

**DEVELOPMENT OF GPS AND OBSTACLE AVOIDANCE  
BASED LOW ALTITUDE NAVIGATION SYSTEM FOR A  
POWERED PARACHUTE AERIAL VEHICLE**

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THE DEGREE OF DOCTOR OF PHILOSOPHY**

To

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June, 2015

**THESIS COMPLETION CERTIFICATE**

This is to certify that the thesis on “**Development of GPS and Obstacle Avoidance Based Low Altitude Navigation System for A Powered Parachute Aerial Vehicle**” by Vindhya Devalla in Partial completion of the requirements for the award of the Degree of Doctor of Philosophy is an original work carried out by her under my supervision and guidance.

It is certified that the work has not been submitted anywhere else for the award of any other diploma or degree of this or any other University.

  
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***Vindhya Devalla***  
*University of Petroleum and Energy Studies*  
*June 2015*

DEDICATED TO  
MY PARENTS  
& ALMIGHTY

## **DECLARATION**

I do hereby declare that this submission is my own work and that, to the best of my knowledge and belief, it contains no material previously published or written by another person nor material which has been accepted for the award of any other degree or diploma of the university or other institute of higher learning, except where due acknowledgment has been made in the text.

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## **EXECUTIVE SUMMARY**

Unmanned Aerial Vehicle is an aircraft with no on board pilot. UAVs can be controlled with remote or autonomously. They are used for number of different missions depending upon the application. There are different types of UAVs available like fixed wing, multi copter and Parafoil UAV. Certain characteristics like low speed, high payload carrying capability, etc. makes Parafoil UAV a versatile platform for various applications.

Parafoil is entirely made of fabric and is a non- rigid wing. A Parafoil get inflated just like a parachute when dropped from a height. The wing has a low aspect ratio with an elliptical or a rectangular plan form when inflated. To act as an airfoil, the upper membrane and the lower membrane are sewn together with a gap between both. The leading edge is kept open so as to allow the air inside the cells creating air pressure, which maintains the shape of the Parafoil as a wing. The vents in the ribs allow the air pass from one cell to another which helps in maintaining uniform air pressure in the wing. To avoid the air loss the fabric is made of non-porous material. The suspension lines are used to connect the Parafoil to the payload. Addition of a Propulsion unit on the payload makes the Paraglider a Parafoil UAV. This Vehicle has a “Fly-bar” to which the Parafoil is connected and a motor on the Payload.

Directional control is achieved by pulling the fly-bar either side, which changes the direction of the lift making the aircraft turn. The Powered Parafoil has a tendency to fly at constant airspeed. These systems have pendulum stability and oscillations, because of the mass of the airframe suspended significantly below the canopy, which allows the system to have a yaw motion rather than roll motion. Lateral control is obtained by the propulsion system which is attached to

the payload. The thrust of the propulsion system is controlled to maintain the altitude, take-off or landing.

Modeling of Parafoil UAV has been studied in detail in this work. A new direction control scheme was developed using a 9 DOF model with a single servo which is connected to “fly-bar” and tilts the Parafoil left and right. Complete Parafoil payload system performance has been studied by open loop simulation and open loop flight test results. These results are then used to develop a closed loop control system for autonomous way point navigation. The Parafoil UAV has inherent pendulum stability due to which simple controller schemes were designed. A Single servo is used for direction control and a Single BLDC motor is used for takeoff, landing and level flight, due to which, the control system design became simpler.

This work focusses on developing a GPS and Obstacle avoidance based low altitude navigation system for a Parafoil UAV. The vehicle would follow a planned trajectory for following the path effectively. This work presents guidance, navigation and control of a Parafoil UAV. Lateral heading and longitudinal altitude hold controller has been designed. A path planning algorithm is also designed for following a trajectory using way point navigation. The lateral heading and longitudinal altitude hold controllers have been verified by the actual flight parameters.

Parafoil UAV being a low speed UAV can be widely used for remote sensing, aerial surveillance and precision delivery applications. The Aerial photographs taken using this system would be precise and very clear. Such a system with autonomous navigation capability can be used for low altitude remote sensing especially oil and gas pipeline monitoring. A benefit of the Parafoil UAV for unmanned aircraft use is their unique ability to glide to the ground in a relatively safe manner, even if all control systems are disabled. This is particularly desirable in urban environments where a failure of any large UAV would likely result in collateral damage to structure on the ground. Powered Parafoils, on the other

hand, would be unlikely to land with a vertical speed above 10mps, without making severe damage to any ground edifice or even the airframe itself is unlikely.

## NOMENCLATURE

- $A, B, C$  = apparent mass terms
- $A^*$  = canopy aspect ratio
- $b$  = canopy span
- $d$  = diameter of a suspension line
- $C_D$  = drag coefficient
- $C_L$  = lift coefficient
- $C_Y$  = side force coefficient
- $C_{lp}, C_{lr}$  = rolling moment damping coefficient
- $C_{mc/4}$  = pitching moment coefficient at quarter chord
- $C_{mq}$  = pitching moment damping coefficient
- $C_{nr}, C_{np}$  = yawing moment damping coefficients
- $c$  = canopy chord length
- $F$  = force
- $g$  = acceleration due to gravity
- $h, h^*$  = canopy span wise camber height, and  $h/c$  ratio, respectively
- $I$  = inertia matrix
- $I_A, I_B, I_C$  = apparent inertia terms
- $M$  = mass matrix
- $L$  = length of control line pulled
- $m$  = mass
- $q(\text{bar})$  = dynamic pressure
- $p, q, r$  = roll, pitch and yaw rates
- $R$  = link length

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# CHAPTER 1

## INTRODUCTION

Unmanned Aerial Vehicles commonly known as drones are aircrafts without human pilot on-board. In past the high resolution remote sensing images were taken by manned airplanes or helicopters. But there are some disadvantages, e.g. under special weather conditions (e.g. low clouds) or when airstrip is blocked, the airplanes cannot be used. Technological advances have allowed engineers to develop unmanned aerial vehicles which have an increasing demand in military, remote sensing, surveillance, etc.

### 1.1 UNMANNED SYSTEMS

The U.S Department of Defense (DOD) defines an unmanned aircraft as follows [1]:

*“A powered vehicle that does not carry a human operator, can be operated remotely or autonomously, can be expendable or recoverable and can carry a lethal or non-lethal payload. Ballistic or semi ballistic vehicle, cruise missiles, artillery projectiles, torpedoes, mines, satellites and unattended sensors are not considered unmanned vehicles. Unmanned vehicles are the primary component of unmanned system.”*

This definition covers multiple forms of unmanned systems including Unmanned Air Systems (UASs), unmanned ground vehicles (UGV), unmanned surface vehicles (USVs), and unmanned underwater vehicles (UUVs).

The definition excludes sensors with no form of propulsion. This exclusion is likely intended to eliminate son buoys and unattended ground sensors (UGS).

Non-powered aircraft, known as gliders, can perform many useful missions and are generally considered to be UAS. They have flight controls which are capable of navigation, and carry payloads. One could argue that a glider's propulsion is the conversion of potential to kinetic energy [2]. UASs have taken many names and forms over their long history can be called in many ways:

- Remotely piloted vehicle
- Unmanned aerial vehicle
- Uninhabited combat aerial vehicle
- Organic aerial vehicle
- Aerial robotics
- Micro aerial vehicle

General attributes of unmanned aircraft are following:

- Smaller size potential
- High versatility
- Greater performance than manned aircraft
- Uninhabited combat aircraft system
- Remotely piloted aircraft
- Remotely piloted helicopter

## **1.2 TYPES OF UNMANNED AERIAL VEHICLES**

A Short Overview of different types of Unmanned Aerial vehicles (UAV) is given. The first remote controlled UAV was developed for military use called drones. UAV generally consist two systems namely, Unmanned Aircraft and Control Station. There is a wide range of UAVs available from small vehicles

with less than 0.8kg (e.g. Sensefly) to very large vehicles with the flight weight more than 900kg (e.g. B-Hunter). The different types of UAVs can be classified as: multi-rotor, fixed wing and Parafoil UAV [3].the classification can be done on weight, height and construction

### 1.2.1 Multi-copter types

Helicopters or multiple copter type UAVs come into this category, which have vertical rotors without any airstrip. The lift is created actively by the whole body which consumes lot of battery having limited flight time and height [4]. Payload constraints are most common in these UAVS.



Figure 1.1. A Multi- Copter UAV [2]

The characteristics of these systems are given below:

- Vertical takeoff and landing (VTOL).
- Equipped with vertical rotor, No runway is needed.
- No dynamic lift is created by wings, the whole lift has to be created actively, which consumes much battery, therefore the flight time and height is limited.
- Heavy payload cannot be carried.
- Need advanced gyro compass and sensors which assist the flight.

### 1.2.2 Fixed wing types



Figure 1.2. A Fixed Wing UAV [2]

These aircrafts are similar to the traditional aircraft design. Most of the lift is created by the wings leading to long flight time [5]. These UAVs can carry good payload compared to multi copter types

The characteristics of these systems are given below:

- Design similar to classical aircrafts
- Runway is needed for landing
- Dynamic lift created by wing, therefore, long flight time
- Can carry higher payload
- High speed
- Can operate under strong wind conditions
- Advanced autopilots are needed
- High landing speed, therefore slight mistake during landing cause severe damage
- Higher expertise needed to operate compared to multi copter

### 1.2.3 Parafoil UAV

These type of UAVs are very robust and easy to fly due to the design as Parafoil as the wing and very safe in case of system crash. Due to the low speed, the images taken using this UAV are very clear [6].



Figure 1.3. A Powered Parafoil UAV [2]

The characteristics of these systems are given below:

- Can carry high payloads
- Long flight time
- Low flight speed
- Very robust
- Easy to fly
- Very safe in the case of system failure
- Cannot be operated in rainy conditions sensitive to wind condition

### **1.3 PARAFOIL UNMANNED AERIAL VEHICLE**

The Powered Parafoil is an aircraft which derives lift from a ram-air inflated canopy, under which the fuselage is suspended. The Parafoil is inflated by the dynamic pressure of the air flowing into the canopy which has a cross section in the shape of an airfoil. This process helps the vehicle to create lift. This feature differentiates these Parafoils from conventional Parafoils which are used to simply create drag. Powered Parafoils have been utilized mostly for recreation activities, but some of the special properties make them a suitable platform for unmanned aerial vehicle (UAV) and remote sensing applications. Powered Parafoils have existed since 1981 [7]. The concept was introduced at the Sun & Fun aviation event by the ParaPlane Corporation as seen in figure 1.4.



Figure 1.4. ParaPlane Corporation first model [7]

They represent aircraft that are somewhere between balloons and fixed wing aircraft when control is considered as shown in figure 1.5. The direction of a powered Parafoil is controlled by the pilot rotating on either a left or right steering bar that pulls down a line attached to the trailing edge of the canopy. The increased drag causes the aircraft to turn. The control lines connected to the canopy are pulled down together, which will drop both trailing ends of the canopy at a time and cause a sudden increase in lift.

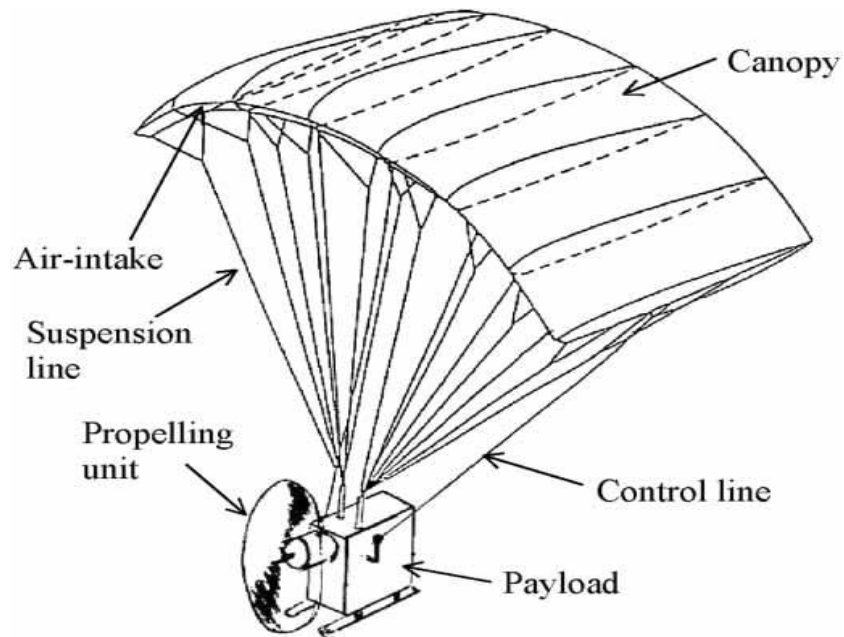


Figure 1.5. Control Surfaces of Powered Parafoil UAV [8]

This maneuver is done during landing, when the pilot wants a smooth touchdown. A different steering configuration which is used on some small-scale aircraft is known as a “fly-bar.” In this design, the Parafoil is connected to the ends of a bar and the bar is tilted, tilting the Parafoil, as seen in figure 1.6.

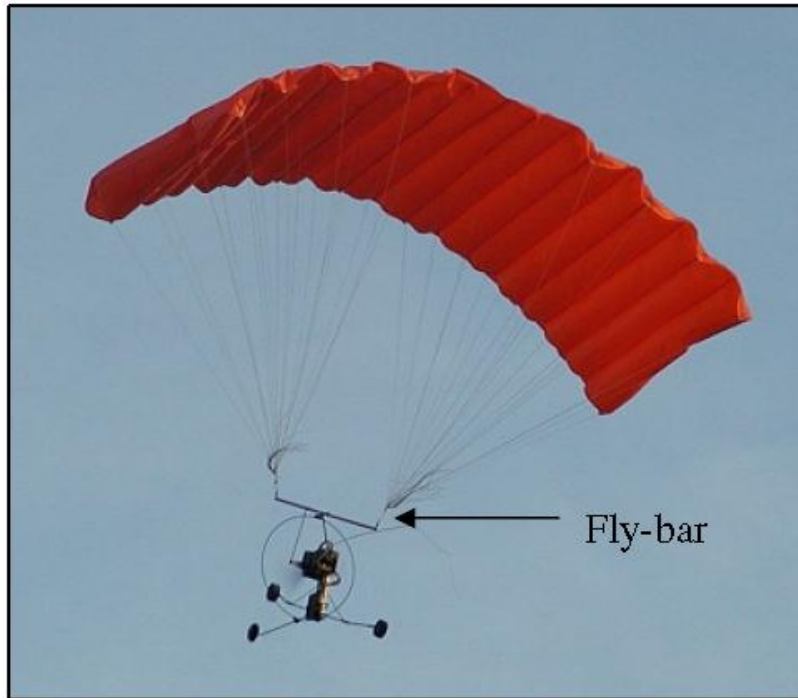


Figure 1.6. Alternate steering in Powered Parafoil [8]

This bar can be tilted either side of the aircraft, changing the direction of the lift and making the aircraft turn. Aircraft using each of the two steering systems behave identically in response to thrust inputs. Powered Parafoils have the tendency to fly at a constant airspeed [8]. A powered Parafoils will climb, cruise and descend somewhere around the speed of 26 – 32 MPH. These Aircrafts have pendulum stability and oscillations as shown in the figure 1.7, because of the mass of the airframe suspended significantly below the canopy. The applications powered Parafoil in surveillance and imaging has benefit of a low-speed, low-cost, and stable platform which is capable of lifting payloads of up to 600 lbs. These platforms are very stable and must only get disturbed with gusts that would change the flight trajectory.



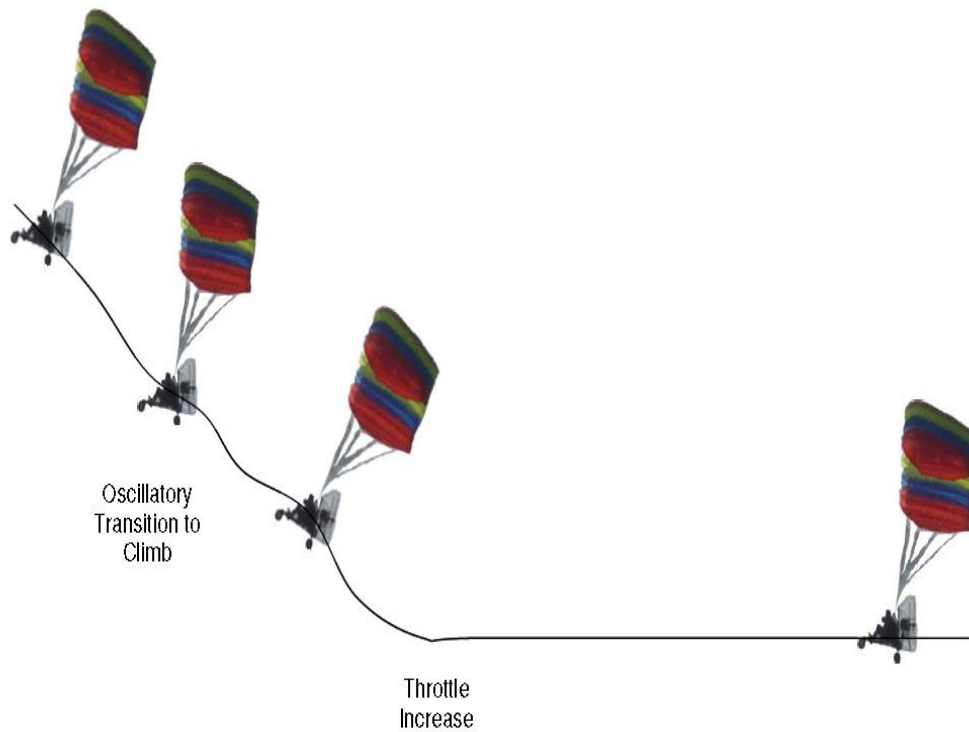


Figure 1.7. Oscillations in Powered Parafoil while takeoff [8]

The addition of a propelling unit makes the paraglider an Unmanned Aerial Vehicle (UAV). A Powered Parafoil consists of a Parafoil and a payload equipped with an engine or motor and a propeller. From the view of dynamics and control, the configuration provides the following unique characteristics, as compared to traditional wing aircraft [8].

- The separation between the centers of gravity of the canopy and the payload produces a swinging motion.
- Changing the thrust induces a considerable pitching motion.
- Relative pitching and yawing motions exists between the canopy and the payload.
- Canopy is a tailless flying wing.

- Directional control is mainly achieved through yawing motion, rather than through rolling motion.
- The apparent mass of the canopy must be taken into account, as in case of an airship.

## **1.4 TERMS USED IN POWERED PARAFOIL AERIAL VEHICLE**

### **1.4.1 Airfoil**

The Surface of the Parafoil which is used to produce lift, typically, the canopy itself is called as airfoil [9].

### **1.4.2 Camber**

The curvature of the wing is called as camber. A Parafoil has two cambers namely upper camber and lower camber [9].

### **1.4.3 Leading edge**

Leading edge refers to the forward edge of the Parafoil [9].

### **1.4.4 Trailing edge**

Trailing edge refers to the rear edge of the Parafoil [9].

### **1.4.5 Chord line**

Chord line is the imaginary line joining trailing edge and the leading edge [9].

### **1.4.6 Relative wind**

Relative wind is the direction of airflow with respect to the wing, which is generally opposite and parallel to the flight path of the Parafoil [9].

### **1.4.7 Angle of attack**

Angle between the relative wind and the chord line is known as Angle of attack [9].

### 1.4.8 Longitudinal axis

Longitudinal Axis is the vertical axis of a powered Parafoil Aerial vehicle; it is also called as roll axis [9].

### 1.4.9 Angle of incidence

Angle between the chord line and the longitudinal axes is known as angle of incidence [9].

### 1.4.10 Trim angle

Trim angle is the angle between the Chord line and the horizontal plane of the powered Parafoil when the vehicle is in unpowered condition [9].

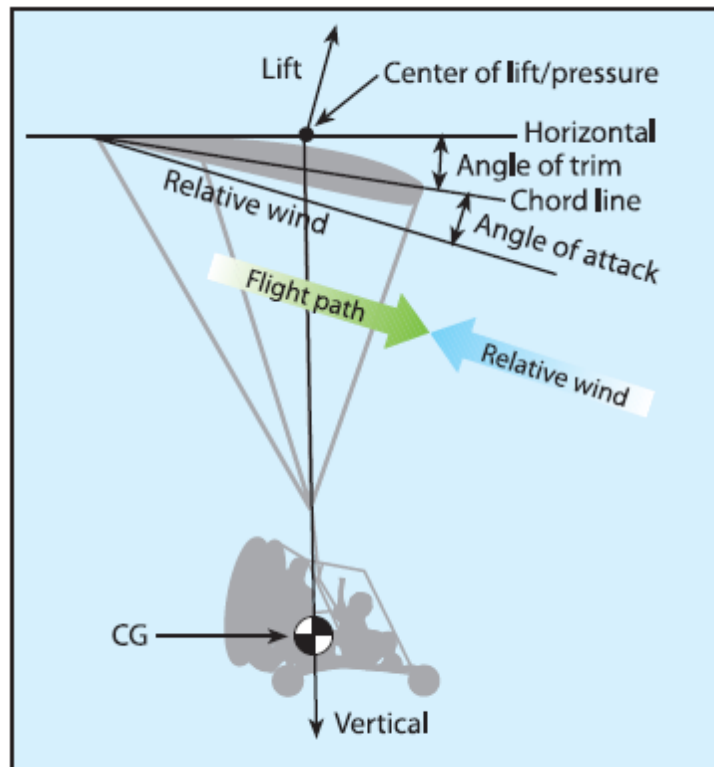


Figure 1.8. Angle of Attack [9]

### 1.4.11 Pitch angle

Pitch angle is the angle between wing chord to the horizontal plane [9].

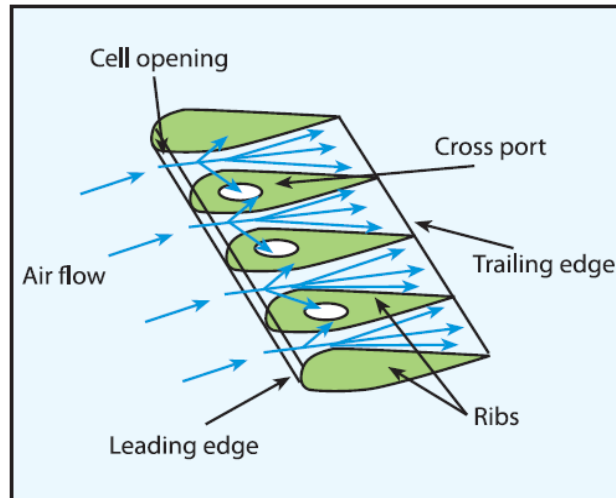


Figure 1.9. Air Flow into the Wing [9]

#### 1.4.12 Aspect ratio

Ratio of wing span by average chord line gives the aspect ratio. More the aspect ratio more will be lift with less induced drag [9].

#### 1.4.13 Wing loading

The total weight the wing can support is known as Wing loading, this can be found by dividing the total weight of the aircraft by the total area of the wing [9].

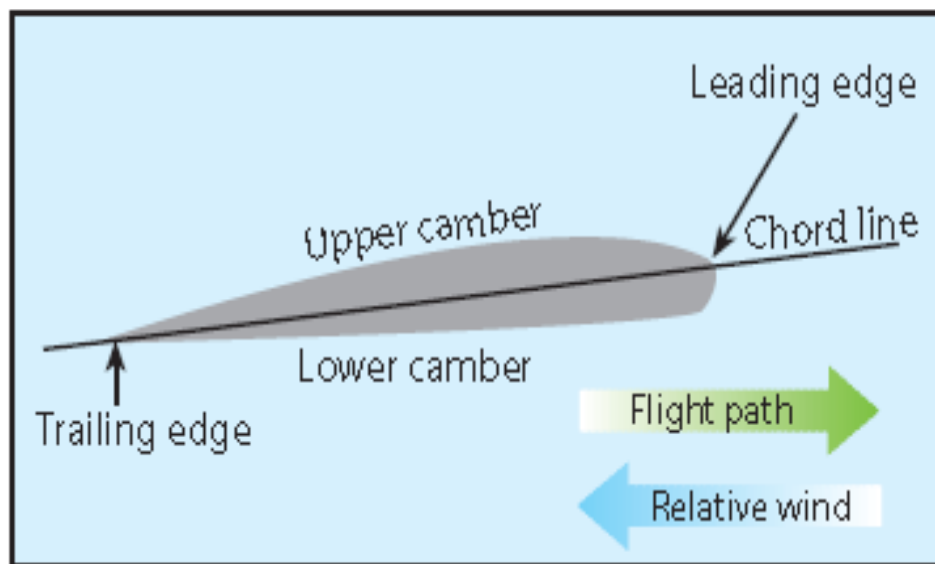


Figure 1.10. Aerodynamic terms of an Airfoil [9]

## 1.5 AERODYNAMICS OF A POWERED PARAFOIL AERIAL VEHICLE

### 1.5.1 Ram Air Parafoil

The powered Parafoil wing retains the rigid shape during the flight because of air pressure. These aircrafts are no different from the conventional aircrafts as both of them have top skin, bottom skin, leading edge and trailing edge. Also they have upper surface curved and lower comparatively flatter. The only difference is fabric and opening in the leading edge. The fabric prevents the air from escaping as it is made of zero porosity material. Once the canopy is filled with air, excess outside air cannot enter the pressurized wing. This results in forming aerodynamically correct and stiff wing

### 1.5.2 Lift, Weight, Thrust, Drag

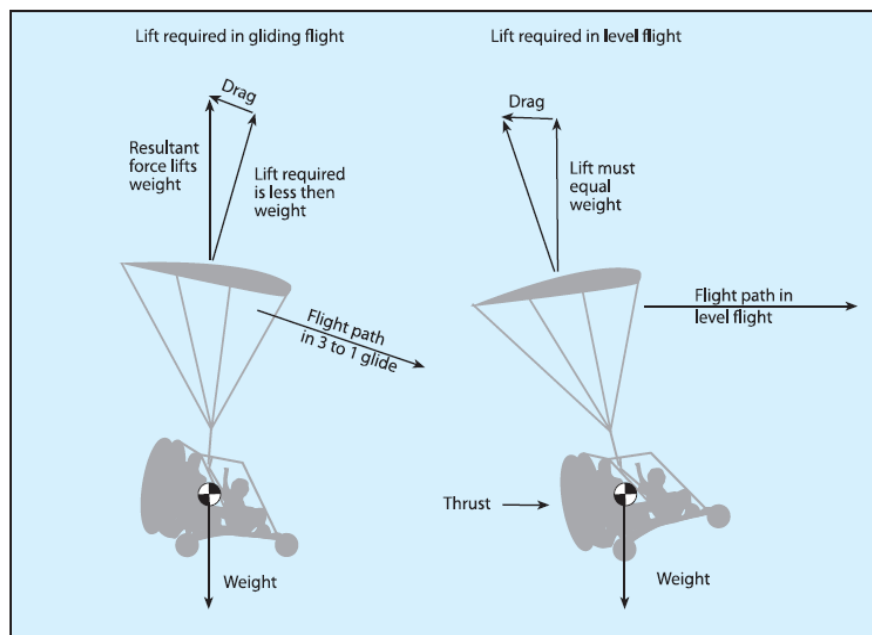


Figure 1.12. Different forces for gliding and level flight [9]

In a level and straight flight condition lift is equal to weight and thrust is equal to drag. With the curved upper surface and flat lower surface moves through the air, it forces the air to flow around it resulting in faster air flow on the upper surface and lower airflow at the lower surface. Air travelling with high

velocity creates low pressure and low velocity creates high pressure. Therefore, high pressure at the lower surface generates lift.

Weight is produced by the gravity equal to weight of the instruments on board and the craft's weight.

When lift is greater than weight and thrust is greater than drag the vehicle will climb up. When lift is less than weight and thrust is less than drag, vehicle will descend down. The thrust is produced by the propulsion system attached to the vehicle. Drag is produced by the resistance due to the chute, lines, vehicle and the steering bar.

### 1.5.3 Throttle Control

Throttle controls the climb and descend of the vehicle by changing the angle of attack of the wind. The rate of climb is controlled by the throttle setting.

### 1.5.4 Pendulum Stability

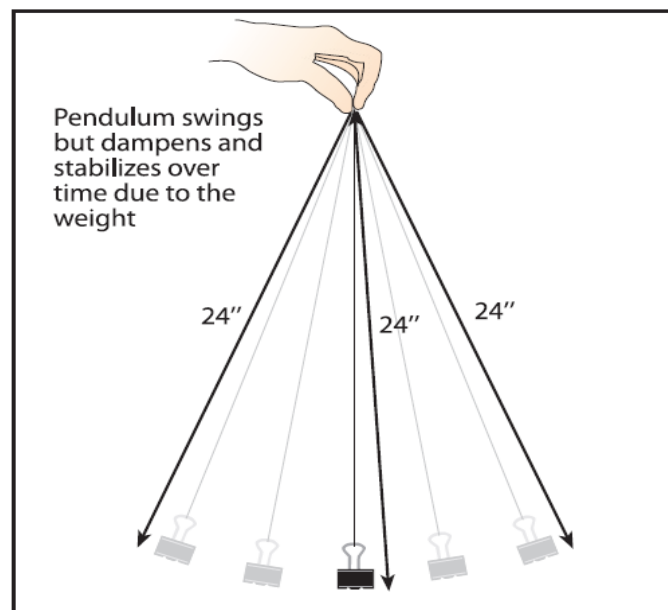


Figure 1.13. Pendulum Effect [9]

A pendulum consists of a suspension point with the weight attached to other end. In case of a powered Parafoil vehicle the canopy acts as a suspension point and

the vehicle act as the weight. When the weight is moved to and fro it tries to swing to get back to its original stable point. An object is said to be stable when it get backs to its original point after subjected to disturbances. When the controls are released the stable aircraft tries to return back to the level flight. Likewise, whenever a wind gust moves the powered Parafoil due to payload weight it tries to get back to the original position which can be called as natural stability.

### 1.5.5 Effect of Wind Gusts on Pendulum Stability

A side gust will move the canopy to side first and vehicle will move back to the center due to pendulum stability.

