CO5
Q. 11	<p>[i] Discuss the reflection and transmission coefficient. Explain the reflection of EM wave by a perfect dielectric. Polystyrene has a relative permittivity of 2.56. If a wave is incident at an angle of <math>\theta_i = 35^\circ</math> from air to polystyrene. Calculate the angle of transmission <math>\theta_t</math>.</p> <p>[ii] Derive wave equations for electric and magnetic fields and find the velocity of an electromagnetic wave in a lossless medium.</p> <p style="text-align: center;"><b>OR</b></p> <p>[i] Find the reflection coefficient and transmission coefficient of an electric field wave travelling in air and incident normally on a boundary between air and a dielectric having permeability <math>= \mu_0</math> and permittivity <math>\epsilon_r = 4.74</math></p> <p>[ii] Define the momentum carried by electromagnetic wave. Derive its expression also.</p>	10+ 10 = 20	CO6

## CONFEDENTIAL

<b>Name of Examination</b> <small>(Please tick, symbol is given)</small>	:	MID		END	<input type="checkbox"/>	SUPPLE	NA
<b>Name of the School</b> <small>(Please tick, symbol is given)</small>	:	SOE	<input type="checkbox"/>	SOCS		SOP	
<b>Programme</b>	:	B.Tech Mechanical Engineering					
<b>Semester</b>	:	First Semester					
<b>Name of the Course</b>	:	Physics					
<b>Course Code</b>	:	PHYS 1005					
<b>Name of Question Paper Setter</b>	:	Dr Rajeev Kumar Gupta					
<b>Employee Code</b>	:	40000040					
<b>Mobile &amp; Extension</b>	:	9897716629, 1414					
<b>Note: Please mention additional Stationery to be provided, during examination such as Table/Graph Sheet etc. else mention "NOT APPLICABLE":</b>							
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**Note: - Pl. start your question paper from next page**

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**SECTION A**

S. No.		Marks	CO
Q 1	Find the total charge in the volume defined by $0 \leq x \leq 1\text{m}$ , $0 \leq y \leq 1\text{m}$ , $0 \leq z \leq 1\text{m}$ , if $\rho_v = 120x^2y \frac{\mu\text{C}}{\text{m}^3}$ .	4	CO2
Q 2	Using cylindrical co-ordinates show that: $[\nabla \times (\nabla V)]_\rho = 0 = [\nabla \times (\nabla V)]_\phi$	4	CO1
Q 3	Define the Laplacian of a scalar field. Find the Laplacian of the scalar field $P = 10r \sin^2\theta \cos \phi$	4	CO1
Q 4	The potential field $V = 2x^2yz - y^3z$ exists in a dielectric medium having $\epsilon = 2\epsilon_0$ . Does V satisfy Laplace's equation?	4	CO2
Q 5	Write Maxwell's equations for time varying field.	4	CO4

**SECTION B**

Q.6	Derive the Continuity equation $\text{div } \mathbf{J} + \frac{\partial \rho}{\partial t} = 0$ and write its physical significance. Prove that the volume charge density decays exponentially with a time constant.	10	CO5
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Q.7	Given the magnetic vector potential $\mathbf{A} = -\rho^2/4 \mathbf{a}_z$ Wb/m, calculate the total magnetic flux crossing the surface $\phi = \pi/2$ , $1 \leq \rho \leq 2$ m, $0 \leq z \leq 5$ m.	10	CO3
Q 8	[i] Calculate the value of Poynting's vector at the surface of the sun if the power radiated by the sun is $3.8 \times 10^{26}$ watt while its radius is $7 \times 10^8$ m.  [ii] If the average distance between the sun and the earth is $1.5 \times 10^{11}$ m, show that the average solar energy incident on the earth is $2 \text{ cal/cm}^2$	10	CO5
Q 9	Define the magnetic materials and explain its two properties. What is the Faraday's law? Explain it by having a time-varying loop area in a time-varying B field.  <b>OR</b> A long solenoid of diameter 0.1 m has $2 \times 10^4$ turns per meter. At the center of the solenoid, a 100 turn coil of radius 0.01 m is placed with the axis coinciding with the solenoid axis. The current in the solenoid is decreased at a constant rate from 2A to -2 A in 0.5 seconds. Find the emf induced in the coil. Also, find the total charge flowing through the coil during this time when the resistance of the coil is $10\pi^2$ ohm.	10	CO4
<b>SECTION-C</b>			
Q. 10	[i] Explain the concept of displacement current. Show that for a conductor subject to electric field $E = E_0 \cos \omega t$ , displacement current density is negligible at a frequencies less than $10^{15}$ c/s  [ii] Find the vector potential of an infinite solenoid with n turns per unit length, radius R, and current I.	10+10 = 20	CO2 CO3
Q. 11	[i] Assume a plane wave with $E = 1 \text{ V/m}$ and a frequency of 300 MHz moving in a free space, impinges on a thick copper located perpendicularly to the direction of propagation. Find the value of E and H.  [ii] Define the electromagnetic wave. Prove that the wave equation for E and H are $\nabla^2 E = \mu\epsilon \frac{\partial^2 E}{\partial t^2}$ and $\nabla^2 H = \mu\epsilon \frac{\partial^2 H}{\partial t^2}$ .  <b>OR</b> Define the reflection and the transmission of the EM wave. Prove that for the EM wave, parallel polarization $\frac{E_r}{E_i} = \frac{\tan(\theta_i - \theta_t)}{\tan(\theta_i + \theta_t)}$ and for perpendicular polarization $\frac{E_r}{E_i} = \frac{\sin(\theta_t - \theta_i)}{\sin(\theta_t + \theta_i)}$ .	20	CO6