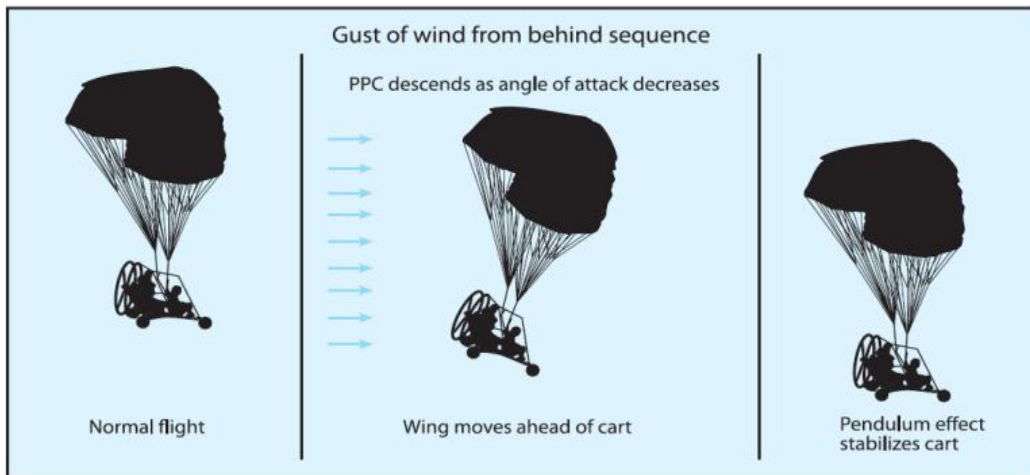


Figure 1.14. Powered Parafoil Stability after backward Wind Gust [9]

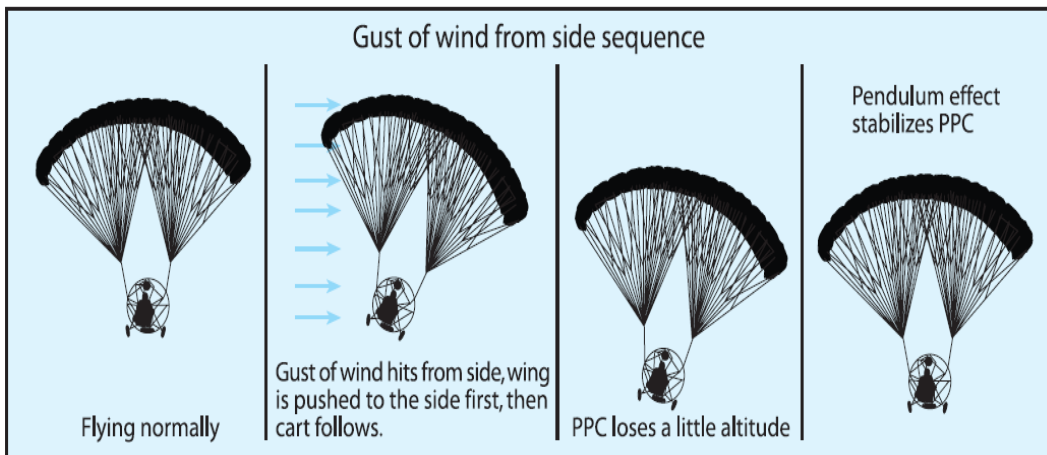


Figure 1.14. Powered Parafoil Stability after Side Wind Gust [9]

A gust of wind will move the canopy backward resulting in lift and after some time the vehicle will come back to the center resulting in reduced angle of attack, which tends to descend the vehicle down again the vehicle, will try to relocate to center of the suspension resulting in level flight.

A gust of wind from backside tries to descend the vehicle, but due to the pendulum effect the when vehicle tries to come back to the stable state angle of attack is increased resulting in lift and vehicle centers itself again and level flight is continued.

### 1.5.6 Axes of movement: Yaw Pitch and Roll

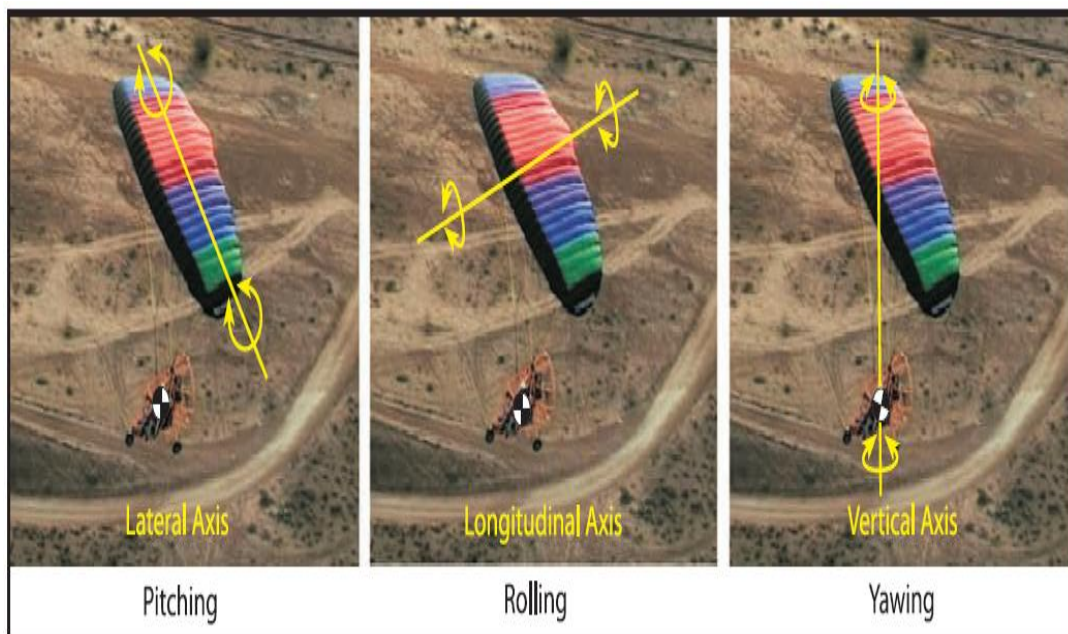


Figure 1.15. Powered Parafoil Axes of Rotation [9]

The Pendulum effect control the longitudinal and lateral or pitch and roll axes, the vehicle must be only programmed to control vertical or yaw axes. To turn the steer bar is pulled down to one of the side. The pitch movement is automatically controlled by the wind gusts. The throttle control can also control pitch moments for climb and descent. This simple control makes the Parafoil easy to fly.



### 1.5.7 Steering Controls

The steering is accomplished by pulling the control string using the steering bar connected to a servo motor.

Whenever the servomotor is controlled by the pilot one side of the steering bar goes down resulting in pulling the side of the canopy connected to it.

| Left String              | Right String             | Result     |
|--------------------------|--------------------------|------------|
| Pulled down              | No Action                | Left Turn  |
| No Action                | Pulled down              | Right Turn |
| Pulled Down (less angle) | Pulled Down (less angle) | Lift       |
| Pulled down (high angle) | Pulled Down (high angle) | Descend    |

Table 1.1. Asymmetric brake deflection

The more the trailing edge deflected the faster will be the turn and shorter the radius more altitude is lost. As the drag increases there is a loss of lift, which can be minimized by increasing the throttle.

### 1.5.8 The effects of wind direction

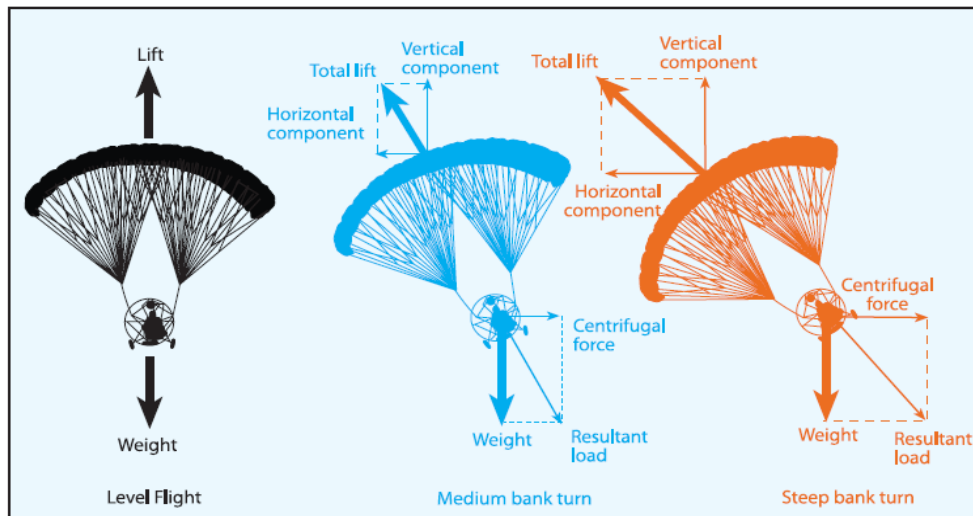


Figure 1.16. Powered Parafoil Loads and Turning Forces [9]

The canopy has to be faced towards the wing when on ground called weather vaning which helps in easy takeoff. Ground steering is accomplished by pulling the control strings either left or right. The difference between wind direction and takeoff roll direction will not allow the canopy to take off properly. Therefore the takeoff and landing must be done directly into the wind.

## **1.6 THESIS OUTLINE**

The further organization of thesis is given in the following manner.

Chapter 2 goes with the brief description of literature review, research outcomes, objectives and methodology. The literature review covers two types of systems namely autonomous unpowered Parafoil systems and Powered Parafoil Systems.

Chapter 3 discusses in detail about the experimental design, which deals with the Basic System Performance calculations, structure of the payload, electronic components installed, detailed description of each component, hardware design. The chapter also explains the data acquisition system. The planned flight tests plan is also given in detail.

The mathematical model is discussed in chapter 4. A 9 DOF nonlinear model has been developed and explained in detail. A new control strategy is also discussed which helps in understanding the turn performance, by pulling one side of the Parafoil, this technique would help in understating the radius of turn and turn rate of the system. The tilt mechanism would help in developing the lateral heading direction control system. A thrust vector is also added to the payload. This helps us understating the amount of thrust required for level flight, take off and gliding flight. This helps in designing the longitudinal altitude hold auto pilot design.

Chapter 5 discusses the control system design for a Powered Parafoil Aerial Vehicle. Before the control system design, the vehicle was first stabilized Roll, pitch and yaw later heading controller and longitudinal altitude hold controller was designed. A waypoint algorithm was then designed and burned into the

controller. Two algorithms steer to target and path restoration algorithms are discussed. The controller gains are also calculated. The flight test closed loop results are then plotted.

Chapter 6 deals with the conclusion and future scope.

## **CHAPTER 2**

### **LITERATURE REVIEW AND METHODOLOGY**

#### **2.1 INTRODUCTION**

This Chapter deals with the literature review and methodology used. The first half of the chapter deals with the literature review. The review is divided into two parts that is on autonomous unpowered gliding Parafoils and the Powered Parafoil Aerial vehicles. The later section gives the detailed description about methodology used, objectives and the research focus.

#### **2.2 LITERATURE REVIEW**

In various designs, the ballistic and Parafoil configurations are more advantageous than other configurations, as they are simple in developing. During the last decade many efforts were made to replace the uncontrolled circular Parachute with maneuverable autonomously guided Ram Air Parafoils that assure more accurate delivery of variety of payloads from high altitudes and standoff distances. Parafoils have proven good in many situations as they are stable and have slow decent rate. This can be more advantageous in surveying as they have long flight duration. Maneuvering is normally achieved by deflecting the trailing edge of the canopy asymmetrically, while some degree of glide slope control is offered with symmetric flap deflection. Dropped from sufficient altitude, a Parafoil controlled vehicle is capable of reaching a much larger area. These attributes offer a great deal of flexibility to precision delivery systems. The rear section housing the arrestor chute for the precision delivery system can be replaced with a module containing the Parafoil and necessary actuators and other components such as computer and avionics would be the same. This setup converts the unpowered Parafoil into a powered Parafoil.

### 2.1.1 Review on Autonomous Un-Powered Parafoil Systems

UAV systems have proven helpful in delivering payloads as well. For the precise delivery of the payload a sensor network must be established. The advantages and disadvantages of the different types of UAVs are mentioned below [10].

| UAV Type   | Advantages  | Disadvantages                                  |
|------------|---|--|
| Ballistic  | Simplicity<br>Packaging                             | Small glide slope<br>High impact deceleration  |
| Parafoil   | Glide slope<br>Maneuverability<br>Slow descent rate | Long flight duration<br>Susceptibility to wind |
| Rotorcraft | Slow descent rate                                   | Cost and complexity                            |
| Fixed Wing | Maneuverability<br>Long range                       | Cost and complexity                            |

Table 2.1. Comparison Between Different UAV Systems

These systems are in use, as the Parafoil concept is not the new one. The main functions of these systems are to deliver cargo to remote areas. The navigation subsystem of the guidance, navigation and control on onboard manages data acquisition, processes sensor data and provides guidance and control subsystems with information about Parafoil states. Using this information along with local wind profiles, the guidance subsystem plans the mission and generates the feasible trajectory to the desired landing point. Finally it is responsibility of the control system to track this trajectory using the information provided by the navigation subsystem and on board actuators.

Several approaches are currently being used by different developers for the precise landing.

- Affordable Guided Airdrop System (AGAS) – Capewell Components Co., LLC

- Controlled Aerial Delivery System (CADS) – Cobham PLC
- Dragon Train – Aerobotics, LLC
- FireFly – Airborne Systems North America
- Improved Container Delivery System (ICDS) – U.S. Army NSDREC & U.S. Air Force
- Low Cost Aerial Delivery System (LCADS) – U.S. Army PM-FSS
- MegaFly – Airborne Systems North America
- MicroFly – Airborne Systems North America
- Mosquito – Stara Technologies, Inc.
- Onyx 300 – Atair Aerospace, Inc.
- Onyx Ultra Light (UL) – Atair Aerospace, Inc.
- Panther 500 – Pioneer Aerospace Corp. / Aerazur
- Panther 2K – Pioneer Aerospace Corp. / Aerazur
- 10K Screamer – Strong Enterprises
- 2K Screamer – Strong Enterprises
- Sherpa 1200/2200 – Mist Mobility Integrated Systems Technology (MMIST), Inc.
- Système de Navigation pour Charge Accompagnée (SNCA) – NAVOCAP
- SPADES 300 – Dutch Space
- SPADES 1000 – Dutch Space

The avionics, hardware and the target accuracy of the above systems is given in detail in Table 2.2

| <b>Year</b> | <b>Organization</b> | <b>System</b>        | <b>Avionics used</b>  | <b>Result</b>          |
|-------------|---------------------|----------------------|---|------------------------|
| 2008        | US SOCOM<br>[11]    | Snow<br>Flake<br>ADS | Three accelerometers,<br>Three rate<br>gyroscopes, a<br>magnetometer, | 55m target<br>accuracy |

|      |                                |               |  |                      |
|------|--------------------------------|---------------|--|----------------------|
|      |                                |               | Global Positioning System Receiver and a Barometric Altimeter, Servo Motor   |                      |
| 2006 | German Aerospace Center [12]   | ALEX          | MEMS accelerometer, Laser altimeter, absolute pressure sensor, temperature sensor, force transducer, rate gyro, 3-axis magnetometer, GPS, Pitot Tube and Camcorder | 200m target accuracy |
| 2004 | DLR [13]                       | X-38          | Embedded GPS/INS system, Optical Range sensor  | Cancelled            |
| 2003 | Cal poly state university [14] | ATRP          | Microcontroller, digital compass, and accelerometer  |                      |
| 1997 | US Soldier Systems[15]         | GPADS - Light | single board computer, Processor, GPS Receiver, Barometric Pressure Sensor, compass and  | 250m Accuracy        |

|      |           |                |  |                   |
|------|-----------|----------------|--|-------------------|
|      |           |                | a servo actuator   |                   |
| 1994 | NASA [16] | Spacew<br>edge | GPS, rate gyro, and<br>compass and on board<br>data recorder | 1600m<br>accuracy |

Table 2.2. Various Autonomous Gliding Parafoils

The addition of a power/ propelling unit makes the paraglider an Unmanned Aerial Vehicle (UAV) which can be used for land observation, surveillance etc. such a paraglider is called powered Parafoil system (PPS) . A PPS consists of a Parafoil and a suspended payload equipped with an engine or motor and a propeller. From the view of dynamics and control, the configuration of the PPS provides the following unique characteristics, as compared to conventional wing aircraft [17].

- The separation between the centers of gravity of the canopy and the payload produces a swinging motion.
- Changing the thrust induces a considerable pitching motion.
- Relative pitching and yawing motions exists between the canopy and the payload
- Canopy is a tailless flying wing
- Directional control is mainly achieved through rolling motion, rather than through yawing motion.
- The apparent mass of the canopy must be taken into account, as in case of an airship

There are several companies working on these kinds of models using remote control such as:

- Hi-Cam aerial and video systems [18]
- Paralight aviation ltd international [19]



- Sea breeze Parafoils [20]
- Powered Parafoil and sports flying [21]
- Really cool toys

### 1.6.1 Review on Powered Parafoil Aerial Vehicles

In 2011, Y Ochi and M Watanabe have designed a flight controller for a powered Parafoil system. The author discussed that the powered Parafoil having canopy, payload with a propeller unit is assumed to be having 8dof.

The same year SUSI 62 [16], a Parafoil UAV has been designed for remote sensing. SUSI 62, has a payload of about 8kg and needs a runway of about 50 m. the system is controlled by a remote control.



Figure 2.2. SUSI 62

In the year **2007**, small scale Powered Parafoil in flight has been examined [17]. The results were simulated and modeled in MATLAB.



Figure 2.3. Small Scale Powered Parafoil

In **2005**, A Vertical Launch Parafoil Aerial Vehicle –Flying Eye was developed [18] to follow a predetermined flight path using sensors, controllers, mechanical components and software.



Figure 2.4. Flying-Eye Project

In the same year Tommy Ike Hailey described the use of powered Parafoil [19] in Archeological aerial photography. He also worked on the performance, altitude

stability, in-flight stability and drift assessment of the vehicle and proved suitable for the aerial photography. The author also discussed the limitations of this vehicle. The author also suggested that Powered Parafoil can be used by agencies responsible for the management of cultural resources for planning site development, monitoring site threats and producing aerial images that will appeal to the public.

In **2004**, A Snowgoose [20], autonomously guided powered Parafoil based UAV that was designed for US Special Operations command. It is meant to be useful for leafleting and resupply operations today. It was designed by Mist Mobility Integrated Systems Technology Inc. (MMIST) of Canada. The developed UAV is a Remote controlled vehicle. It has an unattended ground sensor (UGS). The operator piloted the Parafoil toward the target using a push button on the remote. Later the system was made autonomous by programming the target point.



Figure.2.5. Snowgoose PPC

Papers by Yamauchi and Rudakevych [21], [22] describe the “Griffon” a man portable UAV utilizing the “PackBot” ground-mobile robotics platform and Parafoil wing. The Griffon was developed under phase 1 small business innovation research (SBIR) project. It weighs 57 pounds, and does not fly autonomously; it is remotely piloted. The Parafoil used is an extremely sports traction kite with slight modification. The default angle flight was adjusted, and the kite was converted to a four control-line configuration. The chosen kite was a “Razor”, manufactured by ozone, with a wing area 11 square meters. The authors utilized a similar approach to that which will be used in present research. A simplified free-body diagram was given as the starting point for design of the powered Parafoil fuselage. Torques was summed about the center of the gravity and the motor was placed slightly below the Parafoil attachment point, yet well above the center of mass. The aircraft thrust was measured and noted against the RPM, as will be done in current investigation. The tests presented by yamauchi were stated to be for verification of adequate thrust to lift the given payload. The Griffon was flight tested in June 2003, and achieved an altitude of 200 feet and flight speed in excess of 20 miles per hour, with a 2.2 HP engine. The author did state that the Parafoil wing limits the aircraft’s usability in windy conditions.



Figure 2.6. Griffon PPC

In *2003*, Bukeye was developed [23]. The X-38/Crew Return Vehicle, a lifting body re-entry vehicle, has been developed as a lifeboat in case of emergency at the international space station. To simulate and verify the performance of the onboard Parafoil, guidance, navigation and control system, a commercial powered Parafoil vehicle, known as Bukeye was modified to accommodate the avionics and reduced scale Parafoil for aerodynamic similarity.



Figure 2.7. Buckeye PPC

The Powered Parafoil Systems developed in the last decade are given in detail in table 2.3.

| <b>Year</b> | <b>System</b> | <b>Avionics</b>                                  | <b>Control Surfaces</b> | <b>Operation</b> | <b>Application</b> |
|-------------|---------------|--|-------------------------|------------------|--------------------|
| 2011        | SUSI 62       | Sensors,<br>Engine,<br>Servo Motor,<br>Gyroscope | Two Servos              | Remote Control   | Remote Sensing     |

|      |                  |   |            |                |                            |
|------|------------------|---|------------|----------------|----------------------------|
| 2005 | Flying Eye       | Sensors, controllers, mechanical components         | Two servos | Remote Control | Lab Instrument             |
| 2005 | Powered Parafoil | Sensors, Engine, Servo Motor, Gyroscope             | Two servos | Remote Control | Archeological Surveillance |
| 2004 | Snow Goose       | Gyro, Motor, Servo Motor, Unattended Ground Sensors | Two Servos | Remote Control | US Special Operations      |
| 2004 | Griffon Packbot  | Sensors, Engine, Servo Motor, Gyroscope             | Two Servos | Remote Control | Surveillance               |

Table 2.3. Powered Parafoil Systems

## 1.7 MOTIVATION AND NEED FOR RESEARCH

Parafoil Aerial Vehicle (PAV) can be used for applications that require accurate vertical positioning which include crop dusting, high resolution and close range imaging, proximity sensing of targets and detection of substances and organisms that are altitude specific. The below table gives the comparative study on various UAVs, and their features motivated to select PAV as a subject of research. The

considered model will be controlled using a single servo and the mathematical modeling will also be done for single servo.

| <b>Factor</b>                         | <b>Multi Copter</b> | <b>Fixed wing</b> | <b>PAV</b>    | <b>Selection</b>           |
|---------------------------------------|---------------------|-------------------|---------------|----------------------------|
| <b>Design /Fabrication Complexity</b> | Difficult           | Difficult         | Easy          | PAV                        |
| <b>Aerodynamic Efficiency</b>         | Less                | More              | More          | Multi copter               |
| <b>Flight time</b>                    | Less                | More              | More          | PAV                        |
| <b>Control over Handling</b>          | Difficult           | Difficult         | Easy          | PAV                        |
| <b>Payload Capacity</b>               | Fixed               | Fixed             | Variable      | PAV                        |
| <b>Autopilot</b>                      | Advanced            | Advanced          | Low end       | PAV                        |
| <b>Wind effect</b>                    | Less effect         | Less effect       | More effect   | Fixed wing                 |
| <b>Transportation of Vehicle</b>      | Easy                | Difficult         | Easy          | PAV                        |
| <b>Crash Impact</b>                   | More damage         | More damage       | Less damage   | PAV                        |
| <b>Runway</b>                         | Not required        | Required          | Less Required | Multi copter               |
| <b>Flight Speed</b>                   | Low speed           | High speed        | Low speed     | Depends on the application |
| <b>Flight Stability</b>               | Less stable         | Stable            | Highly stable | PAV                        |

Table 2.4: Comparative Study on Different Technologies

Keeping all the factors in view a Parafoil/Parachute aerial vehicle can be considered to be the most stable Aerial vehicle. A benefit of the powered parachute for unmanned aircraft use is their unique ability to glide to the ground in a relatively safe manner, even if all control systems are disabled. This is particularly desirable in urban environments where a failure of any large UAV would likely result in collateral damage to structure on the ground. Powered parachutes, on the other hand, would be unlikely to land with a vertical speed above 10mph, making severe damage to any ground edifice or even the airframe itself is unlikely.

## **1.8 LITERATURE RESEARCH OUTCOMES**

- Various unmanned aerial systems have been analyzed and it has been observed that the Powered Parafoils have many unique capabilities such as high payload carrying capability, low speed, stabilized flight etc. that makes powered Parafoils advantageous compared to that of conventional UAS systems.
- The literature of the powered Parafoils have been studied and determined that, due to the unique structure, the features can be described only by nonlinear model for Parafoil payload coupled system.
- All the developed powered Parafoil system, use asymmetric brake deflection mechanism on either side through two servo motors to achieve yaw control.
- Measurement systems have been determined which can be used to achieve guidance and navigation control.
- The separation between the centers of gravity of the canopy and the payload produces a swinging motion.
- Changing the thrust induces a considerable pitching motion.
- Relative pitching and yawing motions exists between the canopy and the payload.
- Directional control is mainly achieved through yawing motion, apart from rolling motion.



## 1.9 RESEARCH FOCUS

- A 9 DOF model developed for unpowered Parafoil model has been modified by adding a thrust force vector to the payload to simulate model dynamics under thrust condition.
- The thrust provided will be utilized to increase, decrease and hold the altitude of the vehicle.
- A single servo will be used to control the direction by tilting down the Parafoil to left and right.
- A stability circuit will be developed that will reduce down the oscillations on the vehicle
- Guidance and navigation will be incorporated using way-point navigation technique which loiter and navigate the vehicle
- The mission starts by taking the vehicle to certain height and engaging the autonomous guidance and navigation mode.
- A hardware model will be developed that can be used for various applications.

## 1.10 OBJECTIVES

The project aims at making an Autonomous Flying Para Drone moving on pre-defined path with obstacle avoidance and path restoration technique.

- To develop a Servo motor based direction control System
- To develop a GPS Based navigation system
- To develop a Ultrasonic sensor based obstacle avoidance system
- Interfacing all the above control systems

## 1.11 METHODOLOGY

| <b>Task</b>      | <b>Testing Parameters</b>       | <b>Output</b>           |
|------------------|---------------------------------|-------------------------|
| Selection of UAV | Easy to glide<br>Good Endurance | Parafoil Aerial Vehicle |

|   |  |  |
|---|--|--|
|   | Good Range<br>Moderate Speed<br>Variable payload   |  |
| Design  | Endurance<br>Range<br>Strength<br>Para foil size<br>Payload calculation  | Size of the Parafoil according to the weight of the Parafoil |
| Selection of Material (As per the comparison in next table) | Less weight<br>More strength<br>Easy to mold<br>High impact strength<br>Resistance to effect of temperature variation<br>Corrosion resistant<br>Cost | Aluminum Alloys, CFRP rods                                   |
| Fabrication   | Structural analysis<br>Fabrication of sub - assemblies<br>Assembly   | Structure of the UAV   |
| Power Source Selection                                      | Variable transmission<br>Power output<br>Light Weight<br>High Torque<br>Less Fuel<br>Consumption   | 2 stroke CI or SI IC Engine<br>Li Po Battery                 |
| Modeling  | 3 dof<br>6 dof<br>9 dof  | Controlling parameters                                       |

|                                   |   |   |
|-----------------------------------|---|---|
| Control system design             | Simulink model  | Controlled flight parameters                            |
| Servo motor control               | Decide the angle<br>Interfacing Servo with microcontroller  | Servo motor based direction changing ground robot       |
| GPS                               | Study of GPS<br>Interfacing GPS with Microcontroller<br>Extracting the values using microcontroller                             | GPS navigation based ground robot                       |
| IMU                               | Study of IMU<br>Interfacing IMU with Microcontroller<br>Extracting the values using microcontroller                             | IMU value based direction control ground robot          |
| Ultra Sonic Sensor                | Study of ultrasonic Sensor<br>Interfacing Ultrasonic sensor with Microcontroller<br>Extracting the values using microcontroller | Ultrasonic sensor based obstacle avoidance ground robot |
| Hardware and Software Interfacing | Interfacing GPS and IMU with controller   | Navigation Control                                      |
|                                   | Interfacing Ultrasonic sensors and motor controller   | Obstacle avoidance and Direction control                |
|                                   | Interfacing controller  | Complete UAV  |

|  |                       |  |
|--|-----------------------|--|
|  | and Structure         |  |
| Algorithm Design                         | Main control loop     | Left and right steering using IMU values |
|  | Steer to target       | Steering with IMU and GPS values         |
|  | Landing at the target | Using IMU and GPS and Servo              |
|  | Obstacle avoidance    | Ultrasonic sensor, IMU and GPS           |
|  | Full break algorithm  | Stop the Parafoil                        |
| Testing at different climatic conditions | Remote Controlled UAV | Semi-Autonomous                          |
|  | Autonomous            | Autonomous                               |

Table 2.5. Methodology developed for proposed PAV

Keeping all the factors in view a Parafoil aerial vehicle is selected. Applications that require accurate vertical positioning include crop dusting, high resolution and close range imaging, proximity sensing of targets and detection of substances and organisms that are altitude specific. A benefit of the powered Parafoil for unmanned aircraft use is their unique ability to glide to the ground in a relatively safe manner, even if all control systems are disabled. This is particularly desirable in urban environments where a failure of any large UAV would likely result in collateral damage to structure on the ground. Powered Parafoils, on the other hand, would be unlikely to land with a vertical speed above 10mph, making severe damage to any ground edifice or even the airframe itself is unlikely.

## **CHAPTER 3**

### **EXPERIMENT DESIGN**

#### **3.1 UNMANNED POWERED PARAFOIL AERIAL VEHICLE CONCEPT**

The UPPAV is a concept which consists of a Parafoil and a powered payload. The Parafoil is connected to the payload at two joints using flexible lines. The vehicle is fully stable and requires only two controls, one for direction control and one for take-off and landing. The vehicle has numerous advantages and applications ranging from aerial delivery to remote sensing. The vehicle was developed for remote sensing purpose. The vehicle is a small unmanned powered Parafoil vehicle with payload carrying capability of 2.5 – 4.5 Kg including the electronics, battery and sensors. The vehicle was developed with only two controls. The chapter discusses in detail about the payload concept which includes various parts of the payload, Parafoil Performance which includes the Parafoil size with respect to the payload calculation and the sensors and control unit used in detail. The above mentioned systems are prime requirements to full fill the autonomous remote sensing task.

#### **3.2 PAYLOAD COMPONENTS**

The payload generally consists of the following parts

- Nose
- Main frame
- Propeller guard
- Back landing gears
- Front landing gear

- Control rod
- Sensors and control Unit

The above mentioned parts are discussed in detail in this chapter. The sensors and control unit is placed on the payload.

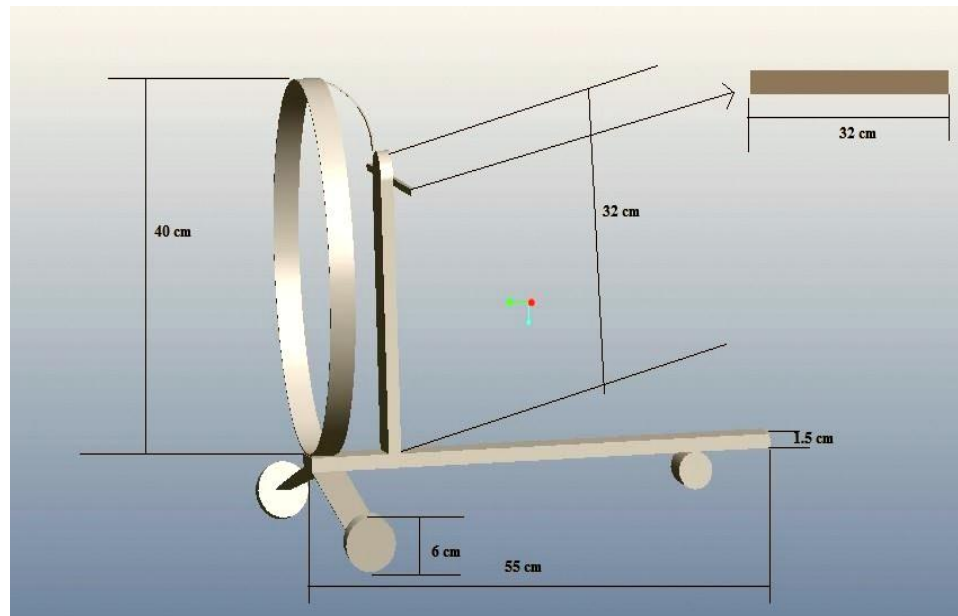


Figure 3.1: Physical Dimensions of the Vehicle

### 3.2.1 Nose to Main Frame Ratio

The nose is made up of balsa wood. The nose is generally considered to be long compared to the main frame in a ratio of 7:5. The length of the nose is 55cm

It is observed that if the nose is taken short the vehicle tends to stall.

### 3.2.2 Main Frame

The mainframe is also made up of balsa wood. The mainframe acts as a house for propulsion unit and the control unit. The propulsion system (motor and the propeller) is placed exactly at the center so that the propeller does not touch the surface of the nose when rotating.

### **3.2.3 Propulsion unit**

The propulsion unit consists of an out-runner Brushless DC Motor (BLDC). The motor selection is done by the power calculation. The power required can be calculated by multiplying volts and amps.

- Input watts per pound gives the power requirement based on the weight of the model.
- If the model weight is considered to be  $x$ , and power required is 100 watts then then  $100x$  input watts per pound is the minimum power required to achieve the desired performance.
- The input power the motor can handle is determined by  
Average voltage X continuous current = input watts

Therefore for a 3 kg payload, 6 Cells, Continuous Power Capability: 19.8 Volts (6 x 3.3) x 40 Amps = 792 Watts. The size propeller attached to the model depends on the motor selected.

### **3.2.4 Propeller Guard**

The propeller guard is made of aluminum which is bent in the form of a circle to give protection to the strings. The diameter of the propeller guard is 32cm.

### **3.2.5 Front and Back Landing Gears**

The front landing gear has one wheel and the back landing gear has two wheels giving the shape of a triac. All the wheels are made of balsa wood. Each wheel is of 6cm diameter

### **3.2.6 Control Rod**

The control rod is hinged to the main frame at the center, and is connected to a servo through a push pull rod. The control rod made of an aluminum rod, and is 32cm.

### 3.2.7 Sensors and Control Unit

The complete set of electronics and the controller used is discussed in detail in the later sections of the chapter (3.6 - Data acquisitions and control system). The total weight of the sensors system is 20 grams.

## 3.3 PARAFOIL SIZING

A Ram Air Parafoil comes under the category of NACA Clark Y aero-foil.

### 3.3.1 Size of the Parafoil

The mass of the payload may range in between 1kg to 8000kg. Change in the weight of the payload increases the size of the parachute [29] The general requirements for calculating the size of the parachute are:



Figure.3.2: Parafoil used for UPPAV

- Payload mass( $W$ )
- Horizontal flight velocity( $w$ )
- Vertical flight velocity( $u$ )



- Lift(L)
- Drag(D)
- Aspect ratio(A)
- Chord length(B)
- Span (B)
- Density(d)

### 3.3.2 Size

The size of the parachute will be determined by the mass of the payload to be delivered. Therefore the velocity of the parachute is also calculated [29].

The wind specifications set the lower limit on wing loading.

The velocity of the parachute is square root of horizontal flight velocity and vertical flight velocity.

$$v = \sqrt{u^2 - w^2} \quad (3.1)$$

The horizontal flight velocity (w) is calculated by, the L/D is assumed to be 3.

$$w = \frac{u}{L/D} \quad (3.2)$$

Using these values the size of the parachute is calculated, which is given by:

$$S = \frac{W}{10 \times \sqrt{(C_l^2 + C_d^2) \times (0.5 \times V^2 \times d)}} \quad (3.3)$$

### 3.3.3 Cord

The cord of the parachute is calculated using Aspect Ratio and the Surface area of the parachute

$$C = \sqrt{S/A} \tag{3.4}$$

### 3.3.4 Width

The Width of the parachute is given by multiplying cord and aspect ratio

$$B = C \times A \tag{3.5}$$

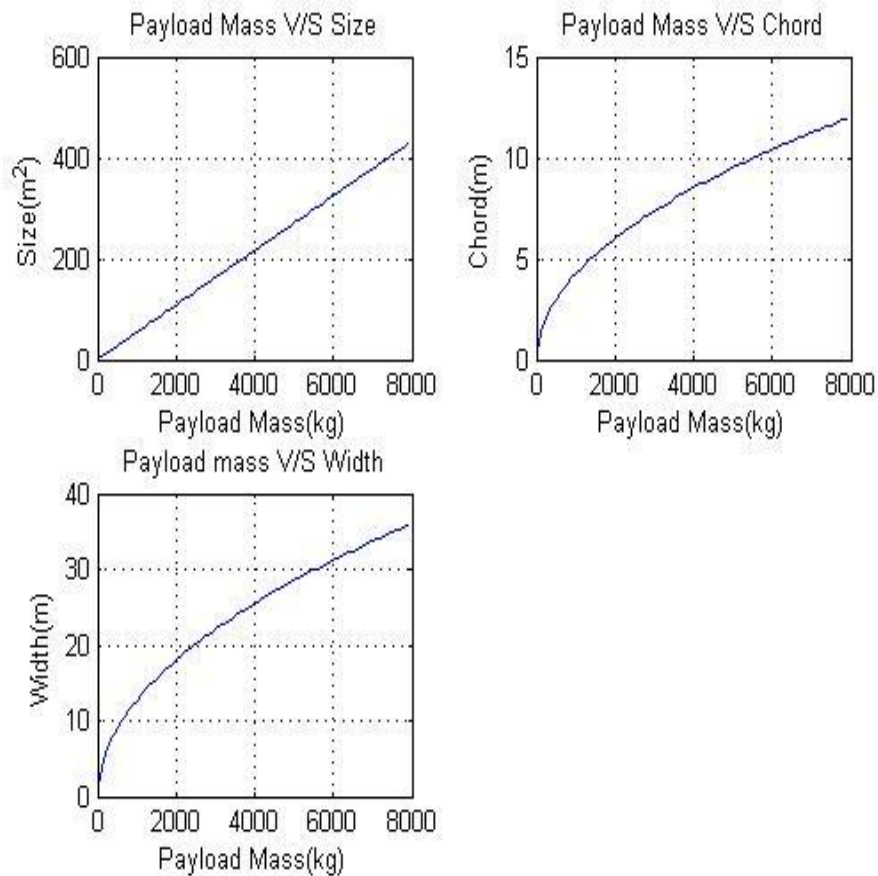


Figure 3.3: Parafoil Size to the Payload

Since our operation has to be performed using a small Parafoil the following table was again calculated to the approximate size of the Parafoil which should be capable of lifting a payload of maximum 5 Kg, which includes the discussed payload components.

| S.No. | Weight (kg)<br>(maximum) | Span<br>(m) | Chord<br>(m) | Area<br>(m <sup>2</sup> ) |
|-------|--------------------------|-------------|--------------|---------------------------|
| 1     | 1                        | 0.84        | 0.28         | 0.24                      |
| 2     | 2                        | 1.2         | 0.4          | 0.48                      |
| 3     | 3                        | 1.47        | 0.5          | 0.73                      |
| 4     | 4                        | 1.68        | 0.56         | 0.97                      |
| 5     | 5                        | 1.89        | 0.63         | 1.2                       |

Table 3.1: Parafoil Payload Relationship

Keeping the Payload components, Parafoil Performance and Parafoil sizing, the Parafoil that was selected is capable of lift 5 Kgs (Maximum), the following is the specification of the vehicle.

|              |                                |
|--------------|--------------------------------|
| Payload mass | 3-4 kg (Including electronics) |
| Cord         | 0.65m                          |
| Span         | 2m                             |
| Area         | 1.3 m <sup>2</sup>             |
| velocity     | 10 km/h                        |
| density      | 1.22                           |
| Aspect Ratio | 3                              |

Table 3.2: UPPAV Specifications

### 3.4 PERFORMANCE PARAMETERS

Performance Parameters include the basic L/D concept and lift and drag coefficient calculation and glide performance.

#### 3.4.1 Parafoil L/D Ratio

The L/D ratio of Parafoil changes according to the angle of attack, thereby getting different L/D ratios at different flight conditions. L/D ratio is also used to determine the drag coefficients it is taken as 3 initially.

### 3.4.2 Parafoil Lift and Drag Coefficient Calculation

The requirement of lift coefficient acting on UPPAV is determined as following from the estimated flight velocity [11]

$$L = \frac{1}{2} \rho V^2 S C_l \quad (3.6)$$

$$L=W \quad (3.7)$$

$$C_l = \frac{2W}{\rho A V^2} = 0.5 \quad (3.8)$$

For the drag coefficient, the lift to drag ratio can be determined by the gliding flight

$$C_d = \frac{C_l}{L/D} = 0.16 \quad (3.9)$$

The total drag that is acting on the Parafoil is given as the sums of the parasite drag and drag due to lift.

$$C_d = C_{d_p} + C_{d_i} \quad (3.10)$$

$$C_{d_i} = \frac{A C_l^2}{\Pi a b^2} = 0.046 \quad (3.11)$$

Parasite drag can be calculated by subtracting the Drag due to the lift from the total drag

$$C_{d_p} = C_d - C_{d_i} = 0.104 \quad (3.12)$$

These estimates suggest that the parasite drag is 50.6 % of the total drag and drag due to the lift is 49.37%.

### 3.4.3 Payload and Lines Drag Calculation

- Height of the payload =  $0.46\text{m} \times 0.015\text{m} \times 0.05\text{m}$
- Length of the Payload =  $0.55\text{m} \times 0.015\text{m} \times 0.05\text{m}$
- Width of the Payload =  $0.32\text{m} \times 0.015\text{m} \times 0.05\text{m}$
- Therefore total drag area of the payload =  $0.05\text{m}^2$

For which the drag coefficient is 0.057, the drag coefficient for the lines comes out to be 0.01.

Therefore the total drag of the vehicle comes out to be  $C_d = 0.21$ .

### 3.4.4 Lift to Drag Ratio of the Complete System (PAV)

$$E = \frac{C_l}{C_d} = 2.5 \quad (3.13)$$

Where, E is known as the lift to drag ratio.

### 3.4.5 Gliding Flight Performance of PAV

Velocity of the vehicle during gliding flight is given as

$$V = \sqrt{\frac{2XW}{\rho X S X C_l}} = 10\text{m/s} \quad (3.14)$$

Gamma (glide angle) is given by

$$\gamma = -\frac{1}{E} = -0.4\text{radians} = -22\text{ deg rees} \quad (3.15)$$

During the level flight lift to drag ratio is zero, which make glide angle 0.

## 3.5 THRUST REQUIREMENT

The motor used for the developed UPPAV is E Flite 60 which generates a power of 1200 Watts which comes out to be 1.6 bhp. The motor used is capable of lifting a payload upto 5 Kgs.

Thrust required by UPPAV can be estimated from the following formula [11]

$$T = \frac{VW}{L / DX(\text{motor}(bhp))} = 8N \quad (3.16)$$

### **3.6 DATA ACQUISITION AND CONTROL SYSTEM**

The data acquisition system consist of a micro controller, which monitors airspeed, altitude, location, ground speed, velocity etc.

#### **3.6.1 Inertial Measurement Unit**

The IMU used is MPU-600. The device has inbuilt 3-axis accelerometer and a 3-axis gyroscope. The device communicates with the microprocessor in SPI mode. The accelerometer has a range of +16g to -16g and gyroscope has a range of +2000deg/sec to -2000deg/sec.

The three steps should be followed to initialize the IMU

1. Low pass filter frequency must be set to half of the sample rate.
2. The range of the accelerometer and gyro must be set.
3. The sample time must match with the sample time of the microprocessor.

#### **3.6.2 Barometric Pressure Sensor**

The MEAS Switzerland MS5611 is a small digital device having an inbuilt 24 bit ADC. The chip provides static pressure value that helps in determining the altitude in inches. The sensor works on 75Hz.

#### **3.6.3 Magnetometer**

The Honeywell HMC5843 3-axis digital Magnetometer measures the magnetic field strength in each of the three axes. The device communicates with serial bus. As the earth's field strength is very weak, the device is sensitive and has high

resolution. The device is susceptible to the noise due to the noise in the vicinity of the sensor. The engine with induced magnetic field further degrades the quality of the sensor.

### 3.6.4 GPS

The MediaTek MT3329 10Hz GPS Receiver includes the GPS receiver, processor, and an antenna. The input values are the simulated GPS values.

### 3.6.5 Pitot Probe

This probe is pitot static probe which is mounted in the forward direction in the triac. The Freescale MPXV7002DP measures the Differential pressure sensor connected to the pitot tube measures the airspeed. Once calibrated, the output is the value of pressure in terms of voltage.

### 3.6.6 Ultrasonic Sensor

Parallax PING ultrasonic sensor provides an easy method of distance measurement. A single I/O pin is used to trigger an ultrasonic burst (well above human hearing) and then "listen" for the echo return pulse. The sensor measures the time required for the echo return, and returns this value to the microcontroller as a variable-width pulse via the same I/O pin. The following table gives the brief idea about the components used and their specifications.

| S.No. | Component  | Specification   | Usage   |
|-------|------------|---|---|
| 1.    | BLDC Motor | Eflite 60 <ul style="list-style-type: none"> <li>• Equivalent to a 60-size glow engine for 6 to 10 lb (2.7 to 4.5 kg) airplanes</li> <li>• 8880 RPM with 22.2V battery</li> </ul> | Provides throttle, to maintain altitude, take off and landing |

|     |                            |   |   |
|-----|----------------------------|---|---|
| 2.  | ESC                        | 100 Amps, Turnigy<br>Requires 3-6 cell Li-Po battery  | Provides PWM signals to BLDC motor, to control the speed of the motor |
| 3.  | Propeller                  | 13X4  | Provides thrust of 5.5 Kg   |
| 4.  | Battery                    | <ul style="list-style-type: none"> <li>• Li-Po</li> <li>• 22.2V</li> <li>• 5000 mAh</li> <li>• 6 Cell</li> </ul>  | Power supply, up to 20 minutes, for continuous flying                 |
| 5.  | Futaba Trans Receiver      | 22.4 GHz <ul style="list-style-type: none"> <li>• 6 channel</li> <li>• 1 Km Range</li> </ul>  | To control the vehicle  |
| 6.  | Servo Motor                | 16 Kg   | For direction control   |
| 7.  | Ardu Pilot                 | <ul style="list-style-type: none"> <li>• ATMEGA2560 (Arduino Mega)</li> <li>• Supported telemetry 433 MHz</li> <li>• 4 PWM Channels</li> <li>• 4 USART</li> <li>• 10 bit ADC</li> </ul> | Controller for auto pilot,  |
| 8.  | Barometric Pressure Sensor | MEAS Switzerland MS5611 <ul style="list-style-type: none"> <li>• 8 bit ADC</li> <li>• 75 Hz</li> </ul>  | Static Pressure and Temperature                                       |
| 9.  | Magnetometer               | Honeywell HMC5843 3-axis digital Magnetometer <ul style="list-style-type: none"> <li>• USART Communication</li> </ul>   | Magnetic field in X, Y and Z direction                                |
| 10. | GPS                        | MediaTek MT3329 10Hz GPS Receiver, Includes the   | Latitude, Longitude, Altitude, Ground                                 |



|     |                   |  |  |
|-----|-------------------|--|--|
|     |                   | GPS receiver, processor, and an antenna  | Speed, Time,                               |
| 11. | Pitot Probe       | Freesscale MPXV7002DP  | Dynamic Pressure                           |
| 12. | IMU               | MPU 600 <ul style="list-style-type: none"> <li>• 3 axis Accelerometer<br/>+2000 deg/s to -2000 deg/s</li> <li>• 3 axis gyroscope<br/>+16g to -16g</li> </ul> | P,q,r (roll rate, pitch rate and yaw rate) |
| 13. | Ultrasonic Sensor | Parallax PING ultrasonic sensor  | Distance in meters                         |

Table 3.3: Component Specification used in UPPAV



Figure 3.4: UPPAV

The methodology followed for achieving the above mentioned target is to develop embedded system (Hardware Model), Autopilot design and the algorithm design. The hardware model is divided into two parts, which are, onboard embedded

system design and ground station design the communication between the onboard embedded system and the ground station is done using 433 MHz Transceiver protocol

### 3.7 HARDWARE DEVELOPMENT

The development of the control system for autopilot is done to provide artificial stability. The autopilots are capable of maintaining pitch roll and heading angles. These control systems are then coded in the microcontroller using “Embedded C” programming. For the powered parachute aerial vehicle two different autopilots have to design which are, altitude hold autopilot and altitude heading autopilot. For programming these autopilot using Embedded C an algorithm have be designed. A detail description of the on board embedded system, ground station embedded system, altitude hold autopilot, altitude heading autopilot and algorithm design is given.

#### 3.7.1 On board Embedded system

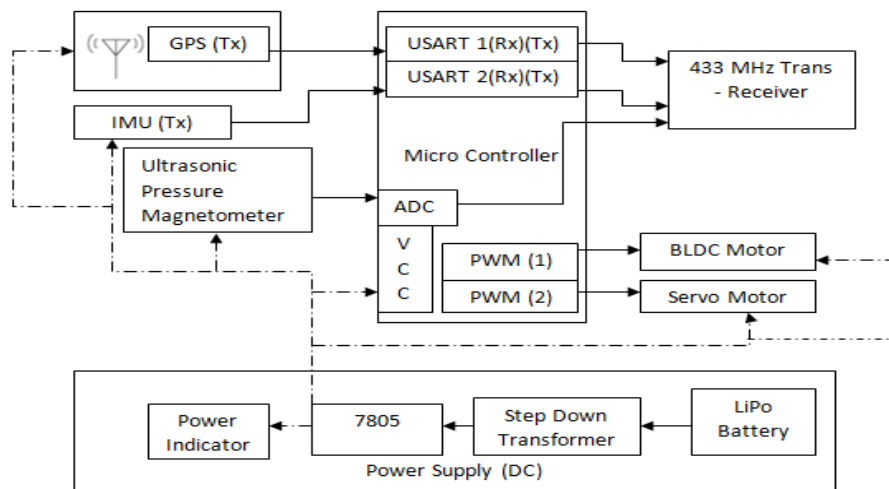


Figure 3.5: Hardware model of Powered Parafoil Aerial Vehicle

The block diagram of transmitting and receiving sections (system with the aerial vehicle and ground station) are given above. The on board Embedded system is

basically placed on the aerial vehicle. The system is interfaced with three sensors GPS, IMU and Ultrasonic sensors. GPS measures the vehicle speed, latitude, longitude and altitude whose values are used to control the vehicle direction also, are transmitted to the ground station using 433 MHz Transmitter Receiver for the operator.

### 3.7.2 Ground Station

The ground station receives the signal from the onboard embedded system and displays all the sensor information to the user.

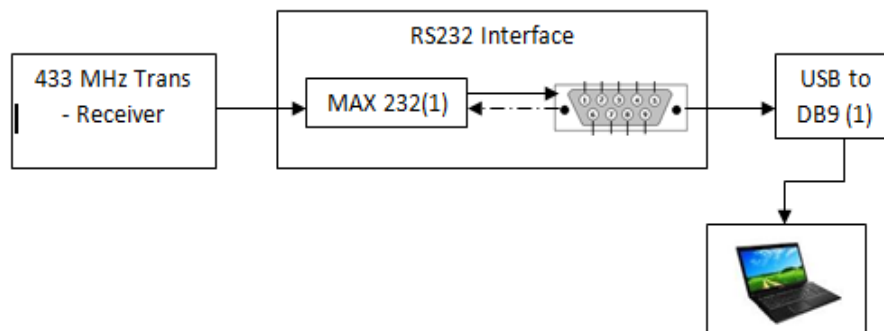


Figure 3.6: Hardware model of Powered Parafoil Aerial Vehicle (Ground Station)

### 3.8 FLIGHT TEST PLAN

The flight tests are planned in two phases. i.e. open loop flight tests and closed loop flight tests to meet the below objectives.

The project aims at making an Autonomous Flying Para Drone moving on pre-defined path with obstacle avoidance and path restoration technique.

- To develop a Servo motor based direction control System
- To develop a GPS Based navigation system
- To develop a Ultrasonic sensor based obstacle avoidance system
- Interfacing all the above control systems

The following open loop flight tests are planned in the following manner. The UPPAV has inherent static stability; therefore the planned light tests would help in acquiring the precise aerodynamic data.

### **3.8.1 Open loop flight test plan**

- *To demonstrate that the flight can be carried out with a single servo*

Most of the developed vehicles use two servos to control the direction of the vehicle, but in UPPAV a single servo is used which has advantages in terms of power and control algorithm design

- *To check the take off*

This test would help us in determining the power required for takeoff, which is generally in full throttle condition.

- *To analyze the turn performance*

Before the closed loop system is designed, the turn rate, turn radius with respect to the servo tilt must be known. Therefore, the turn performance analysis is done

- *Gliding test*

This test would help us understand the AOA, Glide angle and pitch angle performance. This test would also help us in estimating the landing distance and throttle condition.

### **3.8.2 Closed loop Tests**

- *Attitude Stability*

The UPPAV inherently has pendulum stability, due to the turning the vehicle tends to oscillate, these oscillations has to be reduced for precise controller design. The gains of attitude controller is determined using the attitude stability and incorporated in the controller

- *Longitudinal Altitude hold controller*

The vehicle is taken to a certain height and controller is designed such that the vehicle must maintain the same altitude with the same throttle called level flight. The gains are calculated using the controller and are used in the embedded program to hold the required altitude

- *Lateral Heading control*

The heading controller is designed to maintain a heading angle for way point navigation. The gains are calculated using the controller and are used in the embedded program to execute the way point navigation algorithm.

The chapter gives the detailed description of the experiment designed to execute the given PhD problem. The few initial topics deal with the UPPAV structure, the relationship between the payload and the Parafoil, which helped us in determining the size of the Parafoil for executing the experiment. The basic aerodynamic parameters of the vehicle are also determined using the basic formulae. The later section deals with the DAQ system used and their specifications. The Output devices used are also discussed in detail. Flight tests are planned to meet the objectives of the PhD work which are given in detail.

## CHAPTER 4

### MATHEMATICAL MODELLING

#### 4.1 PARAFOIL PAYLOAD MODEL

Parafoil is entirely made of fabric and is a non-rigid wing. A Parafoil gets inflated just like a parachute when dropped from a height. The wing has a low aspect ratio with an elliptical or a rectangular plan form when inflated. To act as an airfoil, the upper membrane and the lower membrane are sewn together with a gap between both. The leading edge is kept open so as to allow the air inside the cells creating air pressure, which maintains the shape of the Parafoil as a wing. The vents in the ribs allow the air to pass from one cell to another which helps in maintaining uniform air pressure in the wing. To avoid the air loss the fabric is made of non-porous material. The suspension lines are used to connect the Parafoil to the payload.

Directional control is achieved by pulling the fly-bar, which changes the direction of the lift making the aircraft turn. The Powered Parafoil has a tendency to fly at constant airspeed. These systems have pendulum stability and oscillations, because of the mass of the airframe suspended significantly below the canopy, which allows the system to have a yaw motion rather than roll motion. Lateral control is obtained by the canopy itself and the propulsion system attached to the payload [30]. The addition of a propulsion system makes the Paraglider an unmanned Aerial vehicle.

The modelling of the Parafoil has been studied in detail. One of the first mathematical models was studied by Goodrick [24]. He developed a three degrees of freedom model in 1975 to study longitudinal stability of Parafoil.

Later he developed six degrees of freedom model to study the control in Parafoil [25]. A guidance algorithm was developed using his six degrees of freedom model [26]. Lingard [22] used longitudinal three degrees of freedom dynamic model of Parafoil payload system to study dynamic effects of various system parameters. These equations were derived about the center of gravity of the total system showing longitudinal motion of the system and pitching motion. The model represented Parafoil mass as well as the apparent mass center at canopy quarter-chord, which is an approximation as apparent mass centers located at canopy centroid. This model was used to analyze the effect of changes in canopy size, line length and break deflection, on longitudinal dynamics of the system. There is always a relative motion between Parafoil and payload to introduce additional degrees of freedom this relative motion should be considered. Also, the relative motion should be taken into account as it affects the altitude of the payload on which the propulsion system is attached. The six degrees of freedom model is a single rigid model, where the relative motion between Parafoil and payload is neglected. In 2011, Y Ochi and M Watanabe have described the non-linear dynamic model using Newtonian mechanics [27]. Body fixed Co-ordinate system are defined for canopy and payload where, six degrees of freedom for canopy and two degrees of freedom for payload. The relative pitch and yawing motions between the canopy and payload are modeled as spring damper system. The internal forces are analytically eliminated. A Six DOF model has been developed by Slegers, N and Nahon, M in 2005, where relative motion between payload and canopy is neglected [28]. Since, the payload on which propulsion and measurement units are placed the relative motion should be taken into account. In early 90's a nine degrees of freedom model was proposed by Doherr and Schilling [29] considering Paraglider as a 2 body system. By constraining to zero the rotation about one or two axes, a seven degrees of freedom and eight degrees of freedom models could be obtained. Mooij et al. [29] used nine degrees of freedom flight dynamic model to develop hardware-in-loop flight simulation environment for the small Parafoil Autonomous Delivery System (SPADES). The Parafoil-

Payload system was represented by two rigid bodies connected by two rigid bars and a hinge. The hinge was modeled as a damped spring. Slegers and Costello [28], Mooij et al. [29], and Yakimenko [30] applied the concept of coupling of moments between the payload and canopy at the joining. This assumption can be applied as the tension plays a major role at the join. A Powered Parachute as shown in Fig.4 has eight degrees of freedom, where six degrees of freedom of canopy and two degrees of freedom of payload. In eight degrees of freedom model roll approximation is neglected as it is considered to be relatively small [31]. Muller et al. [32] considered a non-linear two body eight degrees of freedom model. He considered six degrees of freedom model for Parafoil and two degrees of freedom model for relative motion of payload. The author defined the tensions at the joint to introduce back turning moment about the yaw axis and modeled the moment as the function of tension of the suspension lines. The internal forces in equation of motion were not defined clearly. A linear model was developed by Aakasaka et al. [33], by removing the third co-ordinate system and assuming the tension for a trimmed flight condition to be constant. A non-linear model was developed by Slegers [34] for the same configuration without eliminating the internal forces. Modeling of powered parachute can also be done by analytical methods. Using Lagrange's equations Wise [35] modeled the dynamics of a small propeller. The UAV and the Parafoil are taken as six degrees of freedom systems and the constraints are coupled with eight degrees of freedom model. A Quasi-Hamiltonian formulation was developed by Redelinghuys [36] where, eight degrees of freedom equations were derived. Lagrange's derivations were more complex. An accurate model having nine degrees of freedom, modeled as two-body dynamics, consisting of three degrees of freedom for rotational motion of the Parafoil, three degrees of freedom for the rotational motion of the payload and three degrees of freedom for translational motion of the Parafoil [36]. The turning and gliding flight of Parafoil system is analyzed by Prakash et al. [37] subjected to change in left and right brake deflections. This, nine degrees of freedom model incorporates non-linear aerodynamics to predict all kinds of



behavior. The non-linear simulation demonstrates the validity of the proposed model through comparison with the Lingard's data.

## 4.2 COORDINATE SYSTEMS

Figure 3 shows the coordinate system of the Powered Parafoil Aerial Vehicle used in this study. There are three reference frames called Parafoil Canopy-fixed reference frame ( $X_p, Y_p, Z_p$ ), payload body fixed reference frame ( $X_b, Y_b, Z_b$ ) and Joint C-fixed reference frame ( $X_c, Y_c, Z_c$ ). The Parafoil Canopy-fixed reference frame has its origin located at canopy center of mass P. The  $X_p$  axis points forward, parallel to the canopy chord in the plane of symmetry. The  $Z_p$  axis points downward in the system's plane of symmetry. The  $Y_p$  axis is normal to the plane of symmetry to form a right-handed axis system. In this reference frame, the canopy mass center has translational velocity  $V_p = \{u_p, v_p, w_p\}$ , angular velocity  $\Omega_p = \{p_p, q_p, r_p\}$ , and Euler angles ( $\Phi_p, \theta_p, \psi_p$ ). The payload body fixed reference frame has origin located at payload center of mass b. The  $X_b$  axis points forward normal to the link  $R_b$ . The  $Z_b$  axis points downward, parallel to link  $R_b$ . The  $Y_b$  axis is normal to the  $X_b$  and  $Z_b$  axes as per right-hand rule. In this reference frame the payload mass center has translational velocity  $V_b = \{u_b, v_b, w_b\}$ , angular velocity  $\Omega_b = \{p_b, q_b, r_b\}$ , and Euler angles ( $\Phi_b, \theta_b, \psi_b$ ). The Joint C-fixed reference frame has its origin located at the joint C. the  $X_c$  axis points forward, parallel to each horizontal. The  $Z_c$  axis is normal to  $X_c$ , axis pointing downward. The  $Y_c$  is the axis normal to  $X_c$  and  $Z_c$ . In this reference frame joint C has translational velocity  $V_c = \{u_c, v_c, w_c\}$ . The joint C reaction forces are  $F_c = (F_{cx}, F_{cy}, F_{cz})$ . The suspension lines of the canopy are connected to the payload at to joints  $C_L$  and  $C_R$ , where C is the midpoint between  $C_L$  and  $C_R$ . The derivation of nine degrees of freedom dynamic equations of motion of Parafoil payload system involves separation of system from joint C, and creating the following two sub models such that joint C is exposed to internal forces  $F_c = (F_{cx}, F_{cy}, F_{cz})$ . In the joint C reference frame.

- Payload sub Model

- Parafoil Sub Model

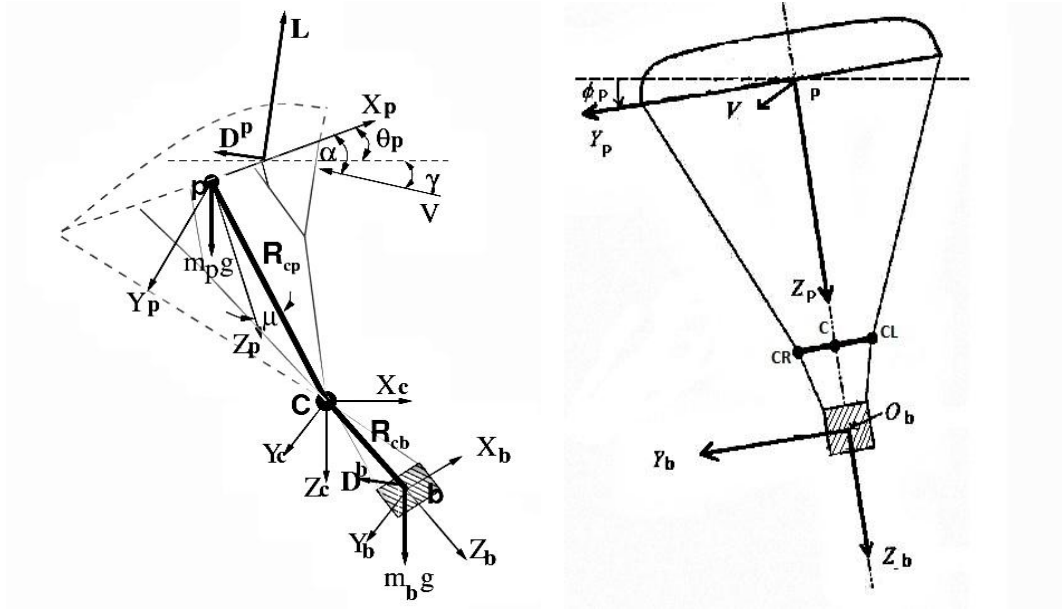


Figure 4.1: Front and Side view of Powered Parafoil Aerial Vehicle

#### 4.3 PAYLOAD SUB MODEL

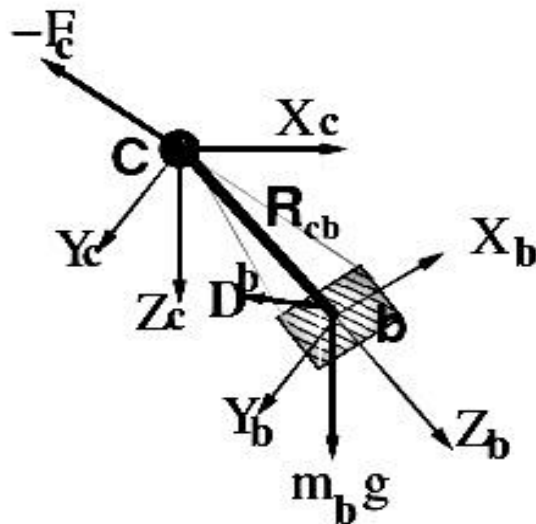


Figure 4.2: Payload Sub Model of Powered Parafoil Aerial Vehicle

The payload sub model consisting of payload center of mass connected to joint C through link  $R_{cb}$ . The payload is allowed to freely rotate about joint C with the  $X_b$  axis pointing forward normal to the link  $R_b$ . The  $Z_b$  axis points downward, parallel to link  $R_b$ . The  $Y_b$  axis is normal to the  $X_b$  and  $Z_b$  axes as per right-hand rule. In this reference frame the payload mass center has translational velocity  $V_b = \{u_b, v_b, w_b\}$ , angular velocity  $\Omega_b = \{p_b, q_b, r_b\}$ , and Euler angles  $(\Phi_b, \theta_b, \psi_b)$ . The forces acting on the payload center of mass are aerodynamic force  $F_b^A$ , Gravitational force  $F_b^G$ , internal Joint force  $F_b^C$  and Thrust force  $F_b^T$ . The internal joint force  $F_b^C$  acting at joint C at a distance of  $R_{Cb} = \{X_{cb}, Y_{cb}, Z_{cb}\}$  from payload mass center in joint C reference frame gives rise to moments  $R_{Cb} \times F_b^C$  about payload mass center.

Translational equations of motion of payload center of mass in payload body fixed reference frame can be expressed as:

$$M_b \dot{V}_b + \Omega_b \times M_b V_b = F_b^A + F_b^G + F_b^T - F_b^C \quad (4.1)$$

Where,

$V_b, \dot{V}_b$ : are inertial reference frame quantities:

$$\begin{aligned} V_b &= T_b V_C + \Omega_b \times R_{Cb} \\ \dot{V}_b &= \dot{T}_b V_C + T_b \dot{V}_C + \dot{\Omega}_b \times R_{Cb} + \Omega_b \times \dot{R}_{Cb} \end{aligned} \quad (4.2)$$

and  $M_b$  is the payload mass matrix:

$$M_b = \begin{bmatrix} m_b & 0 & 0 \\ 0 & m_b & 0 \\ 0 & 0 & m_b \end{bmatrix} \quad (4.3)$$

Matrix  $T_b$  is the transformation matrix from an inertial reference frame to the payload reference frame:

$$T_b = \begin{bmatrix} C\theta_b C\psi_b & C\theta_b S\psi_b & -S\theta_b \\ S\phi_b S\theta_b C\psi_b - C\phi_b S\psi_b & S\phi_b S\theta_b S\psi_b + C\phi_b C\psi_b & S\phi_b C\theta_b \\ S\phi_b S\theta_b C\psi_b + S\phi_b S\psi_b & C\phi_b S\theta_b S\psi_b - S\phi_b C\psi_b & C\phi_b C\theta_b \end{bmatrix} \quad (4.4)$$

$(\Omega_b \times)$  is a cross-product-equivalent matrix for payload body axis angular velocity:

$$\Omega_b \times = \begin{bmatrix} 0 & -r_b & q_b \\ r_b & 0 & -p_b \\ -q_b & p_b & 0 \end{bmatrix} \quad (4.5)$$

And  $(R_{cb} \times)$  is cross product equivalent matrix of components of distance of payload mass center b from joint C in payload body-fixed reference frame:

$$R_{cb} \times = \begin{bmatrix} 0 & -z_{cb} & y_{cb} \\ z_{cb} & 0 & -x_{cb} \\ -y_{cb} & x_{cb} & 0 \end{bmatrix} \quad (4.6)$$

Here  $x_{cb} = 0, y_{cb} = 0$  and  $z_{cb} = R_{cb}$  due to the choice of the reference frame. The distance between joint C and payload mass center is constant, i.e.,  $\dot{R}_{cb} = 0$ , and  $\dot{T}_b = -\Omega_b \times T_b$ , hence

$$\dot{V}_b = (-\Omega_b \times T_b)V_c + T_b \dot{V}_c + \dot{\Omega}_b \times R_{cb} \quad (4.7)$$

Substituting,  $V_b, \dot{V}_b$  from equations 4. 2 and 4.7 in 4.1, we get

$$M_b T_b \dot{V}_c + M_b \dot{\Omega}_b \times R_{Cb} + M_b \Omega_b \times \Omega_b \times R_{Cb} = F_b^A + F_b^G + F_b^T - F_b^C \quad (4.8)$$

The rotational motion of the payload center of mass in payload-fixed reference frame is described by:

$$I_b \dot{\Omega}_b + \Omega_b \times I_b \Omega_b = R_{Cb} \times F_b^C \quad (4.9)$$

#### 4.4 PAYLOAD FORCES AND MOMENTS

The external forces acting on payload sub model are:

- Aerodynamic Force: The aerodynamic drag ( $C_D^b$ ) force acting at payload mass center in payload reference frame

$$F_b^A = \bar{q}_b S_b \begin{Bmatrix} C\alpha_b C_D^b \\ 0 \\ S\alpha_b C_D^b \end{Bmatrix} \quad (4.10)$$

Where,  $\bar{q}_b = \frac{1}{2} \rho V_b^2$ ,  $S_b$  is payload frontal area and  $\alpha_b = \tan^{-1}\left(\frac{w_b}{u_b}\right)$  is the local angle of attack of payload center of mass.

- Gravitational Force: the gravitational force acting at payload mass center in payload reference frame is

$$F_b^G = m_b g \begin{Bmatrix} -S\theta_b \\ S\phi_b C\theta_b \\ C\phi_b C\theta_b \end{Bmatrix} \quad (4.11)$$

Where,  $g$  is the acceleration due to gravity

- Joint Force: the internal joint C reaction forces expressed in payload reference are

$$F_b^C = \begin{bmatrix} C\theta_b C\psi_b & C\theta_b S\psi_b & -S\theta_b \\ S\phi_b S\theta_b C\psi_b - C\phi_b S\psi_b & S\phi_b S\theta_b S\psi_b + C\phi_b C\psi_b & S\phi_b C\theta_b \\ S\phi_b S\theta_b C\psi_b + S\phi_b S\psi_b & C\phi_b S\theta_b S\psi_b - S\phi_b C\psi_b & C\phi_b C\theta_b \end{bmatrix} \begin{Bmatrix} F_{Cx} \\ F_{Cy} \\ F_{Cz} \end{Bmatrix} \quad (4.12)$$

- Thrust force: the force due to the attached propulsion system in  $X_b$  direction

$$F_b^T = \begin{bmatrix} Th \\ 0 \\ 0 \end{bmatrix} \quad (4.13)$$

#### 4.5 PARAFOIL SUB MODEL

Figure 4.3 shows the Parafoil sub model consisting of Parafoil mass center P connected to joint C through link  $R_p$ . The Parafoil is allowed to rotate freely about the joint c having translational velocity  $V_p = \{u_p, v_p, w_p\}$ , angular velocity  $\Omega_p = \{p_p, q_p, r_p\}$ , and Euler angles  $(\Phi_p, \theta_p, \psi_p)$ . The forces acting on the Parafoil center of mass are aerodynamic force  $F_p^A$ , Gravitational force  $F_p^G$ , and internal Joint force  $F_p^C$  acts at joint C.

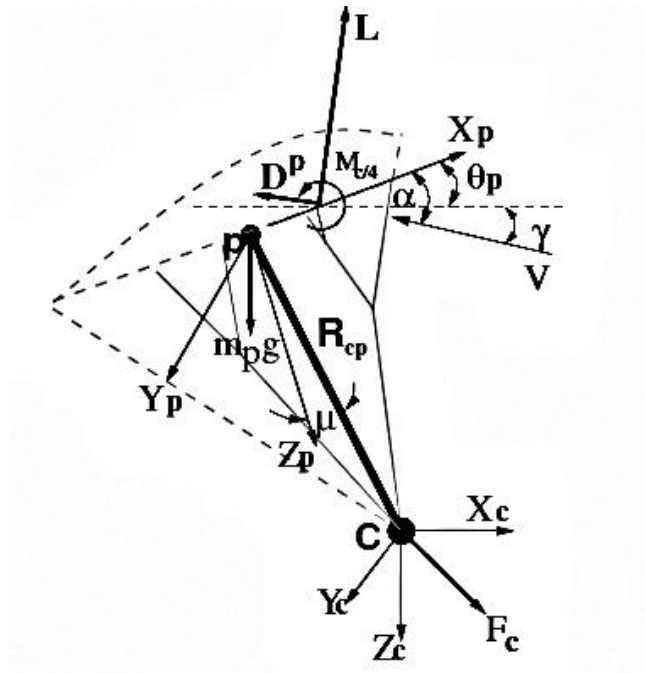


Figure 4.3: Parafoil Sub Model of Powered Parafoil Aerial Vehicle

Translational motion of payload center of mass in Parafoil-fixed reference frame can be expressed as

$$(M_p + M_F)\dot{V}_p + \Omega_p \times (M_p + M_F)V_p = F_p^A + F_p^G - F_p^C \quad (4.14)$$

Where,

$V_p, \dot{V}_p$  are inertial reference frame quantities:

$$\begin{aligned}
V_p &= T_p V_C + \Omega_p \times R_{Cp} \\
\dot{V}_p &= \dot{T}_p V_C + T_p \dot{V}_C + \dot{\Omega}_p \times R_{Cp} + \Omega_p \times \dot{R}_{Cp}
\end{aligned} \tag{4.15}$$

and  $M_p$  is the Parafoil mass matrix and  $M_F$  is Parafoil Apparent mass:

$$M_p = \begin{bmatrix} m_p & 0 & 0 \\ 0 & m_p & 0 \\ 0 & 0 & m_p \end{bmatrix} \tag{4.16}$$

$$M_F = \begin{bmatrix} A & 0 & 0 \\ 0 & B & 0 \\ 0 & 0 & C \end{bmatrix} \tag{4.17}$$

Matrix  $T_p$  is the transformation matrix from an inertial reference frame to the Parafoil reference frame:

$$T_p = \begin{bmatrix} C\theta_p C\psi_p & C\theta_p S\psi_p & -S\theta_p \\ S\phi_p S\theta_p C\psi_p - C\phi_p S\psi_p & S\phi_p S\theta_p S\psi_p + C\phi_p C\psi_p & S\phi_p C\theta_p \\ S\phi_p S\theta_p C\psi_p + S\phi_p S\psi_p & C\phi_p S\theta_p S\psi_p - S\phi_p C\psi_p & C\phi_p C\theta_p \end{bmatrix} \tag{4.18}$$

$(\Omega_p \times)$  is a cross-product-equivalent matrix for Parafoil body axis angular velocity:

$$\Omega_p \times = \begin{bmatrix} 0 & -r_p & q_p \\ r_p & 0 & -p_p \\ -q_p & p_p & 0 \end{bmatrix} \tag{4.19}$$

And  $(R_{cp} \times)$  is cross product equivalent matrix of components of distance of Parafoil mass center b from joint C in Parafoil body-fixed reference frame:

$$R_{cp} \times = \begin{bmatrix} 0 & -z_{cp} & y_{cp} \\ z_{cp} & 0 & -x_{cp} \\ -y_{cp} & x_{cp} & 0 \end{bmatrix} \tag{4.20}$$

The distance between joint C and payload mass center is constant, i.e.,  $\dot{R}_{cp} = 0$ , and  $\dot{T}_p = -\Omega_p \times T_p$ , hence

$$\dot{V}_p = (-\Omega_p \times T_p)V_C + T_p\dot{V}_C + \dot{\Omega}_p \times R_{Cp} \quad (4.21)$$

Substituting  $V_p, \dot{V}_p$  from equations 4.15 and 4.21 in 4.14, we get

$$(M_p + M_F)T_p\dot{V}_C + (M_p + M_F)\dot{\Omega}_p \times R_{Cp} - M_F\Omega_b \times T_pV_C + \Omega_p \times M_F T_pV_C + \Omega_p \times (M_p + M_F)\Omega_p \times R_{Cp} = F_p^A + F_p^G - F_p^C \quad (4.22)$$

The rotational motion of the Parafoil center of mass in Parafoil-fixed reference frame is described by:

$$I_p\dot{\Omega}_p + \Omega_p \times I_p\Omega_p = M_p - R_{Cp} \times F_p^C \quad (4.23)$$

#### 4.6 PARAFOIL FORCES AND MOMENTS

The external forces acting on Parafoil sub model are:

- **Aerodynamic Force:** The aerodynamic forces acting at Parafoil mass center in payload reference frame

$$F_p^A = \bar{q}_p S_p \begin{Bmatrix} C_X \\ C_Y \\ C_Z \end{Bmatrix} \quad (4.24)$$

Where,  $\bar{q}_p = \frac{1}{2} \rho V_p^2$ ,  $S_p$  is Parafoil surface area and  $\alpha_p = \tan^{-1} \left( \frac{w_p}{u_p} \right)$  is the local

angle of attack of payload center of mass and  $C_X, C_Y, C_Z$  are components of aerodynamic force in Parafoil – fixed reference frame.

- **Gravitational Force:** the gravitational force acting at Parafoil mass center in Parafoil reference frame is



$$F_p^G = m_p g \begin{Bmatrix} -S\theta_p \\ S\phi_p C\theta_p \\ C\phi_p C\theta_p \end{Bmatrix} \quad (4.25)$$

Where,  $g$  is the acceleration due to gravity

- Joint Force: the internal joint C reaction forces expressed in payload reference are

$$F_p^C = \begin{bmatrix} C\theta_p C\psi_p & C\theta_p S\psi_p & -S\theta_p \\ S\phi_p S\theta_p C\psi_p - C\phi_p S\psi_p & S\phi_p S\theta_p S\psi_p + C\phi_p C\psi_p & S\phi_p C\theta_p \\ S\phi_p S\theta_p C\psi_p + S\phi_p S\psi_p & C\phi_p S\theta_p S\psi_p - S\phi_p C\psi_p & C\phi_p C\theta_p \end{bmatrix} \begin{Bmatrix} F_{Cx} \\ F_{Cy} \\ F_{Cz} \end{Bmatrix} \quad (4.26)$$

#### 4.7 NINE DEGREES OF FREEDOM MODEL

Collecting Parafoil translational and rotational motion equations, Payload translational and rotational motion equations we get nine degrees of freedom equations of motion of combines Parafoil payload system in concatenated matrix form as:

$$\begin{bmatrix} -M_b R_{cb} & 0 & -M_b T_b & T_b \\ 0 & -(M_p + M_F) R_{cp} & -(M_p + M_F) T_p & -T_b \\ I_b & 0 & 0 & -R_{cb} T_b \\ 0 & I_p + I_M & 0 & R_{cp} T_p \end{bmatrix} \begin{bmatrix} \dot{\omega}_b \\ \dot{\omega}_p \\ V_c \\ F_c \end{bmatrix} = \begin{bmatrix} B_1 \\ B_2 \\ B_3 \\ B_4 \end{bmatrix} \quad (4.27)$$

$$\begin{aligned} B_1 &= F_b^A + F_b^G + F_b^T - \omega_b \times M_b \omega_b \times R_{cb} \\ B_2 &= F_p^A + F_p^G - \omega \times (M_p + M_F) \omega_p \times R_{cp} + M_F \omega_p \times T_p V_c - \omega_p \times M_F T_p V_c \\ B_3 &= -\omega_b \times I_b \omega_b - M_c \\ B_4 &= M_p^A - \omega_p \times (I_p + I_M) \omega_p + M_c \end{aligned} \quad (4.28)$$

Where,

$$M_c = \begin{bmatrix} 0 \\ 0 \\ K_c (\Psi_p - \Psi_b) + C_c (\dot{\Psi}_p - \dot{\Psi}_b) \end{bmatrix} \quad (4.29)$$

$$\Psi_p = \tan^{-1} \left( \frac{\sin \Phi_p \sin \theta_p \cos \Psi_p + \cos \Phi_p \sin \Psi_p}{\cos \theta_p \cos \Psi_p} \right) \quad (4.30)$$

$$\Psi_b = \tan^{-1} \left( \frac{\sin \Phi_b \sin \theta_b \cos \Psi_b + \cos \Phi_b \sin \Psi_b}{\cos \theta_b \cos \Psi_b} \right)$$

$$\dot{\Psi}_p = -\cos \Psi_p \tan \theta_p \dot{p}_p + \sin \Psi_p \tan \theta_p \dot{q}_p + r_p \quad (4.31)$$

$$\dot{\Psi}_b = -\cos \Psi_b \tan \theta_b \dot{p}_b + \sin \Psi_b \tan \theta_b \dot{q}_b + r_b \quad (4.32)$$

$$\tan \theta_p = \frac{\cos \Phi_p \sin \theta_p \cos \Psi_p - \sin \Phi_p \sin \Psi_p}{\cos \theta_p \cos \Psi_p} \cos \dot{\Psi}_p \quad (4.33)$$

$$\tan \theta_b = \frac{\cos \Phi_b \sin \theta_b \cos \Psi_b - \sin \Phi_b \sin \Psi_b}{\cos \theta_b \cos \Psi_b} \cos \dot{\Psi}_b \quad (4.34)$$

The rotational stiffness and damping coefficients at joint C is taken as 0.35N.m/rad and 0.25N.m/rad

$$\begin{aligned} \begin{Bmatrix} \dot{x}_C \\ \dot{y}_C \\ \dot{z}_C \end{Bmatrix} &= \begin{Bmatrix} u_C \\ v_C \\ w_C \end{Bmatrix} \\ \begin{Bmatrix} \dot{\phi}_b \\ \dot{\theta}_b \\ \dot{\psi}_b \end{Bmatrix} &= \begin{bmatrix} 1 & S\phi_b t\theta_b & C\phi_b t\theta_b \\ 0 & C\phi_b & -S\phi_b \\ 0 & \frac{S\phi_b}{C\theta_b} & \frac{C\phi_b}{C\theta_b} \end{bmatrix} \begin{Bmatrix} p_b \\ q_b \\ r_b \end{Bmatrix} \\ \begin{Bmatrix} \dot{\phi}_p \\ \dot{\theta}_p \\ \dot{\psi}_p \end{Bmatrix} &= \begin{bmatrix} 1 & S\phi_p t\theta_p & C\phi_p t\theta_p \\ 0 & C\phi_p & -S\phi_p \\ 0 & \frac{S\phi_p}{C\theta_p} & \frac{C\phi_p}{C\theta_p} \end{bmatrix} \begin{Bmatrix} p_p \\ q_p \\ r_p \end{Bmatrix} \end{aligned} \quad (4.35)$$

Equation 4.27 gives 12 equations of 9 equations of motion and 3 joint force equations. Thus, the 9 equations from equation 4.27, together with kinematic equations 4.27, 4.28 and 4.35 give 21 equations of motion for combined Parafoil

– payload system in 18 state variables. The 3 additional equations in equation 4.26 give magnitude of internal forces at joint C.

#### 4.8 RIGGING ANGLE MODELING

As shown in figure 4.4, the rigging angle  $\mu$  is the angle between the line joining mid-baseline point of the canopy to the joint C and the line parallel to the  $Z_p$  axis passing through the mid baseline point. Therefore,

$$\begin{aligned} Z_{cp} &= R_{cp} \cos \mu \\ X_{cp} &= R_{cp} \sin \mu \\ Y_{cp} &= 0 \end{aligned} \tag{4.36}$$

#### 4.9 DIRECTION CONTROL MODELING

As shown in figure 4.5, the angle  $\delta_s$  is the angle between the mid-baseline point and the steer bar tilt, this angle is called canopy tilt angle. Therefore,

$$\begin{aligned} Z_{cp}^2 &= Z_{cp} \cos \delta_s \\ X_{cp}^2 &= Z_{cp} \\ Y_{cp}^2 &= -Z_{cp} \sin \delta_s \end{aligned} \tag{4.37}$$

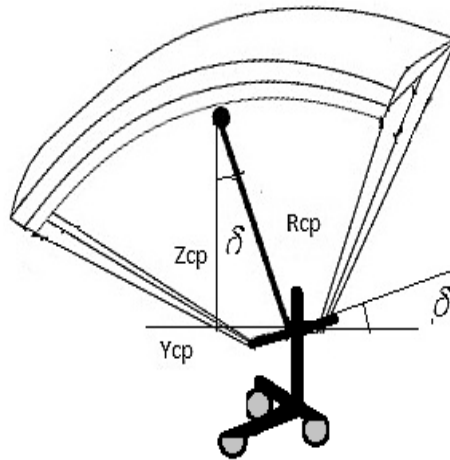


Figure 4.4: Direction Control Model

#### 4.10 APPARENT MASS TERMS

Unlike aircraft, Parafoil-payload is a lightly wing-loaded system. Therefore, apparent mass terms show a strong effect on Parafoil- payload system dynamics. The apparent mass terms show a strong effect on Parafoil-payload system dynamics. The apparent mass (A, B, C) and inertia (I<sub>a</sub>, I<sub>b</sub>,I<sub>c</sub>) terms are estimated from the analytical formulas.

$$\begin{aligned}
 A &= K_A \frac{\pi}{4} t^2 b \\
 B &= K_B \frac{\pi}{4} t^2 c \\
 C &= K_C \frac{\pi}{4} c^2 b \\
 I_A &= K_A^* \frac{\pi}{48} c^2 b^3 \\
 I_B &= K_B^* \frac{\pi}{48} c^4 b \\
 I_C &= K_C^* \frac{\pi}{48} t^2 b^3
 \end{aligned} \tag{4.38}$$

Where

$$\begin{aligned}
 K_A &= 0.85(1 + \frac{8}{3} h^{*2}) \\
 K_B &= 1(\text{Barrows}[24]) \\
 K_C &= [1 + 2h^{*2}(1 - t^{*2})]^{1/2} \frac{A^*}{1 + A^*} \\
 K_A^* &= 0.84 \frac{A^*}{1 + A^*} \\
 K_B^* &= 1.161 \frac{A^*}{1 + A^*} [1 + \frac{\pi}{6} (1 + A^*) A^* h^{*2} t^{*2}] \\
 K_C^* &= 0.855(1 + 8h^{*2})
 \end{aligned} \tag{4.39}$$

These apparent mass and inertia terms are to be multiplied by local air density  $\rho$ .

The included mass  $m_{pl} = \frac{\rho bct}{2}$  and corresponding inertia of the air inside the

canopy are added to respective terms of equation 4.39 to get the final apparent mass and inertia of the Parafoil.

#### 4.11 AERODYNAMIC MODEL

The aerodynamic forces and moments acting at Parafoil canopy mass center are modeled in terms of aerodynamic force and moment coefficients as (the values are extracted from Table 4.1):

$$\begin{aligned}
 C_L &= C_L(\alpha_p, \delta_s) \\
 C_D^p &= C_D(\alpha_p, \delta_s) \\
 C_Y &= C_{Y\beta} + C_{Y\gamma} r_p \frac{b}{2V_p}
 \end{aligned} \tag{4.40}$$

In terms of Parafoil canopy-fixed axis coefficients:

$$\begin{aligned}
 C_X &= (-C_D^p u_p + C_L w_p) / V_p \\
 C_Y &= C_Y \\
 C_Z &= (-C_D^p w_p + C_L u_p) / V_p \\
 C_l &= C_{l\beta} \beta + C_{lp} p_p \frac{b}{2V_p} + C_{lr} r_p \frac{b}{2V_p} \\
 C_m &= \{C_{m\alpha/4}(\alpha_p, \delta_s) + x_{pa} C_Z\} + C_{mq} q_p \frac{C}{2V_p} \\
 C_n &= C_{n\beta} \beta + C_{np} p_p \frac{b}{2V_p} + C_{nr} r_p \frac{b}{2V_p}
 \end{aligned} \tag{4.41}$$

| Parameter     | Value       |
|---------------|-------------|
| $C_{L0}$      | 0.45[34]    |
| $C_{D0}$      | 0.15[34]    |
| $C_{Y\beta}$  | -0.0095/deg |
| $C_{Y\gamma}$ | -0.0060/deg |
| $C_{l\beta}$  | -0.0014/deg |

|              |             |
|--------------|-------------|
| $C_{lp}$     | -0.1330     |
| $C_{lr}$     | 0.0100      |
| $C_{n\beta}$ | 0.0005/deg  |
| $C_{np}$     | -0.0130     |
| $C_{nr}$     | -0.0350/deg |

Table 4.1. Lateral Derivatives

Since a single servo is used to control the direction of the PAV, the servo angle is represented as  $\delta_s$ . Since both the ends of the canopy is connected to a “fly-bar”  $\delta_s$  gives positive and negative values representing left and right turn, as there is no asymmetric brake deflection in our model.

#### 4.12 OPEN LOOP SIMULATION RESULTS

The developed PAV model has been validated using the Lingard model. Angle of attack (alpha), pitch angle (theta) and glide angle (gamma) values obtained (shown in the Figure 4.5) are compared with the Lingard values under no thrust conditions

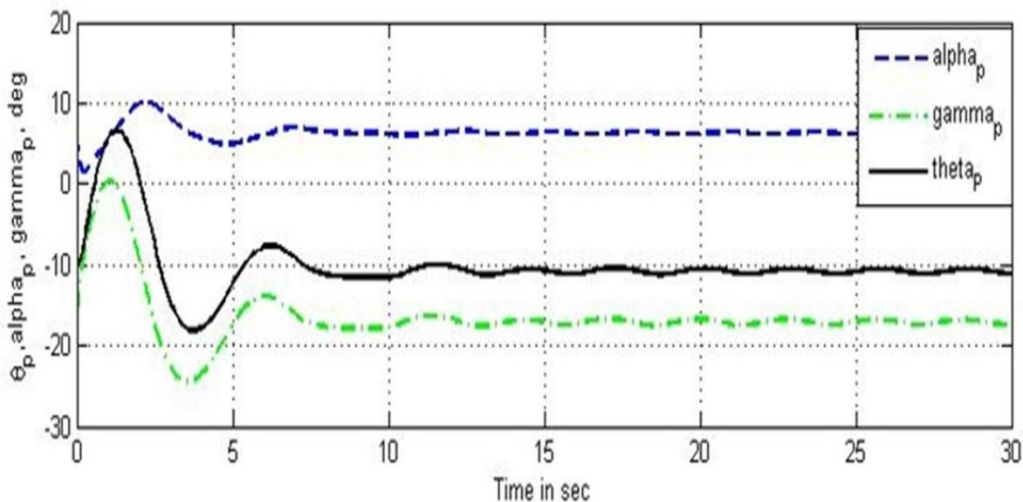


Figure 4.5. Parachute Aerial Vehicle under no Thrust condition

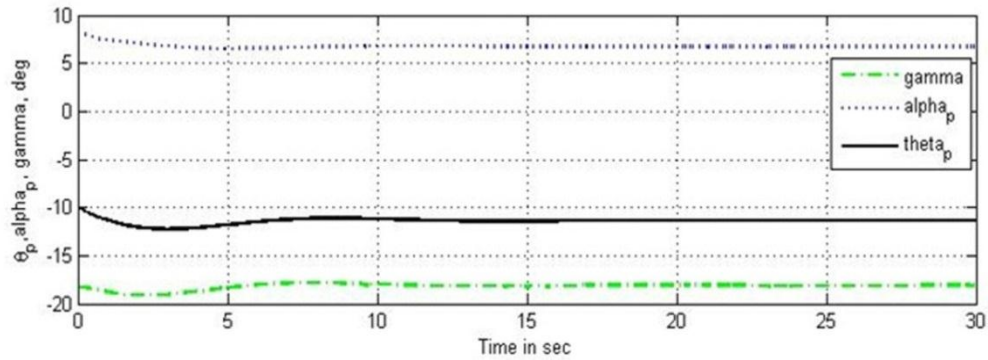


Figure 4.6. Validation of Parachute Aerial Vehicle with Lingard model

The model is validated using the Lingard results (shown in Figure 4.6) by checking the values of angle of attack ( $\alpha$ ), pitch angle ( $\theta$ ) and glide angle ( $\gamma$ ) of the Parafoil with respect to time. From Table 4.2 it can be observed that the developed 9 DOF model is providing accurate data. The developed 9 DOF simulation model has been simulated at various thrust conditions, keeping the thrust as 4.5N, 7.75N and 10N (Shown in Figure 4.6). It is observed that the  $\gamma$  value is zero at the thrust input of 7.75N. This indicates that at thrust value 7.75N the vehicle is maintaining a level flight. Table 4.3 also indicates the same.

|                      | Lingard | Parachute Aerial vehicle (Thrust = 0N) |
|----------------------|---------|--|
| <b>Alpha_p (deg)</b> | 3       | 5                                      |
| <b>Theta_p (deg)</b> | -9      | -10                                    |
| <b>Gamma(deg)</b>    | -18     | -18                                    |

Table 4.2. Powered Parafoil Model validation with Lingard's Model

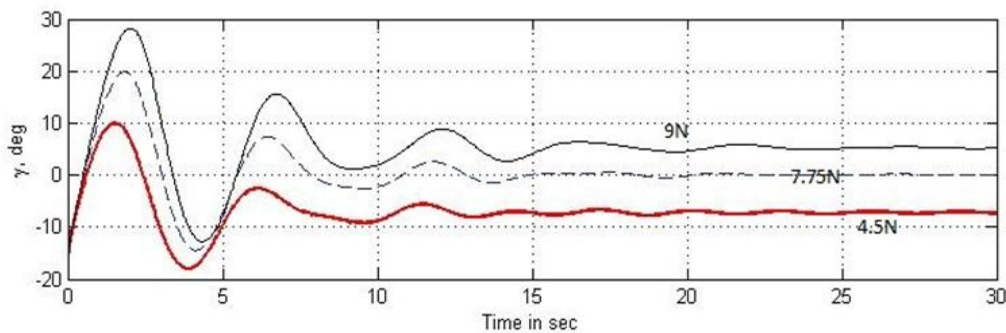


Figure 4.7. Gamma values for various thrust conditions

| S.No. | Thrust (N) | Gamma(deg) |
|-------|------------|------------|
| 1     | 4.5        | -8         |
| 2     | 7.75       | 0          |
| 3     | 9          | 7          |

Table 4.3. Gamma values for various thrust conditions

Keeping the thrust value 7.75N the alpha, theta and gamma values are seen in Figure 4.7.

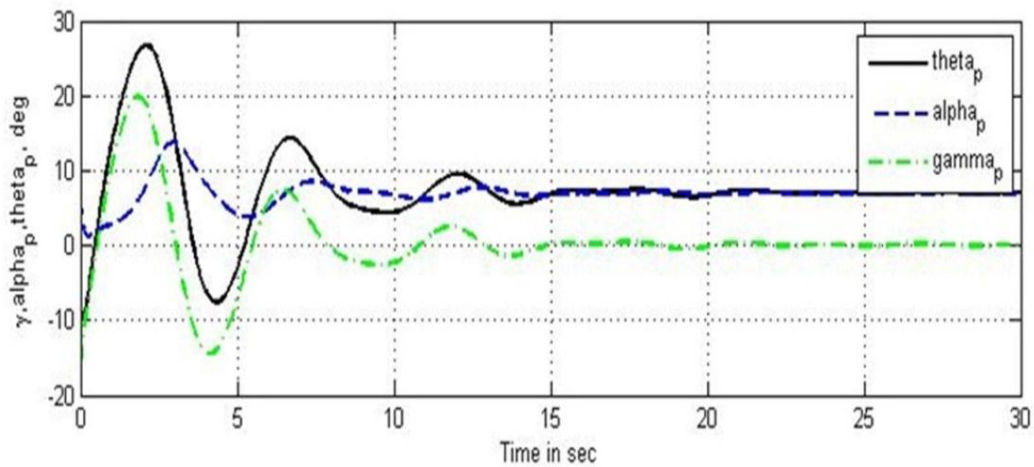


Figure 4.8. Parachute Aerial Vehicle with 7.75N thrust

|               | Parachute Aerial vehicle<br>(Thrust = 4.5N) | Parachute Aerial vehicle<br>(Thrust= 7.75N) | Parachute Aerial vehicle<br>(Thrust = 9N) |
|---------------|---|---|---|
| Alpha_p (deg) | 10  | 8   | 7   |
| Theta_p (deg) | 0   | 8   | 10  |
| Gamma(deg)    | -8  | 0   | 7   |

Table 4.4. Alpha, beta and gamma values for various thrust conditions



From the figure 4.8, the theta value can be observed, while landing there is glide angle of approximately 8 degrees.

Figure 4.9, shows that, at 0N thrust the vehicle loses 150ft altitude as it move 450ft forward. Theoretically the L/D ratio of a ram air Parafoil is 3. From this Figure 4.9 the ratio of the altitude lost to the distance covered is 3, which can be validated with the Lingard's L/D value. It can be further concluded that, as the thrust increases the amount of altitude lost decreases. Figure 4.9, further describes that under gliding condition the Parafoil vehicle loses 70 m as it travels 240 m.

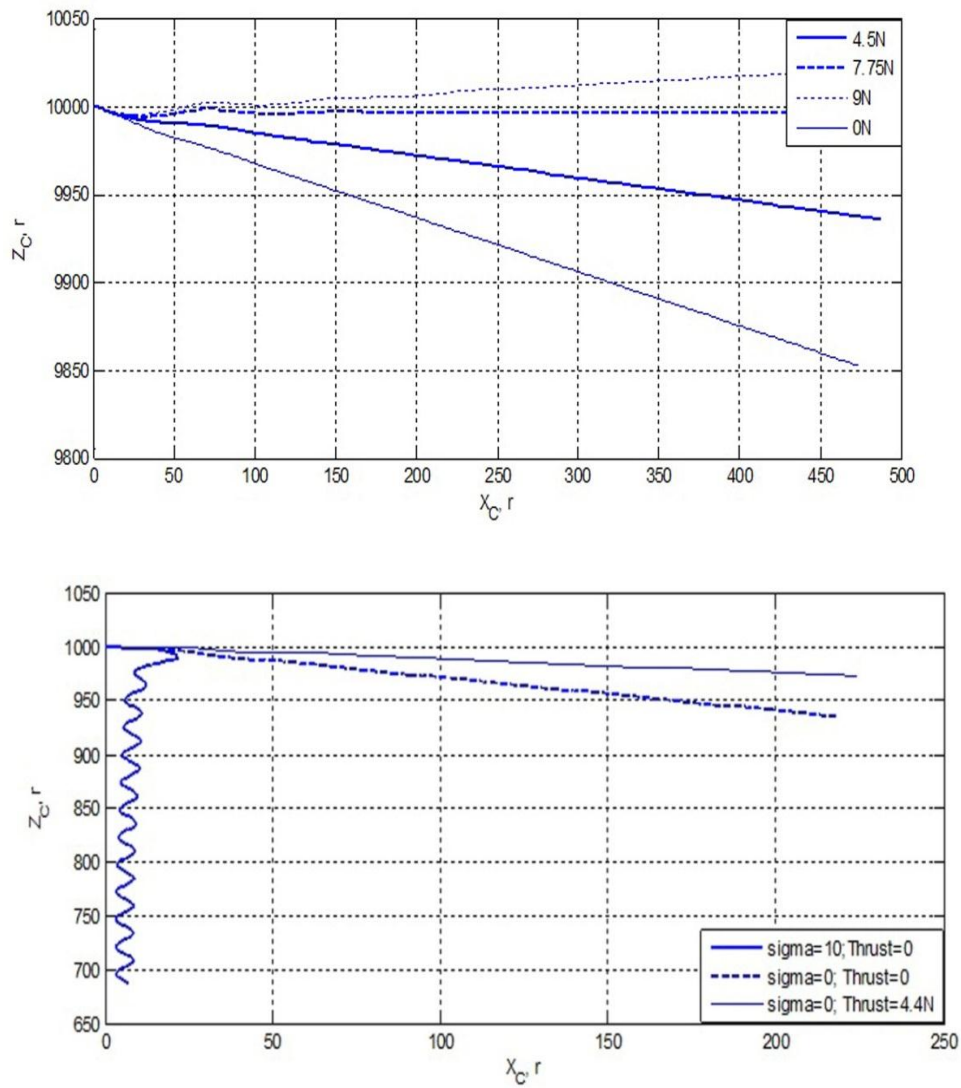


Figure 4.9. Altitude loss at various thrust and sigma inputs.

When the thrust is added to the vehicle the vehicle covers a distance up-to 300ft to lose an altitude of 60ft. To land the vehicle with in the glide range one end of the steer bar should be pulled so that the vehicle turns and make spiral landing. Figure 4.9 shows the front view and the top view of the direction control model keeping the canopy tilt angle to be 10 degrees. Keeping the sigma value to be 10 degrees, the  $Y_c, X_c$ , plot is as shown in the figure 4.10.

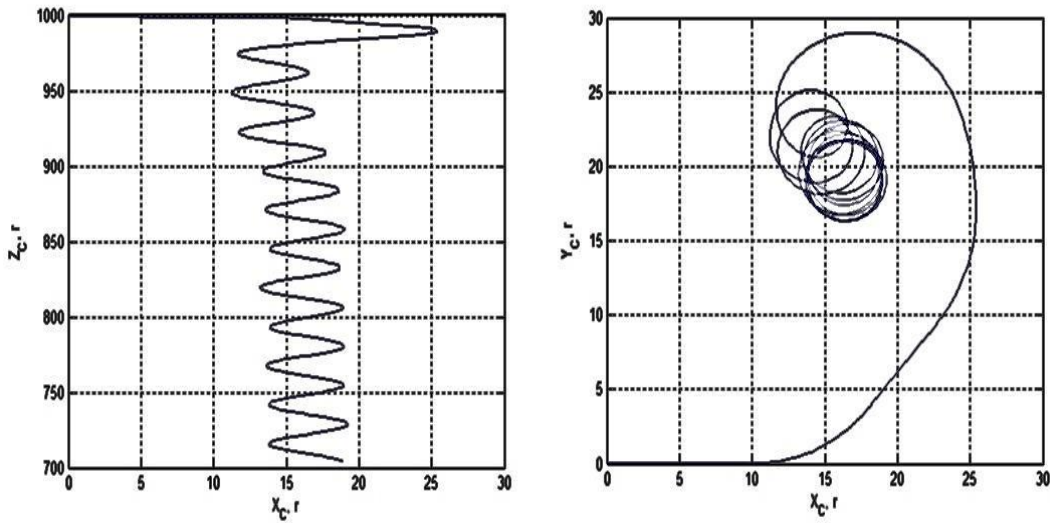


Figure 4.10.  $X_c$  Vs  $Z_c$  and  $X_c$  Vs  $Y_c$  Plot with  $\delta = 10$  degrees

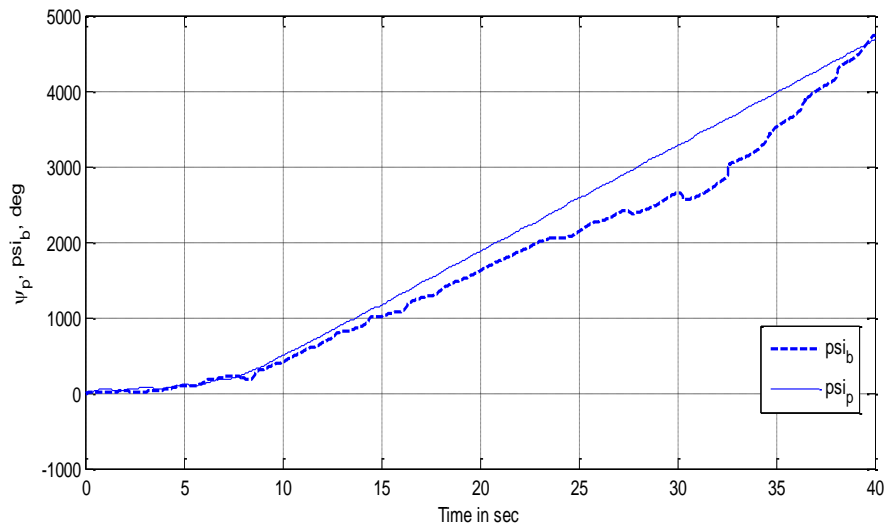


Figure 4.11.  $\psi_b, \psi_p$  Vs Time

The  $\psi_b$  and  $\psi_p$  curve with respect to time is plotted for about 5000 degrees with the  $\sigma$  value 10 degrees as shown in figure 4.11. It is observed that the payload tends to have certain oscillations but after certain time it tries to re-orient itself when Parafoil yaws during a turn.

| Cases | Tilt Angle (Degrees)<br>$\delta_s$ | Turn Rate (Degrees/Sec) |
|-------|------------------------------------|-------------------------|
| A     | +20                                | 20                      |
| B     | +10                                | 10                      |
| C     | +5                                 | 5                       |
| D     | +2                                 | 2                       |
| E     | -2                                 | -2                      |
| F     | -5                                 | -5                      |
| G     | -10                                | -10                     |
| H     | -20                                | -20                     |

Table 4.5. Tilt Angle and Turn Rate values for various cases

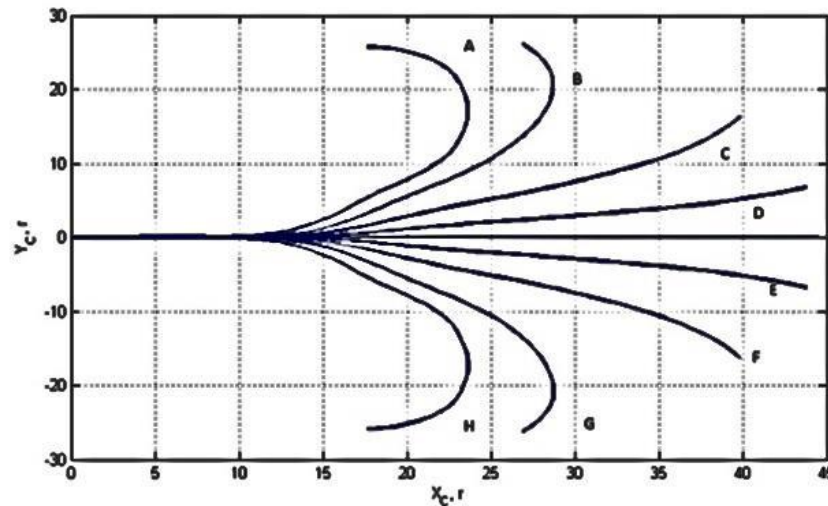


Figure 4.12. Canopy Tilt angle Vs Horizontal Distance Covered (Simulated and Flight Results)

Figure 4.12 shows the response of the powered Parafoil vehicle with different canopy tilt angles. For positive tilt angle the vehicle turns in the positive Y direction and for negative tilt angle the vehicle moves in the negative Y direction. Figure 4.13 shows the turn rates for various tilt angles under various cases, A, B, C, D, E, F, G, H, I. In the practical flight test the vehicle was responding in the similar manner, i.e. when the servo tilts right the vehicle also moves right and when servo tilts left the vehicle also turns left and the same can be observed in figure 4.13.

| S.No | Servo               | Simulated Radius (m) | Flight Test Radius (m) |
|------|---------------------|----------------------|------------------------|
| 1    | Minimum Servo Angle | 25m                  | 18m                    |
| 2    | Maximum Servo Angle | 50m                  | 52m                    |

Table 4.6. Turning Radius Vs Distance Covered (Simulated and Flight Results)

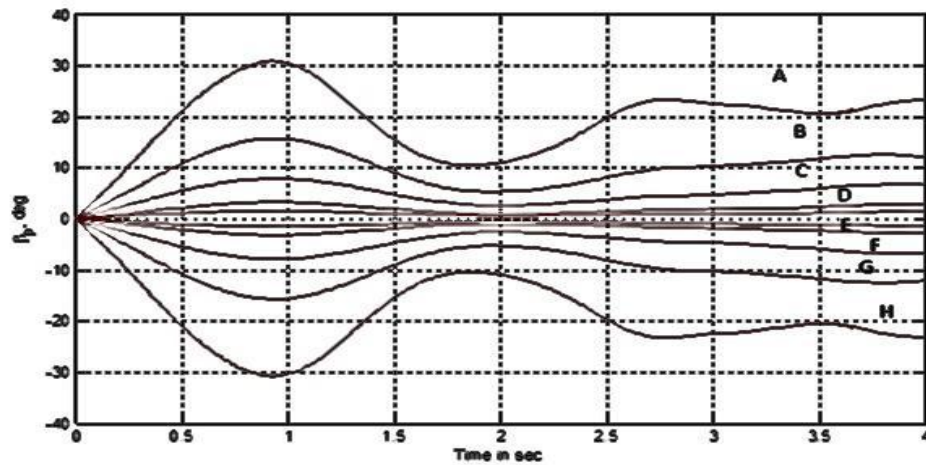


Figure. 4.13. Turn Rate Vs Time

As seen in the figure 4.12, it can be observed that the vehicle took 18m radius to turn with minimum servo turn. Similarly the vehicle took 52 m radius to turn with maximum servo turn.

### 4.13 OPEN LOOP FLIGHT TEST RESULTS

As discussed in chapter 3, open loop flight tests were done to understand the system behavior. Flight tests were done for take-off, landing and turn performance analysis.

These results would give an insight about the attitude of the Powered Parafoil Aerial Vehicle. Which helped us in interpreting the controller gain values as discussed in chapter 3.

#### 4.13.1 Take-Off Mode

During the take-off mode the pitch angle observed is about 20 degrees. These variations are due to vibration of the motor.

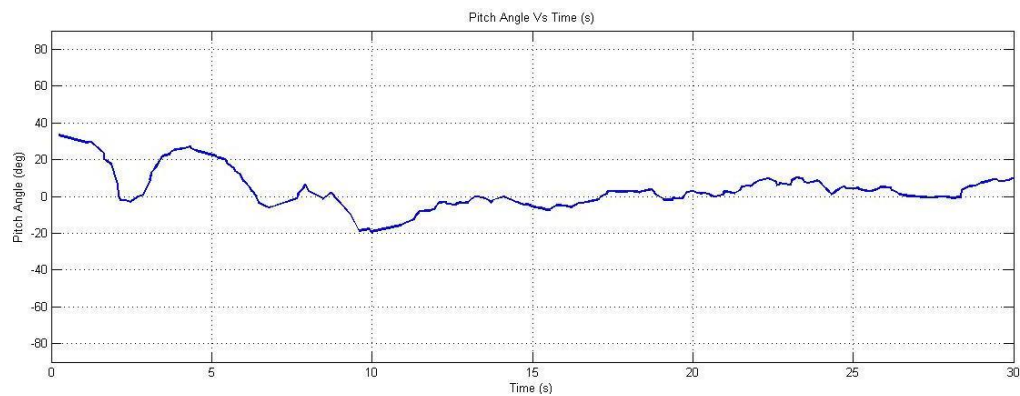


Figure. 4.14. Pitch Variation of PAV during Take off

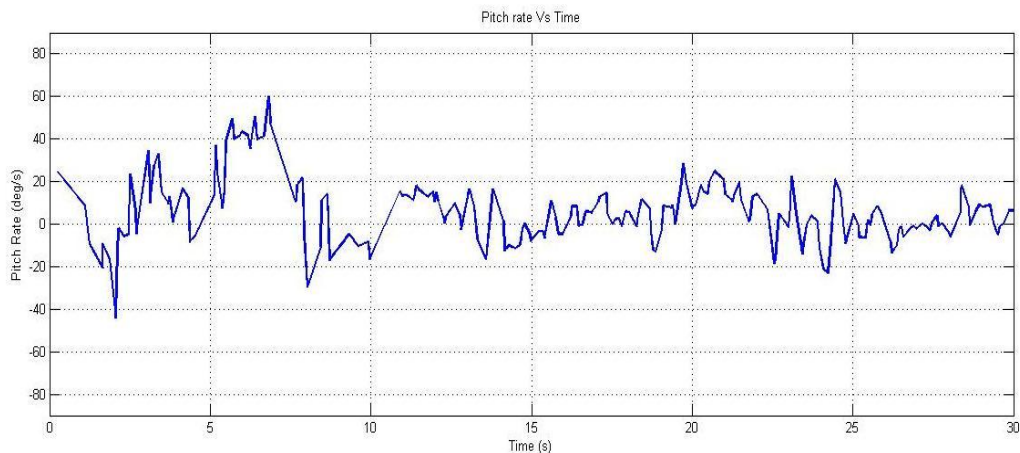


Figure. 4.15. Rate of Pitch Variation of PAV During Take Off

The pitch angle tends to increase indicating that the vehicle tends to climb for 7 seconds. After 7 seconds the PAV tried achieve a level flight decreasing the pitch angle. The rate of pitch also is also maintained about zero. This can be observed in figures 4.14 and 4.15.

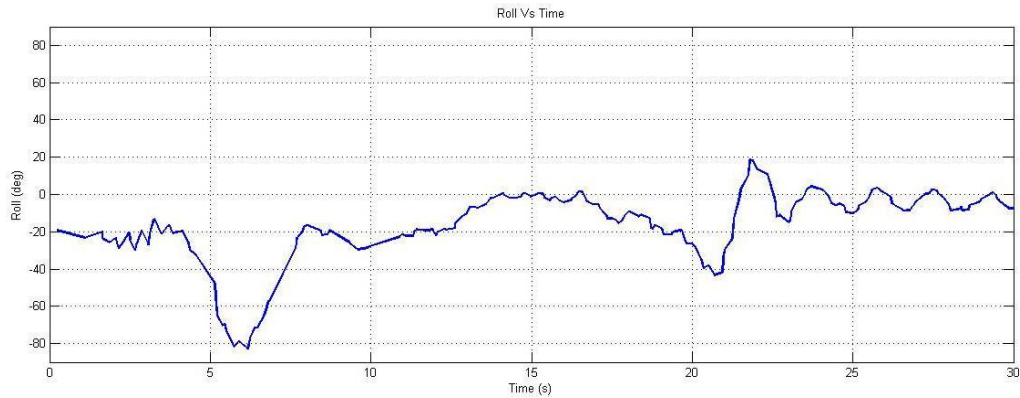


Figure 4.16. Roll Variation of PAV During Take Off

The roll variation is about -20 degrees initially. This initial angle is due to the turn as seen in the latitude longitude graph. The variations are due to the vibrations due to the motor attached on the payload. Figure 4.16 and 4.17 replicates the same. The roll rate is also about zero degrees due to the static stability of the vehicle. The oscillation are about +/- 20 degrees.

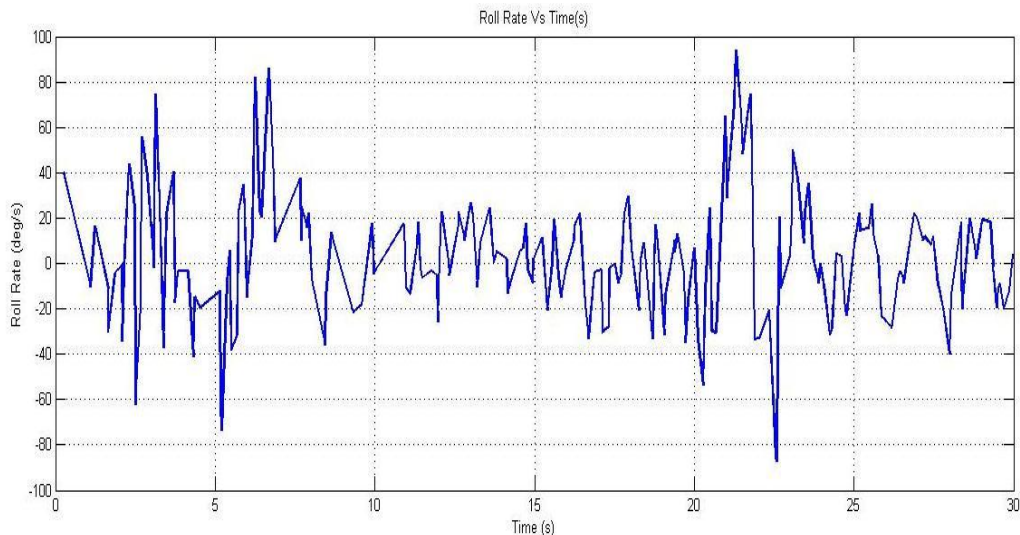


Figure 4.17. Roll Rate Variation of PAV During Take Off

The vibrations are observed due to the large motor propeller. It can be highlighted that due to the vibrations a variation in the values are observed. The range of the variations tends to be very small. In figure 4.18 it can be observed that the PAV take off and the takes a left turn

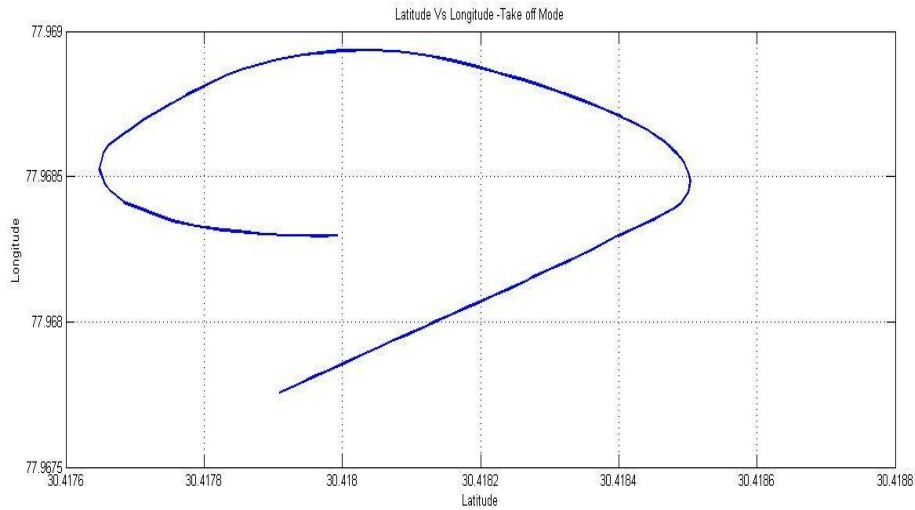


Figure 4.18. PAV Latitude and longitude Positions During Take-Off.

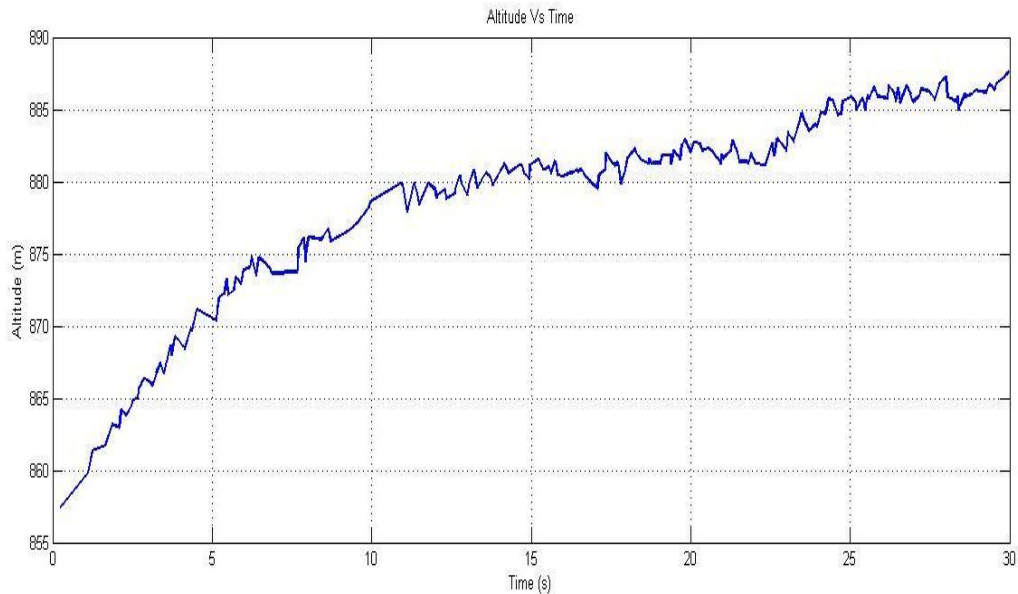


Figure 4.19. PAV Altitude variation during the takeoff

Figure 4.18 and 4.19 shows the PAV position with respect to latitude, longitude and altitude. The PAV tends to gain an altitude of 30m in 250ms.

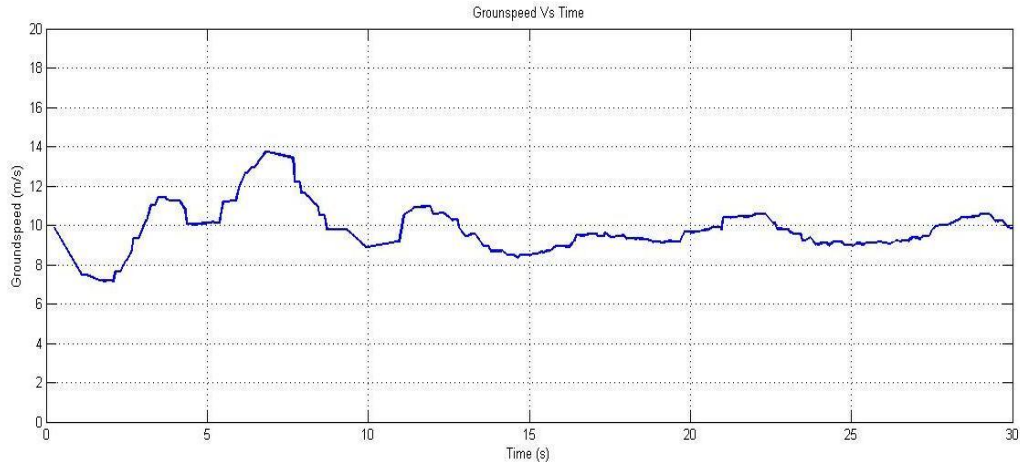


Figure 4.20. PAV Ground Speed during Take-Off

The ground speed remains to be approximately 10m/s during take-off which can be seen in figure 4.20. It can be further observed from figure 4.18 and 4.19 that during the take-off flight, while the vehicle is turning it there are less number of oscillations, while the vehicle is climbing up oscillations is more.

#### 4.13.2 Landing

During the landing mode the pitch angle observed is about -2.5 degrees. These variations are due to vibration of the motors. The pitch angle tends to decrease indicating that the vehicle is tending to climb down. The rate of pitch also is also maintained about zero. The same can be seen figure 4.21 and 4.22.

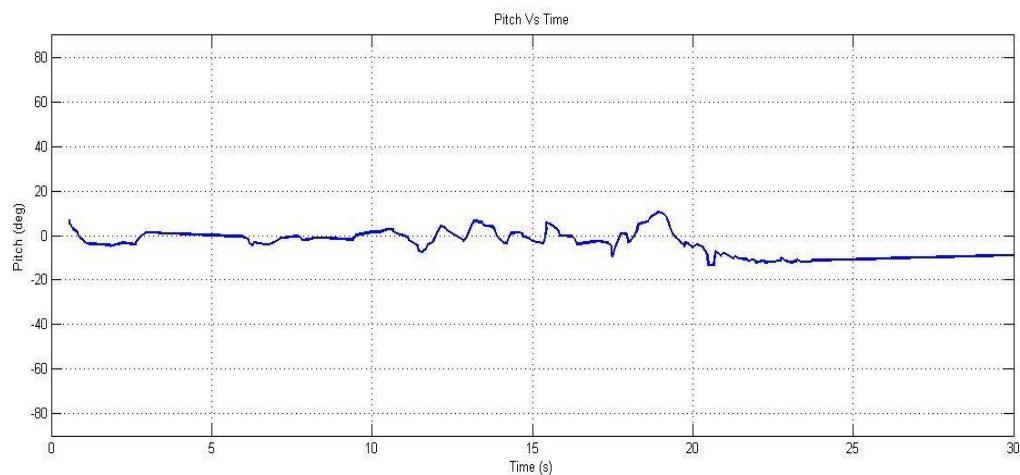


Figure 4.21. Pitch Variation of during Landing



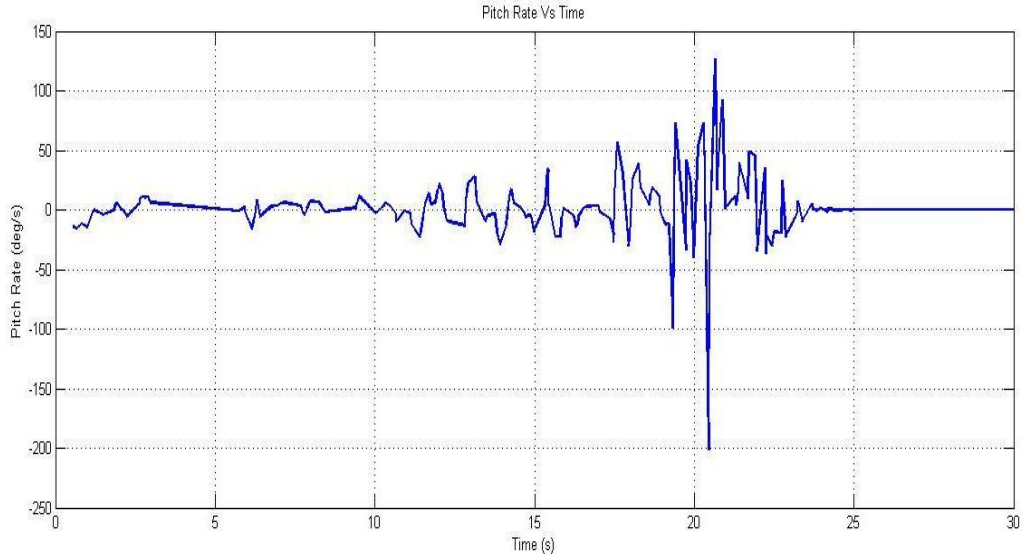


Figure 4.22. Pitch Rate Variation of during Landing

The roll variation is about 11 degrees. The variations are due to the vibrations due to the motor attached on the payload. Figure 4.23 and 4.24 replicates the same.

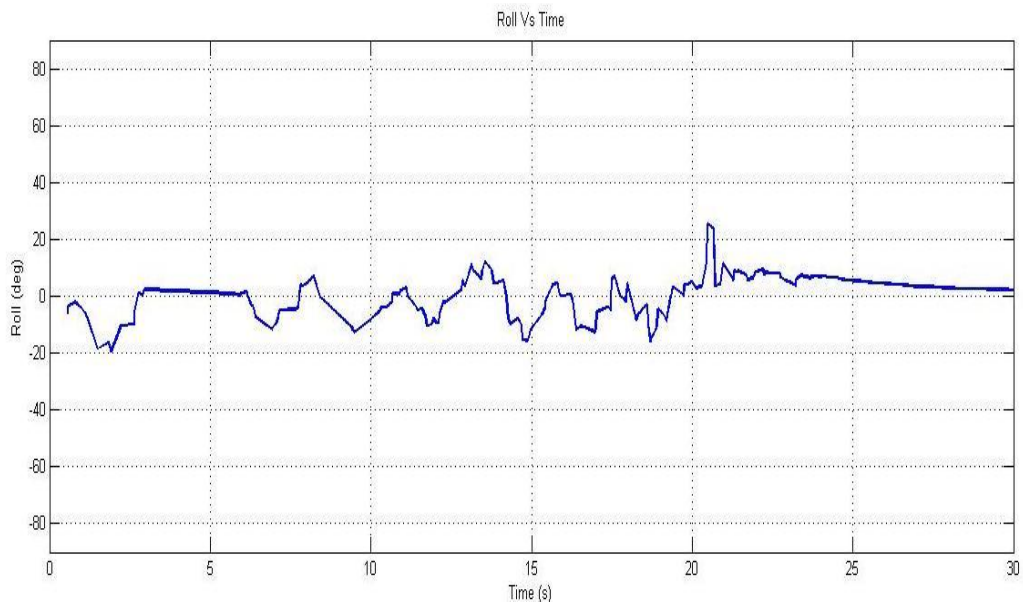


Figure 4.23. Roll Variation of PAV during Landing

The roll rate is also about zero degrees due to the static stability of the vehicle. The oscillation are about +/- 5.7 degrees.

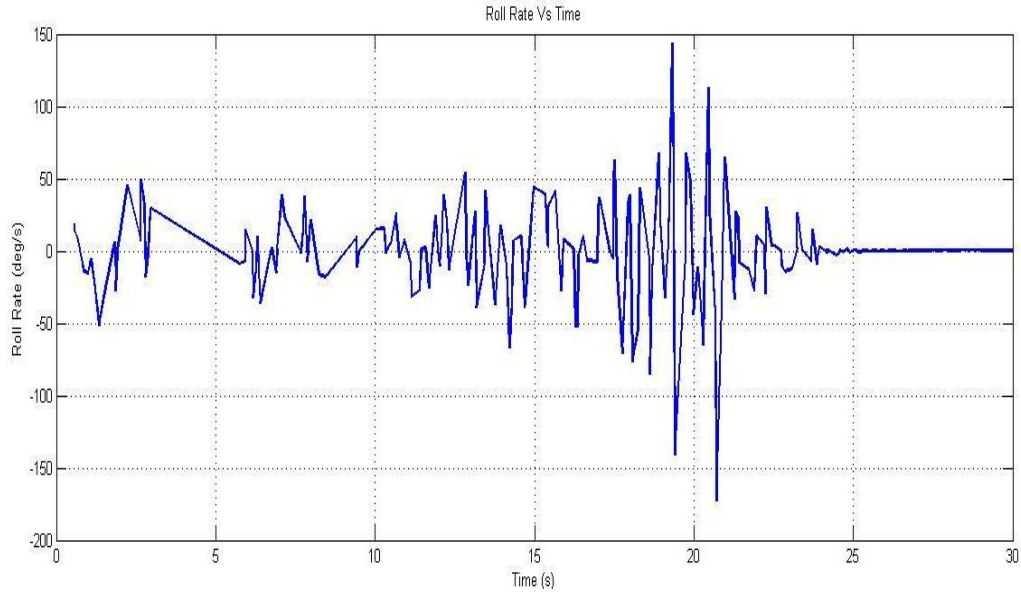


Figure 4.24. Roll Rate Variation of PAV during Landing

The Yaw Pitch and Roll values are plotted while take off the. The vibrations are observed due to the large motor propeller. A lot of oscillations are found in pitch rate, roll rate and yaw rate during touch down. These oscillations are due to the flare maneuver. Figure 4.25 shows the PAV position with respect to latitude, longitude and altitude.

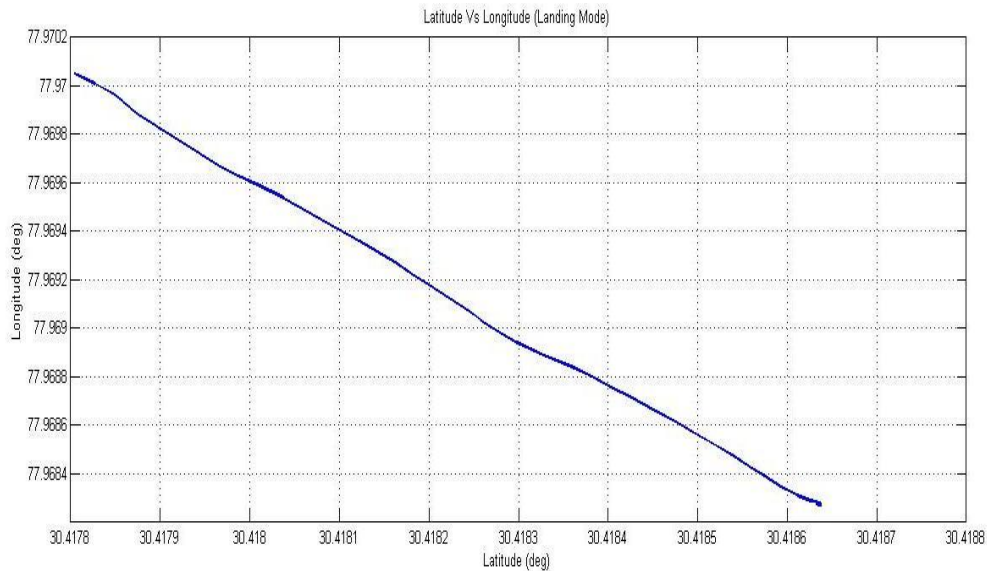


Figure 4.25. Latitude and Longitude variation of PAV during Landing

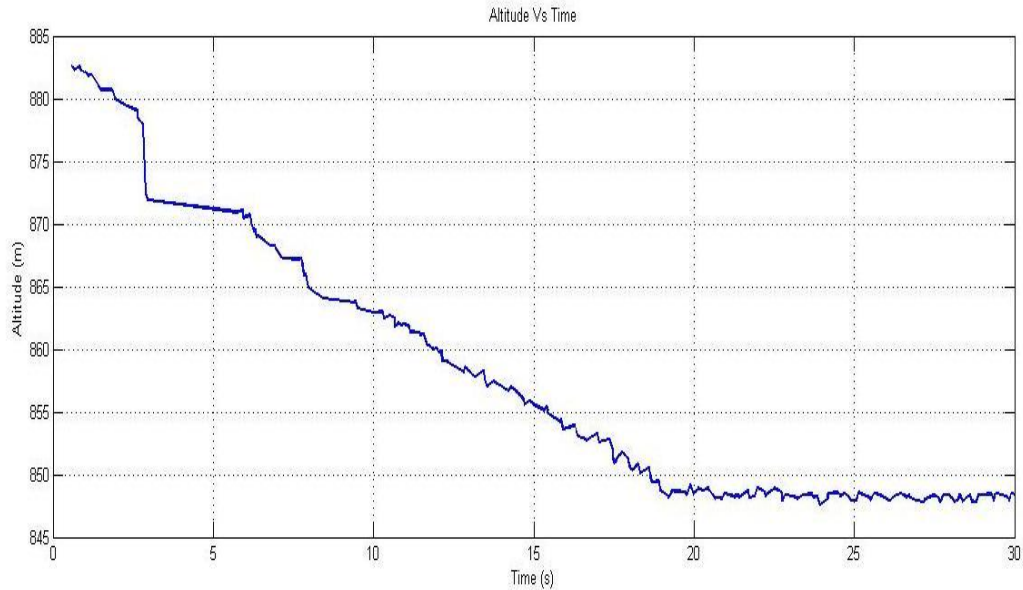


Figure 4.26. Altitude Variation during Landing

PAV loses an altitude of 40 meters in 20 seconds with a minimum thrust provided as seen in figure 4.26.

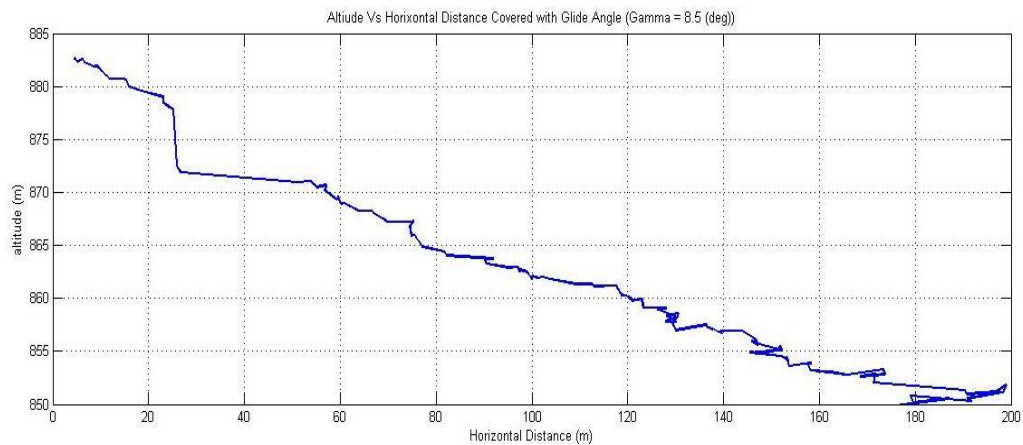


Figure 4.27. Altitude lost to the horizontal distance covered

In figure 4.27 the gamma angle tends to be 8.5 degrees which can be seen by horizontal distance covered to the altitude lost graph

The ground speed value of the vehicle remains to be 10 m/s, as discussed in chapter 3; theoretically the velocity of the vehicle tends to be in 10m/s, as seen figure 4.28.

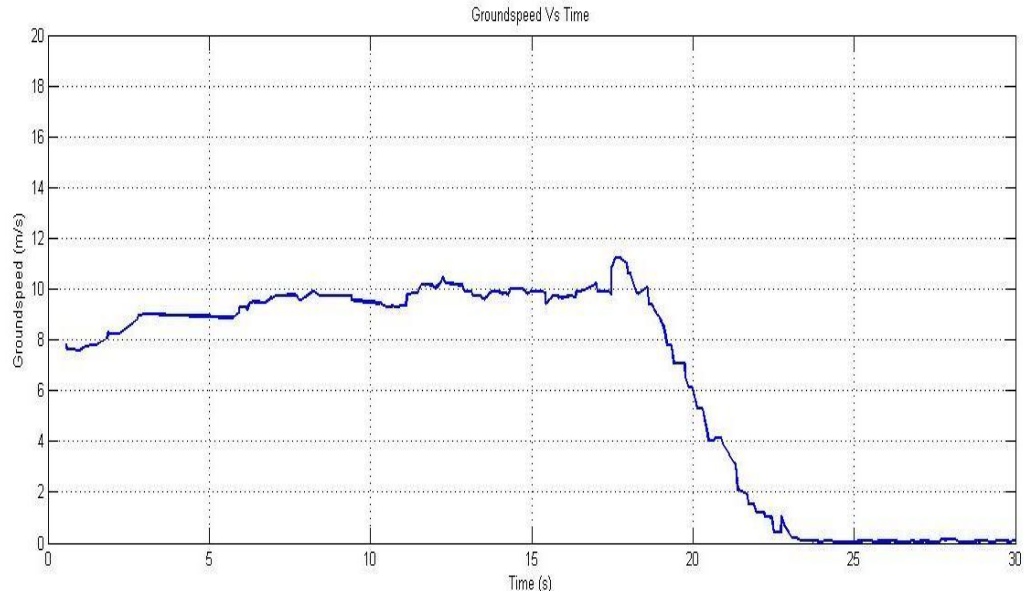


Figure 4.28. PAV Groundspeed during Landing

### 4.13.2 Turn Flight

During the take-off mode the pitch angle observed is about zero degrees. The variation in roll is about zero degrees which is very less.

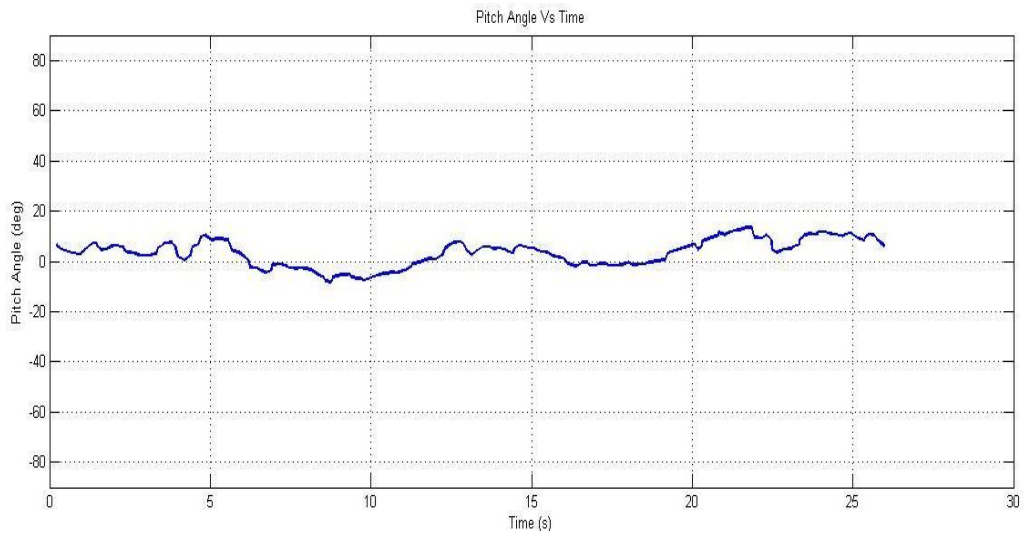


Figure 4.29. Pitch Variation During PAV Turning Flight

These variations are due to vibration of the motors. The pitch angle tends to be around zero indicating that the vehicle tends to maintain level flight. The rate of

pitch also is also maintained about zero. The same can be seen figure 4.29 and 4.30.

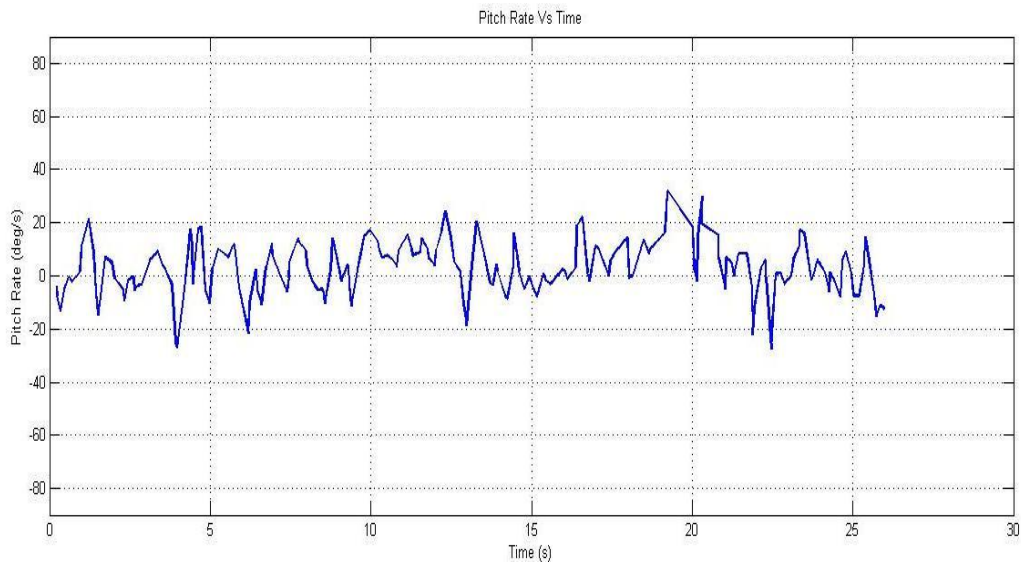


Figure 4.30. Pitch Rate Variation During PAV Turning Flight

The roll variation is about zero degrees which is again negligible. The variations are due to the vibrations due to the motor attached on the payload. Figure 4.31 and 4.32 replicates the same.

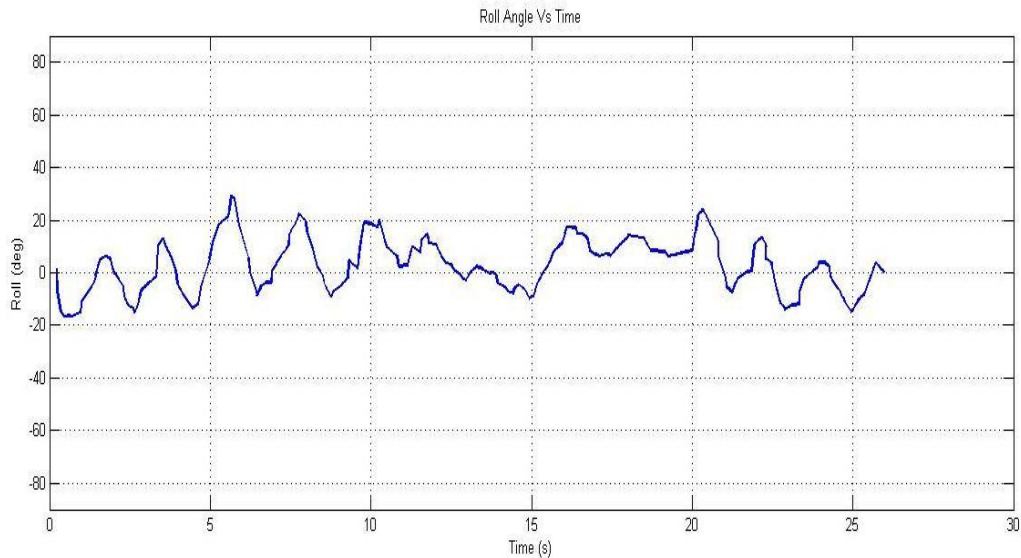


Figure 4.31. Roll Variation During PAV Turning Flight

The roll rate is also about zero degrees due to the static stability of the vehicle. The oscillation are about zero degrees which again very low. It can be observed from figure 4.31 that during the turn (from 14 seconds to 19 seconds) there was a change in roll angle of about 10 degrees due to the turn.

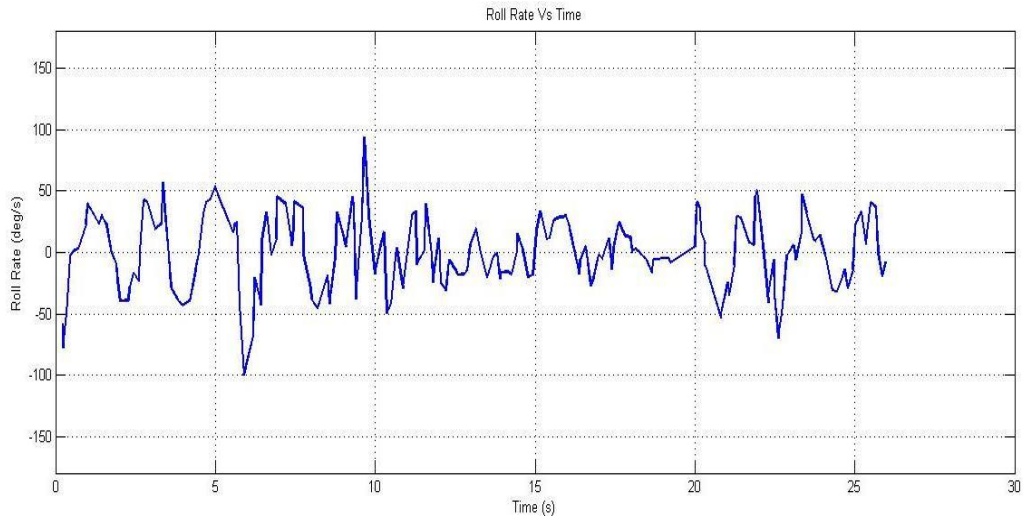
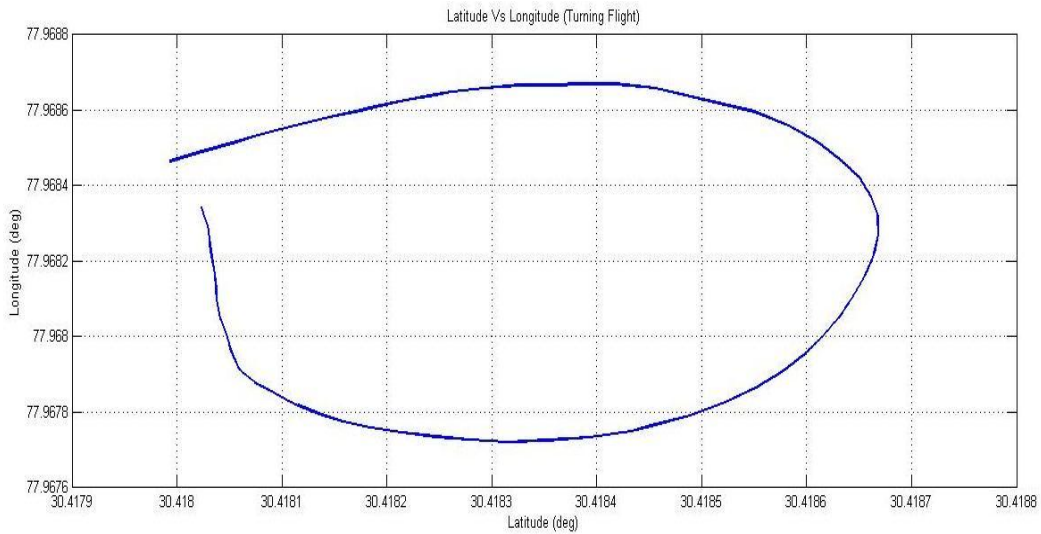


Figure 4.32. Roll Rate Variation During PAV Turning Flight

Figure 4.33 shows the PAV position with respect to latitude, longitude and altitude. There is no altitude change and the vehicle is maintaining a turn rate of 18 deg/s.



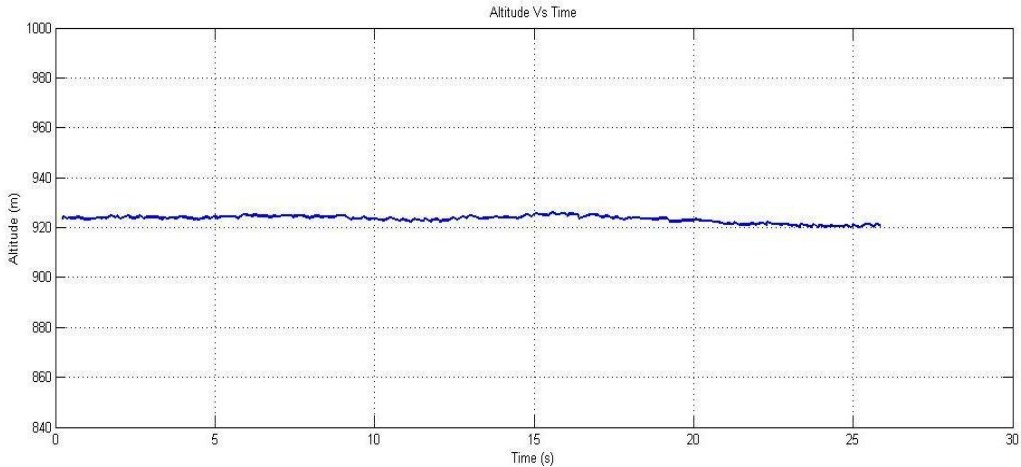


Figure 4.33. Latitude, Longitude and Altitude Variation During PAV Turning Flight

Figure 4.34 shows that the glide angle for the level flight is 0. When seen from altitude lost with respect to the horizontal distance covered. Since the PAV is in level flight as discussed in the open loop simulation result the glide angle is zero.

Analytically, as discussed in chapter 3, the velocity is 10 m/sec using the empirical formula, It can also be seen from figure 4.35 that the PAV maintains a velocity of 10 m/s for level flight and during the turn the velocity goes up to 12 m/s. and the vehicle tends to loose the altitude which is then covered up by increasing the speed to 12 m/s.

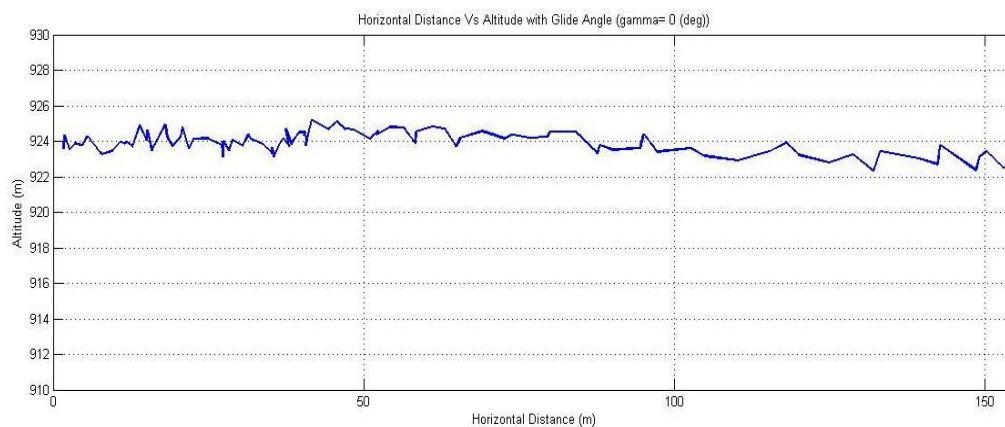


Figure 4.34. Altitude lost to the horizontal distance covered During PAV Turning Flight

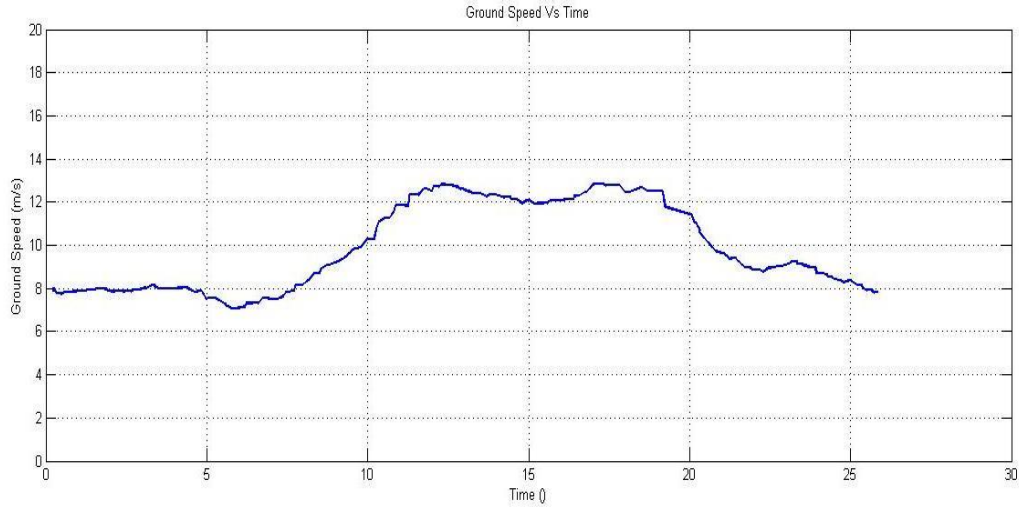


Figure 4.35. Velocity During PAV Turning Flight

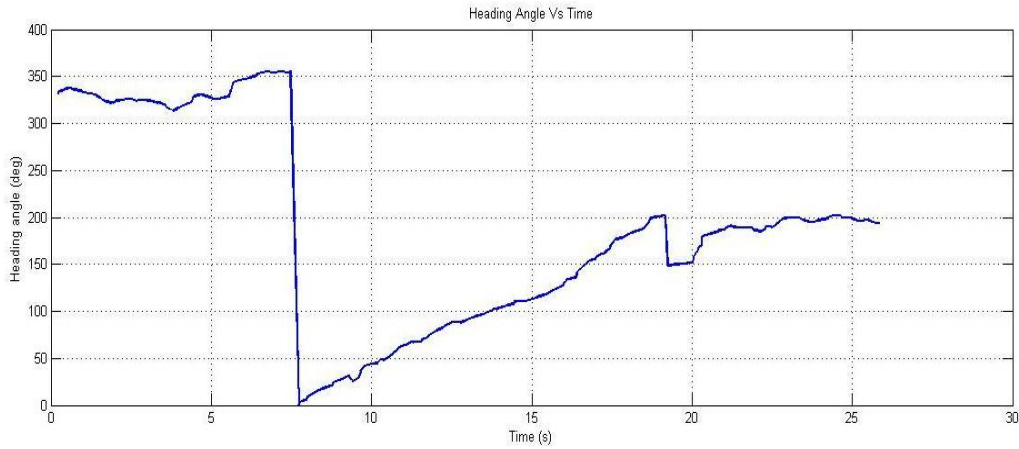


Figure 4.36. Heading Angle During PAV Turning Flight

From the figure 4.36, in the heading angle graph, it can be observed that the PAV is taking turn from 14 seconds to 19 seconds, at the turn rate of 18 deg/s with a bank angle of 10 degrees. It can also be observed that the vehicle took a smooth turn in figure 4.36. All the observations in this section are done on Payload. A lot of oscillations/ vibrations are seen in the graphs as the sensors are placed on the Payload. The vibrations on the Parafoil would be comparatively lesser. Pitch angle, Glide Angle, heading angle, latitude, longitude, altitude and ground speed



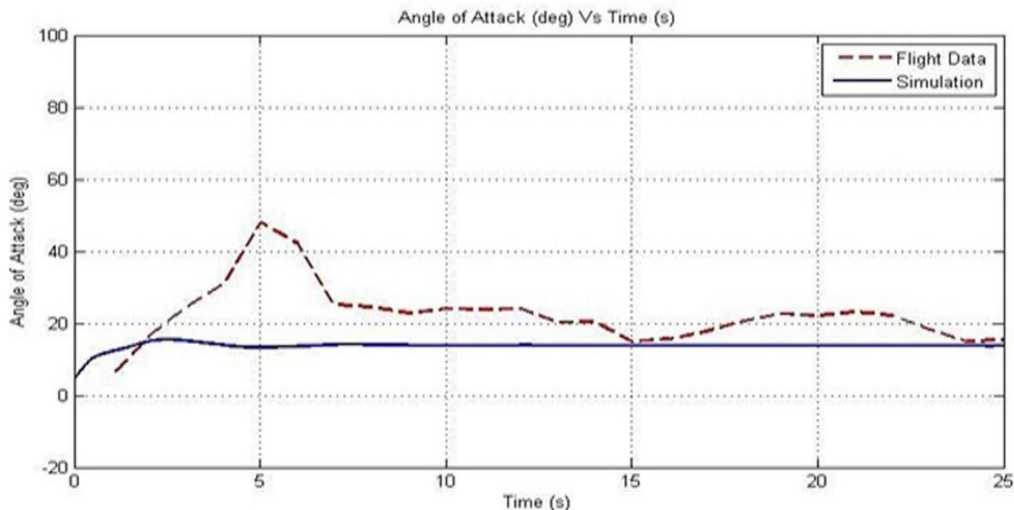
give the performance analysis of the complete system. The above mentioned graphs would help us in understanding the Parafoil performance.

#### 4.14 COMPARISON OF SIMULATED VS FLIGHT RESULTS

The results are classified in two categories. The first part of the results shows the validation of the developed simulation results with Lingard and Flight test results during the unpowered glide condition and the second part shows the direction control using a single servo, which will help us in understanding the servo tilt and turn condition of the Parafoil.

##### 4.14.2 Pitch angle, Glide angle and Angle of Attack Results during Unpowered Glide Condition

The developed Powered Parafoil Aerial vehicle model has been validated using the Lingard model. Angle of attack ( $\alpha$ ), pitch angle ( $\theta$ ) and glide angle ( $\gamma$ ) values obtained are compared with the Lingard values under no thrust conditions. The model is validated using the Lingard results by checking the values of angle of attack ( $\alpha$ ), pitch angle ( $\theta$ ) and glide angle ( $\gamma$ ) of the Parafoil with respect to time.



Figur.4.37. Angle of Attack Simulated Vs Flight Test

|                      | Lingard | Simulated Parafoil Arial vehicle no thrust condition |
|----------------------|---------|--|
| <b>Alpha_p (deg)</b> | 3       | 5  |
| <b>Theta_p (deg)</b> | -9      | -10  |
| <b>Gamma(deg)</b>    | -18     | -18  |

Table 4.7. Powered Parafoil Model validation with Lingard's Model

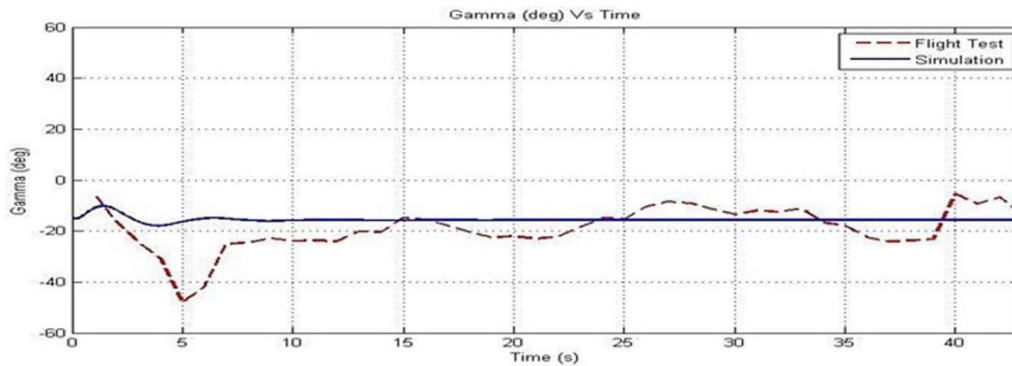


Figure.4.38. Glide Angle Simulated Vs Flight Test

Keeping the zero thrust value under unpowered condition, the simulated and flight test values of angle of attack (alpha), pitch angle (theta) and glide angle (gamma) of the Parafoil are plotted with respect to time. The same can be observed in figures 4.37 through 4.39. It can be observed from figure 4.38 that the glide angle gamma replicates the Parafoil condition. The actual and flight test data approximately match the same.

|                      | Simulated Results of Parafoil Arial vehicle with zero thrust condition | Flight Test results of Parafoil aerial vehicle under zero thrust |
|----------------------|--|--|
| <b>Alpha_p (deg)</b> | 12   | 13   |
| <b>Theta_p (deg)</b> | -5   | -5   |
| <b>Gamma(deg)</b>    | -18  | -17  |

Table 4.8. Simulated Powered Parafoil Model Comparison with Flight Test data

In the figure 4.39, during the simulation, there tends to be oscillations for a time period of 5 seconds as the system is the dynamic system. The same pattern is observed in flight test but there are internal oscillations due to the pendulum effect of the payload. The same can be treated as phugoid dynamics as in aircraft.

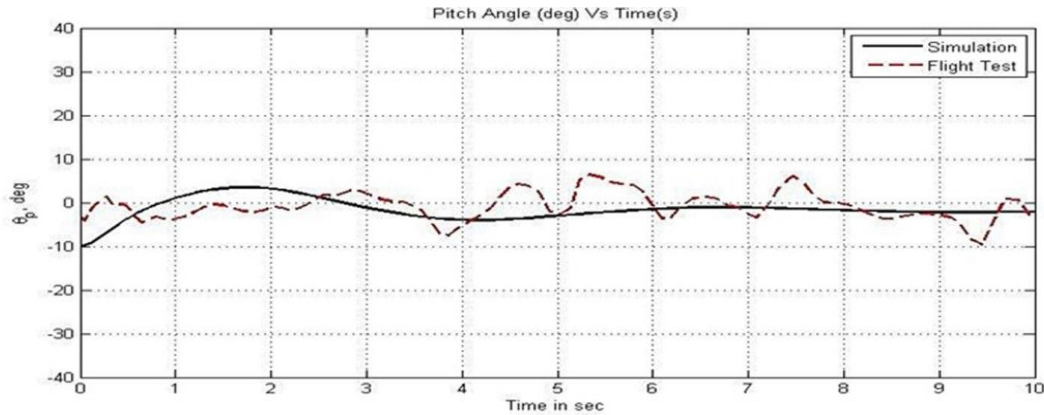


Figure.4.39. Pitch Angle Simulated Vs Flight Test

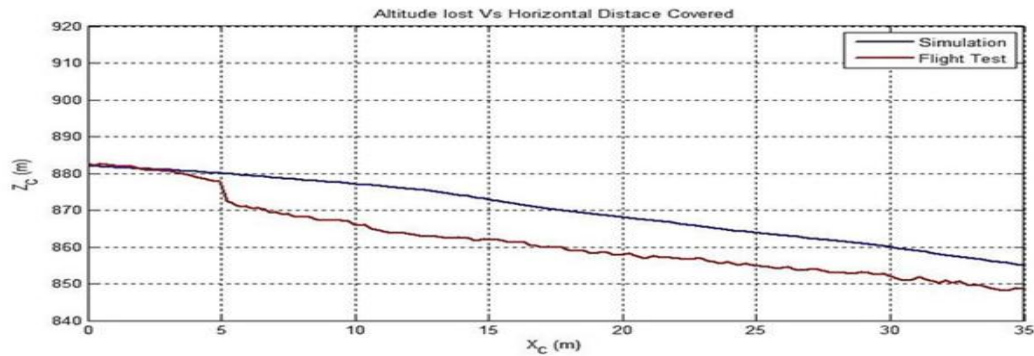


Figure.4.40. Comparison of Altitude lost and Horizontal Distance Covered, Simulated Vs Flight Test

Theoretically the L/D ratio of a ram air Parafoil is 2.5 as discussed in chapter 3. From this Figure 4.38 the ratio of the altitude lost to the distance covered almost remains to be the same in case of the practical and simulation results. As seen in the figure 4.40 there is a sudden drop of height in the flight test result initially after five seconds but it maintains the same glide ratio as that of the simulation in the later stage. The glide rate ( $\gamma$ ) as in the above figure tends to be

following the same manner. The estimated glide rates are used to estimate the lift and drag coefficients needed for the dynamic model. The estimated glide angle is 15 degrees. The PAV covered 12mts distance for a loss of altitude of 10mts.

#### 4.14.3 Direction Control Using a Single Servo

Parafoils are made up of flexible membranes. Therefore, pulling down one side would deflect the Parafoil resulting in a turn. In this model the two ends of the Parafoil is attached to a single control called “Fly-Bar” unlike the conventional systems. Deflection of the fly-bar helps the Parafoil to tilt to one side. The two rotations that can be observed in these kinds of vehicles are yaw and pitch.



Figure 4.41. Control Deflection of Fly-Bar

The figure above (4.41) indicates how the fly-bar works and helps in tilting. It is observed that there was a maximum turn with a tilt of 18 degrees to the right for right turn and 18 degrees to the left. Here the flight test is performed at an altitude 890 m providing a constant thrust of 7.75N indicating the level flight. This test is performed to analyze the turn performance due to the servo tilt.

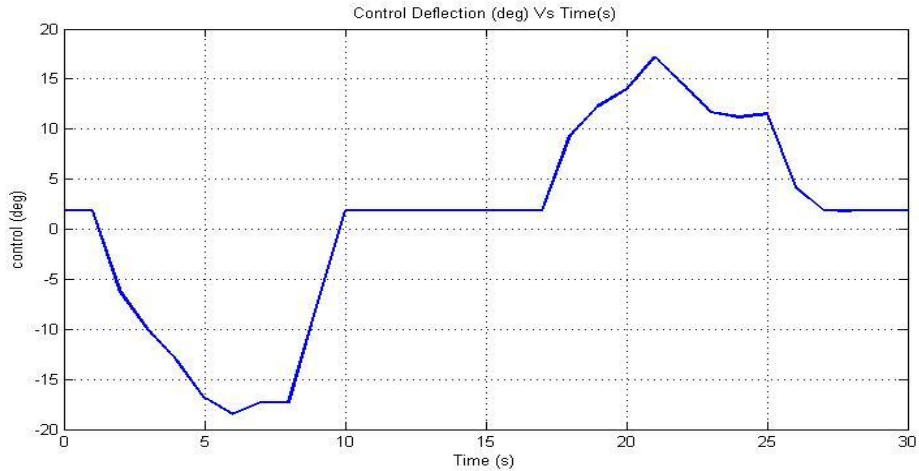


Figure.4.42. Fly- Bar Deflection

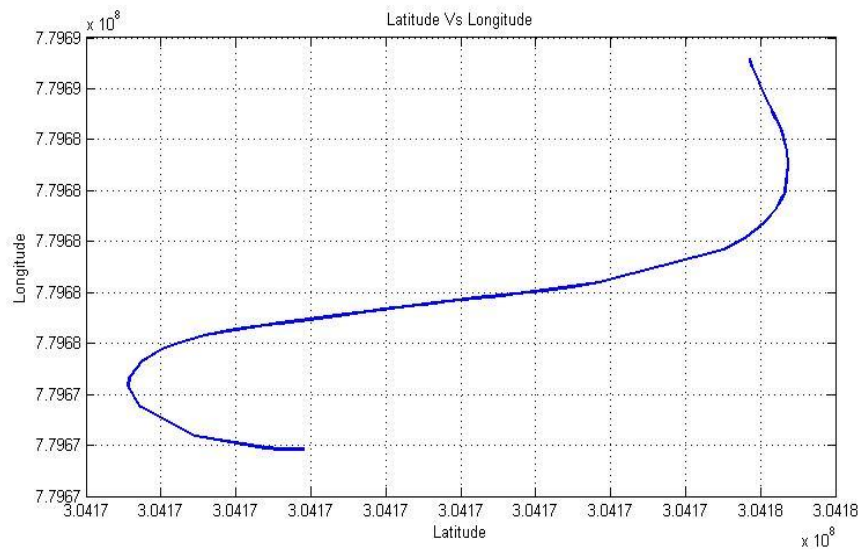


Figure.4.43. Flight Path with the Given Fly-Bar Deflection

Figure 4.42 shows the servo tilt in positive and negative side going maximum upto +/- 18 degrees. Figure 4.43 shows the change in direction indicating an ‘S’ turn. The yaw change is also seen in figure 4.44 oscillating between +/- 15 degrees. The experiment was performed for 30 seconds.

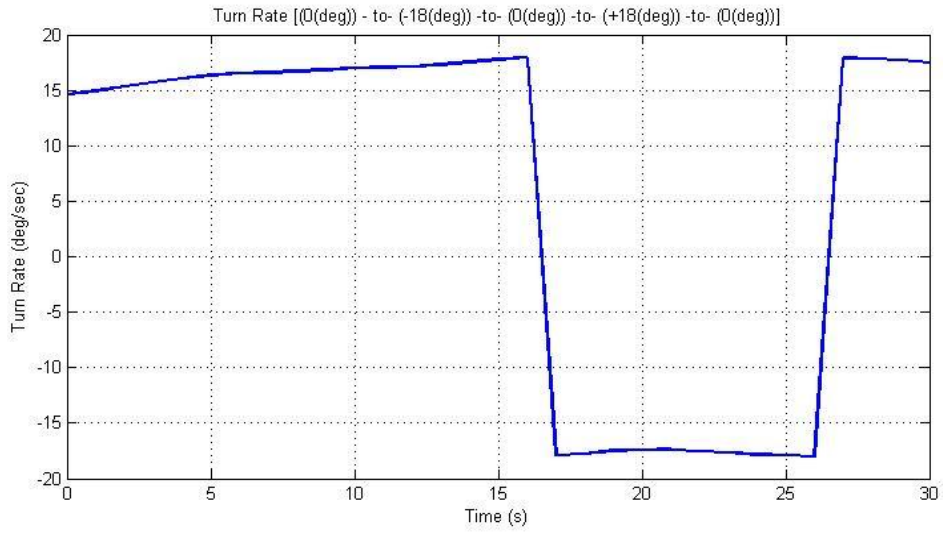


Figure.4.44. Turn Rate with the Given Fly-Bar Deflection

## CHAPTER 5

### CONTROL SYSTEM DESIGN AND ALGORITHM

#### 5.1.GUIDANCE LOGIC

The task of guidance logic is to generate heading and altitude signals that will enable the PAV to follow desired path specified by the sequence of points. For the autonomous flight conducted, the only concern was to maintain the altitude; hence, the guidance logic is only concerned with the heading angle of the vehicle in the horizontal plane. A simple scheme was implemented as depicted in the figure 5, which shows the guidance logic, specified distance to generate heading angle that will direct PAV back to the path between the waypoints.

##### 5.1.1. Lateral Heading controller

The controller has a heading tracking algorithm, which receives the target heading angle from the higher level guidance logic and outputs a control signal to minimize the error between the measured and the target heading [42].

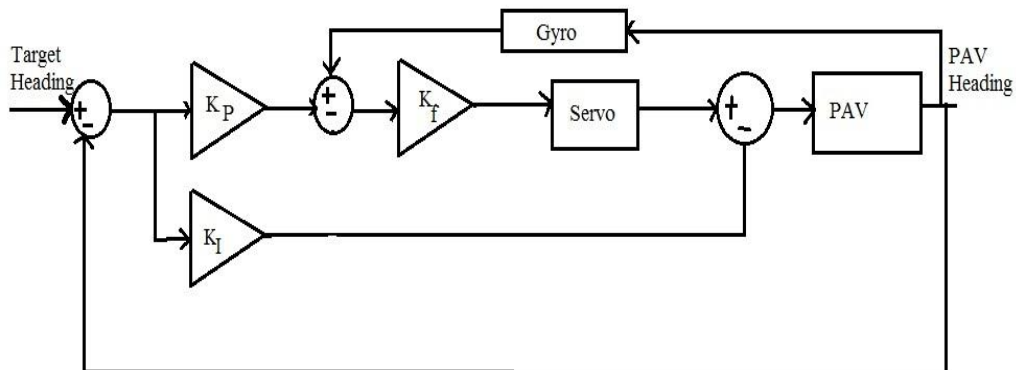


Figure 5.1 Lateral Heading Controller Powered Parafoil Aerial Vehicle

Classical feedback compensation controller was adopted such that the gyroscope output can be used directly. The servo is modeled by simple first order transfer. The servo transfer function is simply

### 5.1.2. Longitudinal Altitude Controller

The controller has an altitude tracking algorithm, which receives the target altitude from the guidance scheme and outputs throttle signal to minimize the error between measured and the target altitude [42]. A classical proportional, integral and derivative (PID) controller was implemented.

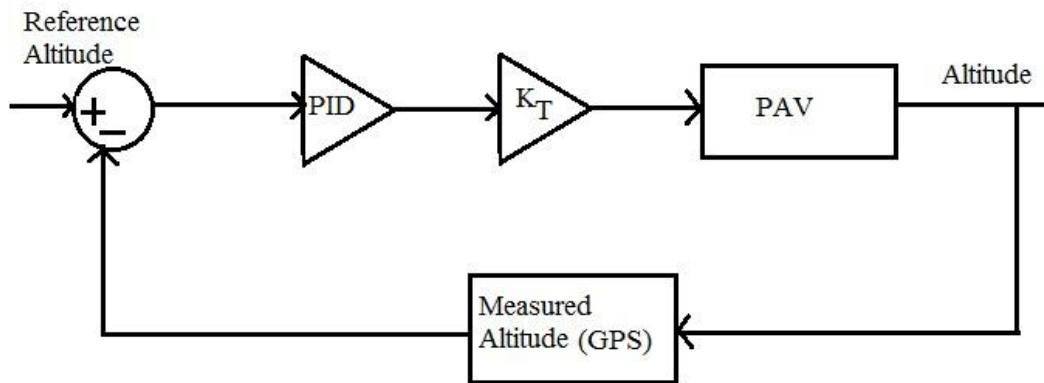


Figure 5.2 Altitude Hold Controller Powered Parafoil Aerial Vehicle

A throttle control regime has been developed. A PID controller has been and is implemented in the cascade configuration scheme. The PID is used to supply the exact signal to be supplied to the motor to eliminate the steady state altitude error. A simple feedback loop has been used to stabilize the PAV. A relationship between thrust and altitude is developed so altitude gained is linearly proportional to the throttle provided. The throttle is allowed to vary from 0 to unity.

### 5.1.3. Attitude

The attitude of the PAV is controlled by a nested PI->PID loop. Tuning the inner PID loop is essential to good stable flight. The outer PI loop is less sensitive and effects mostly the style of flying desired (fast or slow). The inner PID loop looks



at the desired rate of angular rotation and compares that to the raw gyro output. The difference is feed back into the PID controller and sent to the motor to correct the rotation. This is the heart of both Rate mode, Stabilize mode, and all other modes. It is also the most critical gain to adjust for PAV. The outer PI loop generates the desired rate of angular rotation. The input for this loop can either be user with stick movement, or the stabilizer, which tries to achieve a specific angle.

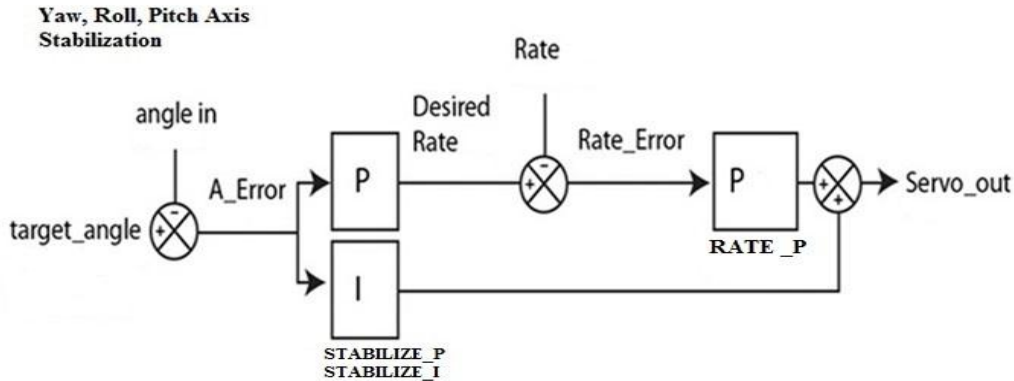


Figure. 5.3. Roll, Pitch and Yaw Axis Stabilizer for Powered Parafoil Aerial Vehicle

- STABILITY\_P is 1.3 or 1.3° per second rotation for every 1° of error. If you want more or less speed of rotation based on user input, adjust this value.
- STABILITY\_I is 0.1, used to overcome imbalance in the PAV. If the PAV is not symmetrical this term will bring the PAV to level. The higher the number the faster the PAV will compensate. Low numbers can have adverse effects by causing a very slow oscillation measured in seconds.
- RATE\_P is the proportional response and the default is 0.2. The PAV will vary quite a bit depending on the weight and thrust of the motor.

#### 5.1.4. PI control for Loiter and Navigation

Loiter and navigation uses the same PID rate controllers. The location error is calculated in centimeters for X (Longitude) and Y (Latitude) which is fed to the controller. The first stage of the controller takes the XY position error and decides how fast the PAV should go to reach the correct location.

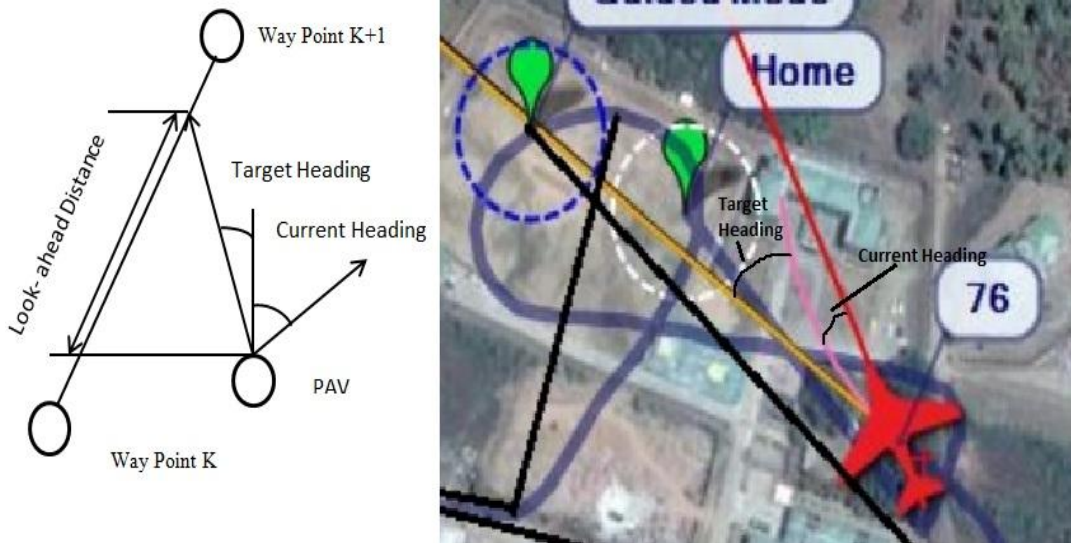


Figure.5.4. Loiter and Navigation Control for Powered Parafoil Aerial Vehicle

Now that we have a desired rate, we need to change the copter pitch and roll to give us that rate of travel.

- Parameter: LOITER\_LAT\_P and LOITER\_LON\_P are the proportional response and the default is 2.2. PAV will vary quite a bit depending on the weight and thrust of the engines.

### 5.1.5. PI Control for altitude hold

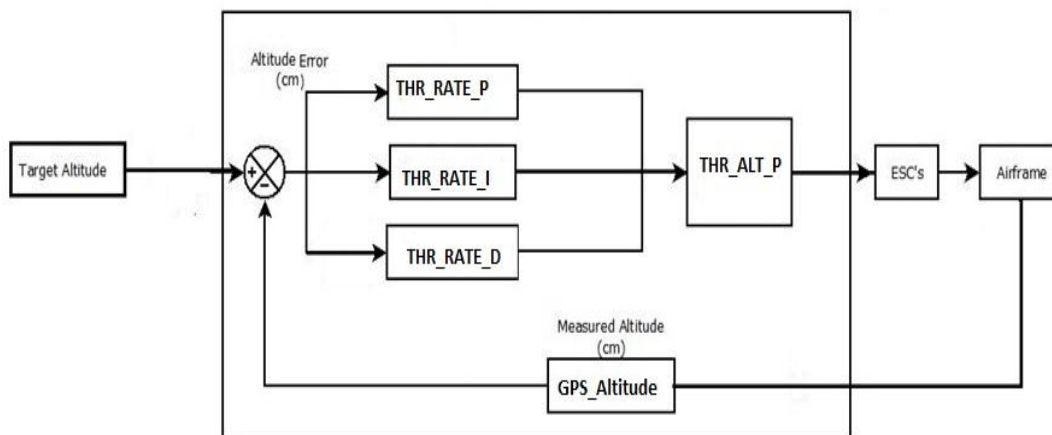


Figure.5.5. Altitude Hold Control for Powered Parafoil Aerial Vehicle

The altitude error is calculated in centimeters and fed to the controller. The first stage of the controller takes the altitude error and decides how fast the PAV should go to reach the correct altitude.

- Parameter: THR\_ALT\_P is 4 or 4 m/s for a 1m error. The desired rate maxes out at 1m/s.
- Parameter: THR\_ALT\_I is used to close the gap between the actual hover throttle and current assumed hover throttle.

**PID Rate Control for altitude hold**

Now that we have a desired rate, we need to change the thrust to give us that rate.

- Parameter: THR\_RATE\_P is the proportional response and the default is .35. PAV will vary quite a bit depending on the weight and thrust of the motors. The value should be lowered in order to minimize the oscillations
- Parameter: THR\_RATE\_I is set to 0 by default.
- Parameter: THR\_RATE\_D is 0.02 by default, but the noise of the Baro sensor can cause issues. If the value is too high bad oscillations are seen.

There was similar study done for similar Parafoil Vehicle by Jack Umenberger et al. [42], the gain values for various two different controls have been compared. Table 5.1. shows the theoretical and flight test gain of the PAV

| #                     | Theoretical [42]  |                |                | Practical Flight Test |                |                |
|-----------------------|-------------------|----------------|----------------|-----------------------|----------------|----------------|
| Gain                  | K <sub>P</sub>    | K <sub>I</sub> | K <sub>D</sub> | K <sub>P</sub>        | K <sub>I</sub> | K <sub>D</sub> |
| Attitude              | -                 | -              | -              | 1.3                   | 0              | 0.0025         |
| Later Heading Control | 1.8               | 0              | 0              | 2.2                   | 0              | 0              |
| Altitude hold         | 0.17              | 0.02           | 0.01           | 0.35                  | 0              | 0.02           |
|                       | 4.5<br>(Throttle) | -              | -              | 4<br>(Throttle)       | -              | -              |

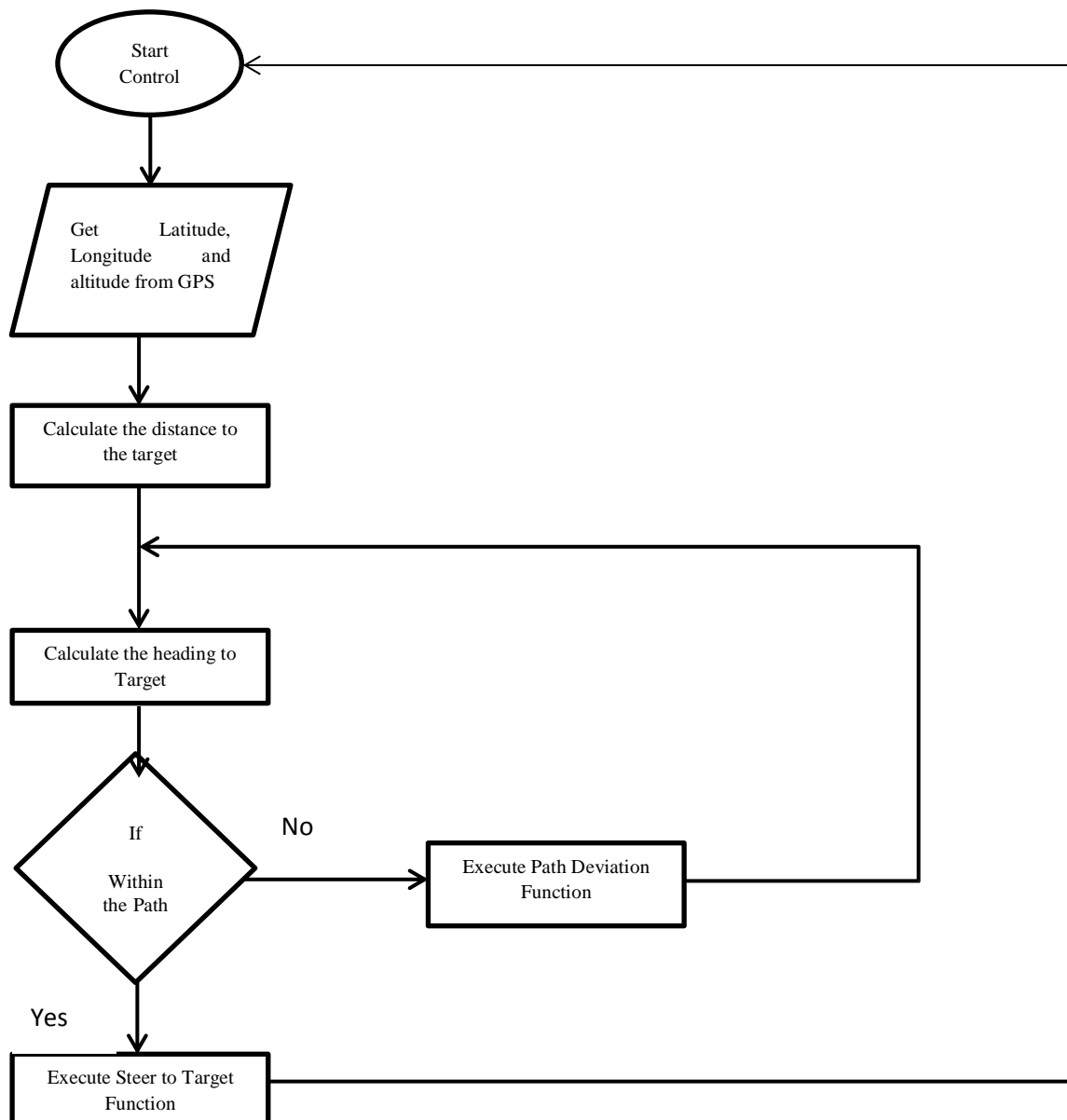
Table 5.1. Gain Values for Theoretical and Practical

## **5.2.ALGORITHM DESIGN FOR GUIDANCE LAW**

The algorithm general takes in the sensors value and a defined path is followed using the sensors data. The algorithm starts with starting data logging of all the sensor information. The received sensor information a path is defined for the aerial vehicle. For achieving the defined path the servo motors are controlled automatically to change the direction and BLDC motor is controlled for holding the vehicle at desired altitude. The guidance logic is developed using way point navigation technique, where the controller gets the latitude, longitude and the altitude values from the GPS. The controller then calculates the heading angle and distance to the next waypoint. If the calculated distance and the angle, determines that the vehicle is within the path, then the controller executes steer to target algorithm. If the vehicle is deviated from the path due to wind or any other problem then the controller executes path deviation algorithm.

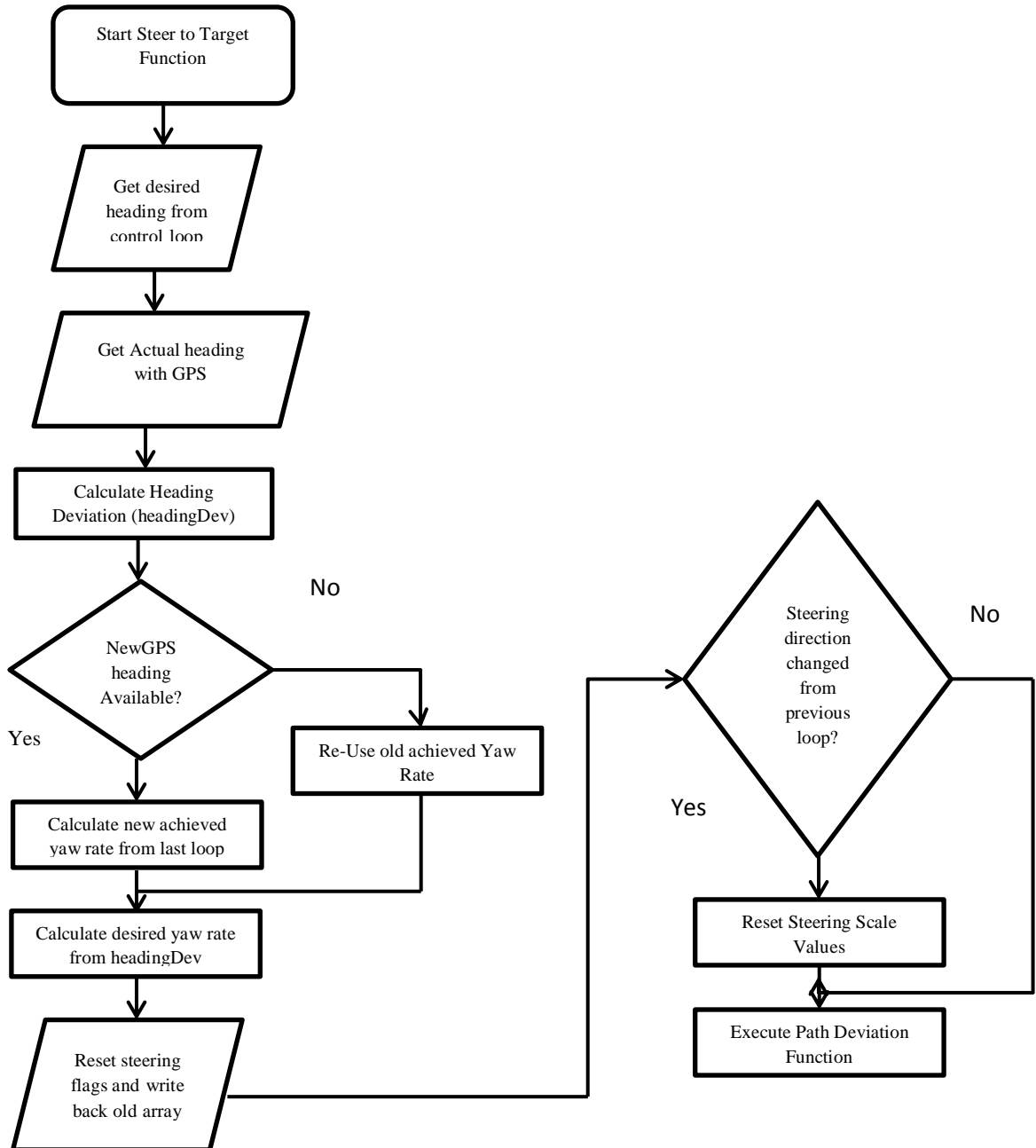
### 5.2.1. Main Control Loop

The guidance logic is developed using way point navigation technique, where the controller gets the latitude, longitude and the altitude values from the GPS. The controller then calculates the heading angle and distance to the next waypoint. If the calculated distance and the angle, determines that the vehicle is within the path, then the controller executes steer to target algorithm. If the vehicle is deviated from the path due to wind or any other problem then the controller executes path deviation algorithm.



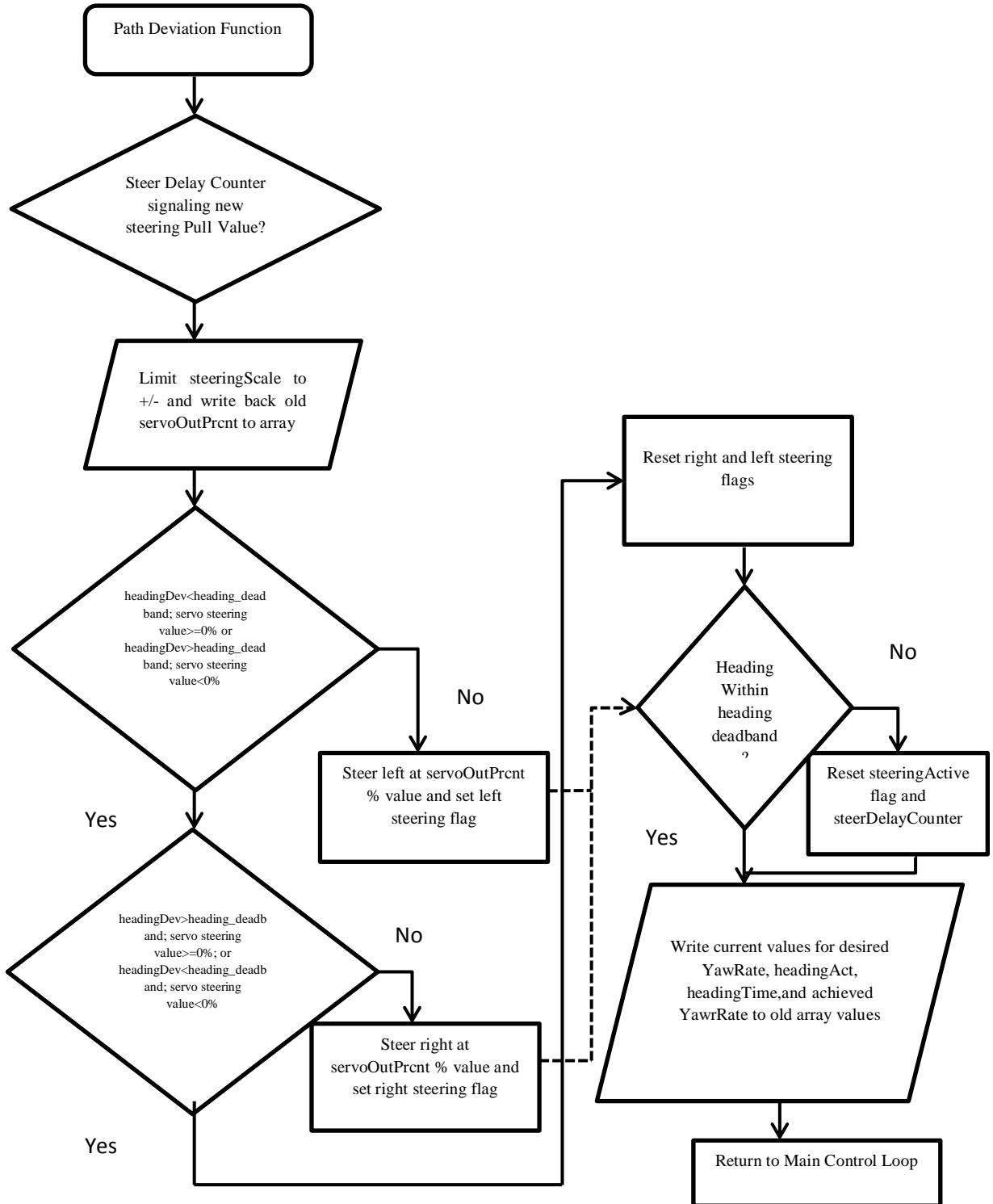
### 5.2.2. Steer to Target Algorithm

During this algorithm the vehicle gets the actual heading from the control loop and the current heading from the GPS and then calculates the deviation error. The deviation error along with the gain is given to the servo with the calculated yaw rate

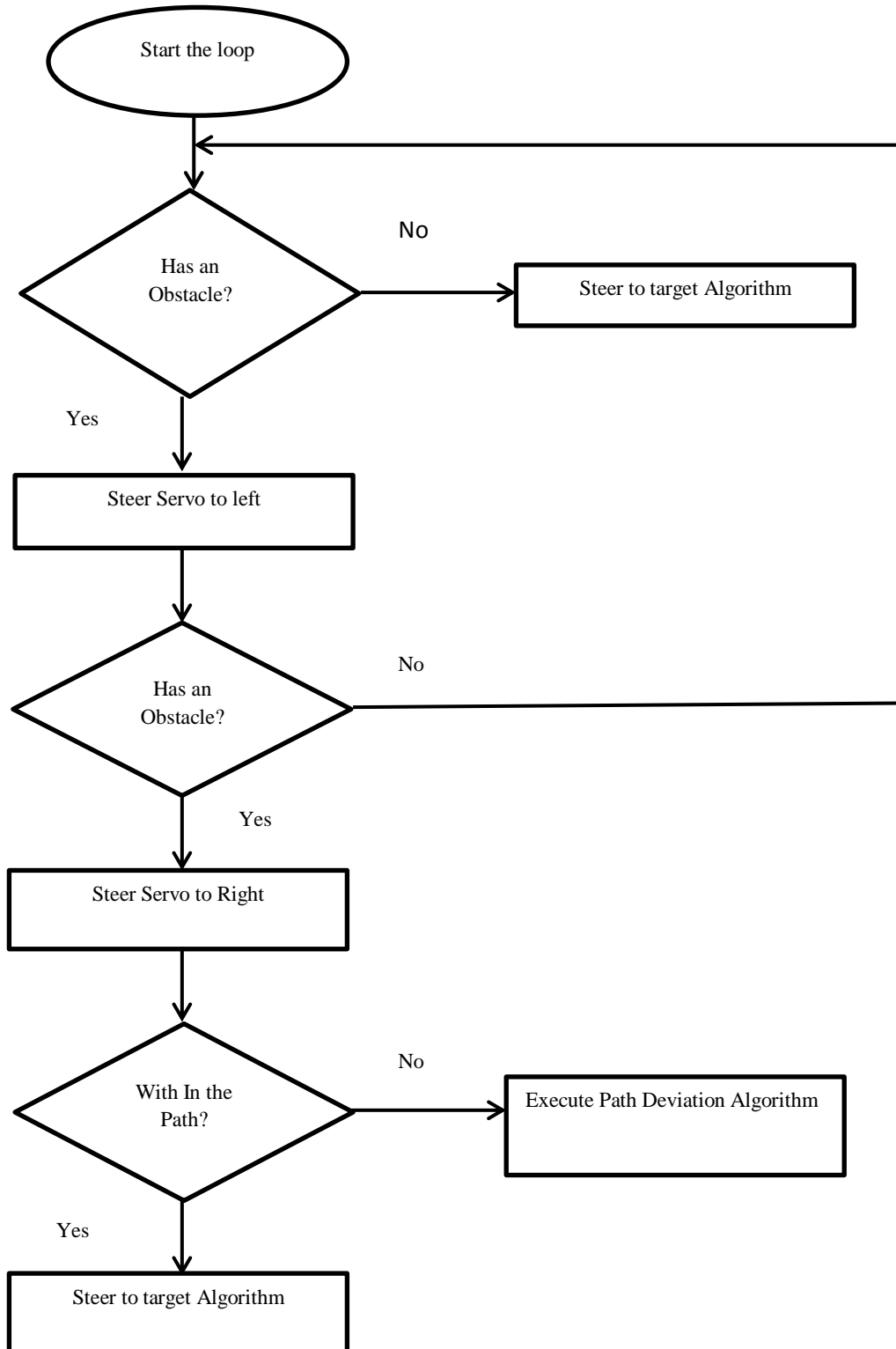


### 5.2.3. Path Restoration Algorithm

In this algorithm the controller compares the heading deviation angle with the desired deviation angle, two conditions occur in the case:



### 5.2.4. Obstacle Avoidance Algorithm





### 5.3.CLOSED LOOP RESULTS

The control system described in chapter 5 was implemented in the PAV. The PAV was launched under manual control and after reaching an altitude of 100 meters the control was made autonomous and attitude stability was performed.

#### 5.3.1. PID Tuning for Attitude Stability

In figures 5.6 through 5.9 it is observed that initial gain value was considered to be 2.4, and was reduced in steps to 2 and then 1.3. The gain value was set to 1.3 using visual inspection. By visual inspection we could conclude that the roll oscillations were damped down to almost zero. But certainly, there were internal oscillations due to the motor vibrations. Altogether the major oscillations were damped down keeping the proportional gain value to be 1.3.

The Proportional gain effect on roll rate can be clearly observed in figure 5.6. It can be seen that with proportional gain 2.4, the oscillations were there for 5 seconds. With the implementation of gain value to 1.3 the oscillation were reduced down to 3 seconds. Since the Parafoil Aerial Vehicle has a pendulum effect, the attitude is much effected due to the roll moment, whereas, yaw moment and pitch moment has less oscillations. Similar damping of oscillations can be seen in figure 5.7 in Roll angle.

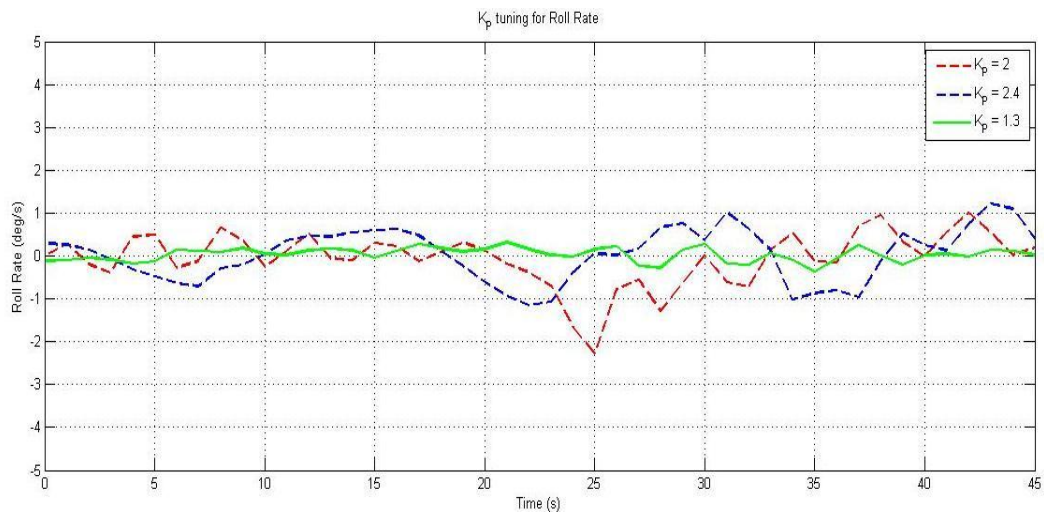


Figure. 5.6. P Tuning Roll Rate

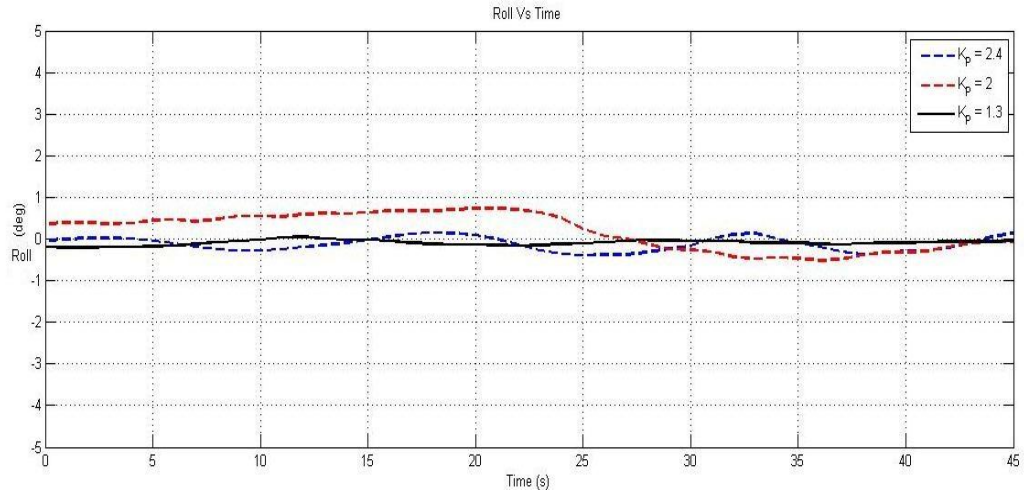


Figure. 5.7. P Tuning Roll Angle

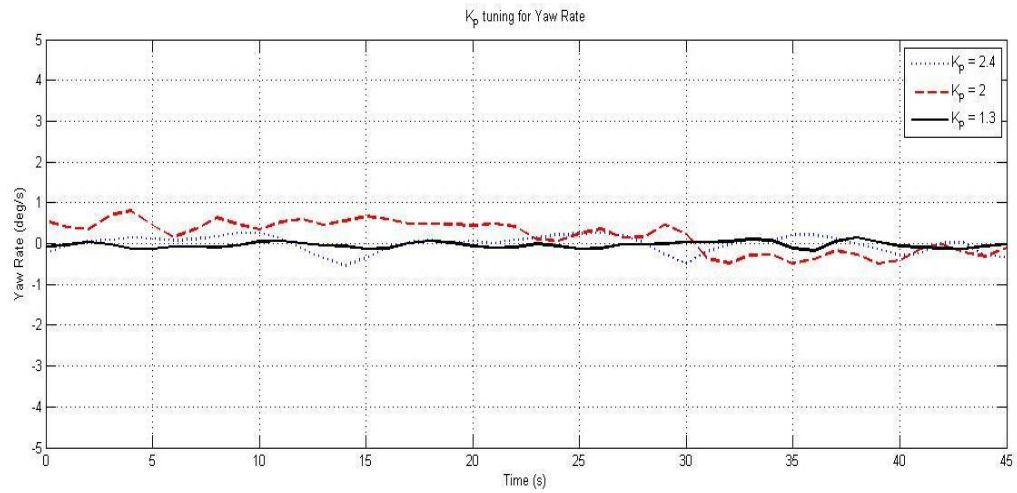


Figure. 5.8. P Tuning Yaw Rate

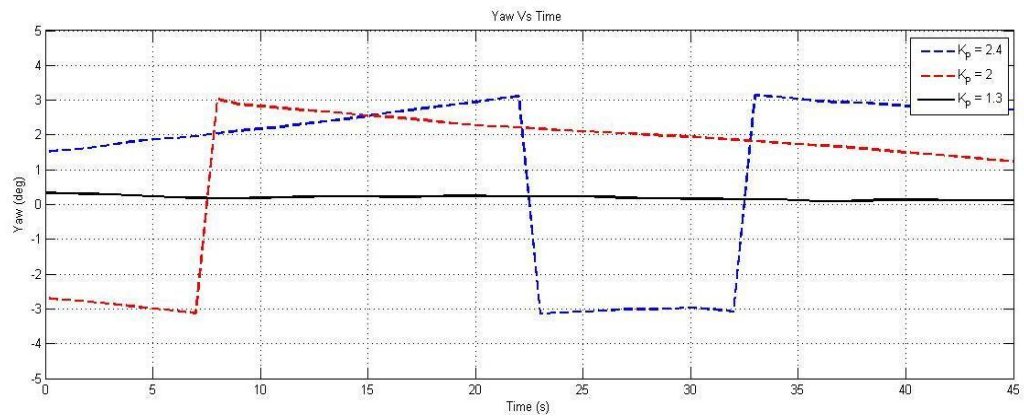


Figure. 5.9. P Tuning Yaw Angle

Proportional gain effect on yaw rate can be seen in figure 5.8. With gain value of 1.3 the oscillations were completely damped down. As stated earlier Yaw moment has very less effect on attitude stability due to pendulum stability, which was discussed in detail in chapter 1. Similar damping effect can be seen in Yaw angle in figure 5.9.

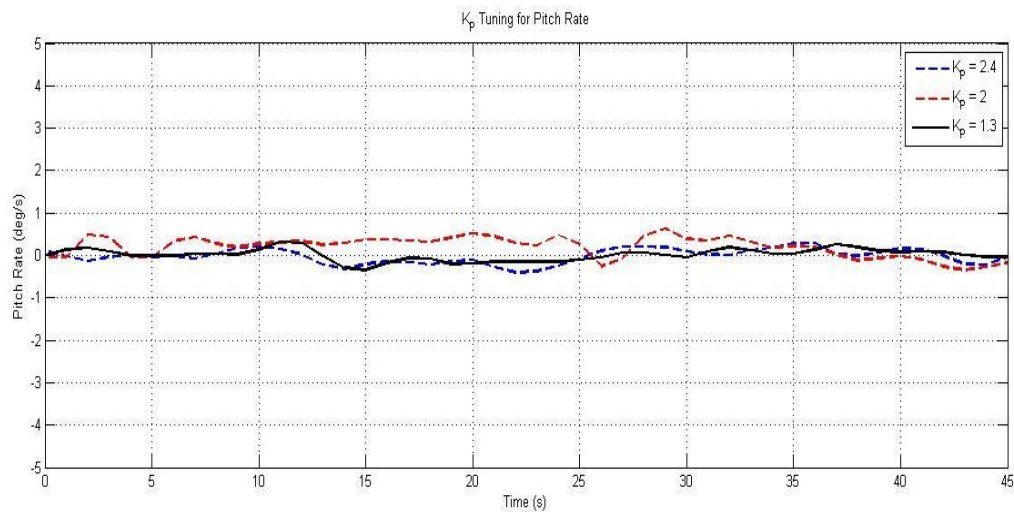


Figure. 5.10. P Tuning Pitch Rate

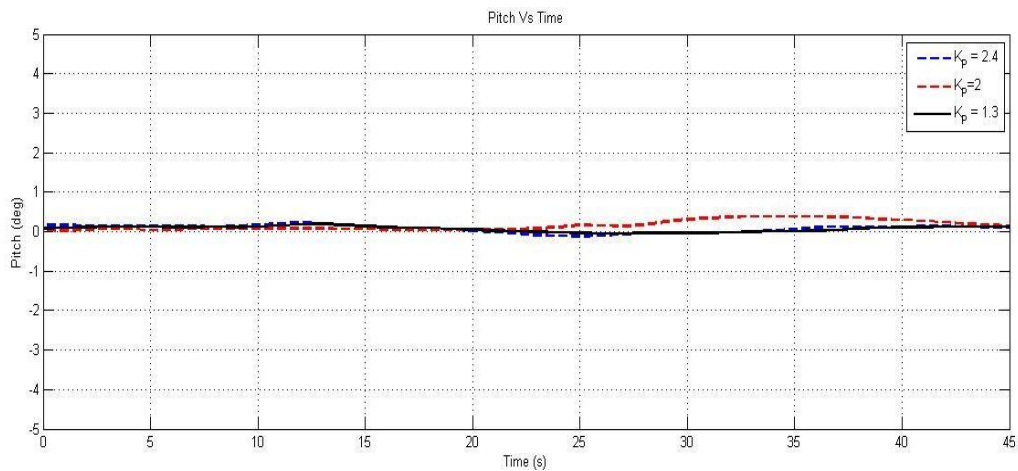


Figure. 5.11. P Tuning Pitch Angle

The effect of proportional tuning on pitch rate can be observed in figure 5.10. The oscillations were damped down to zero having a frequency of less than 1 second. Pitch angle also show similar changed due to the tuning can be seen in figure

5.11. In figure 5.12 it can be observed the effect of proportional gain 1.3 on roll pitch and yaw rates. As discussed due to the pendulum stability the oscillations can be much seen in roll moment. Total effect of tuning gain of 1.3 can be seen in figure 5.13 in angles.

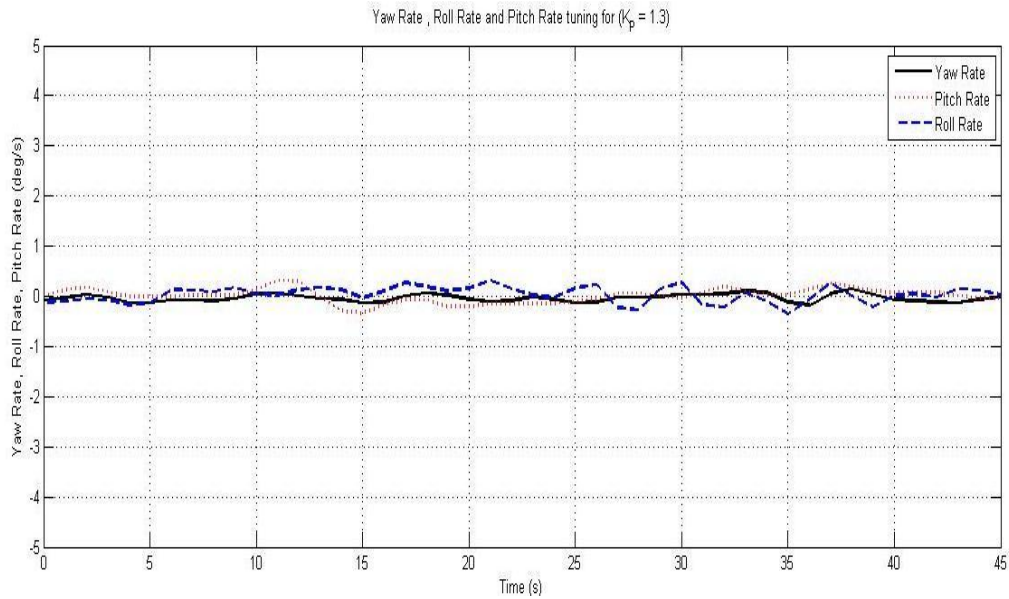


Figure. 5.12. P Tuning Roll Rate, Pitch Rate, Yaw Rate

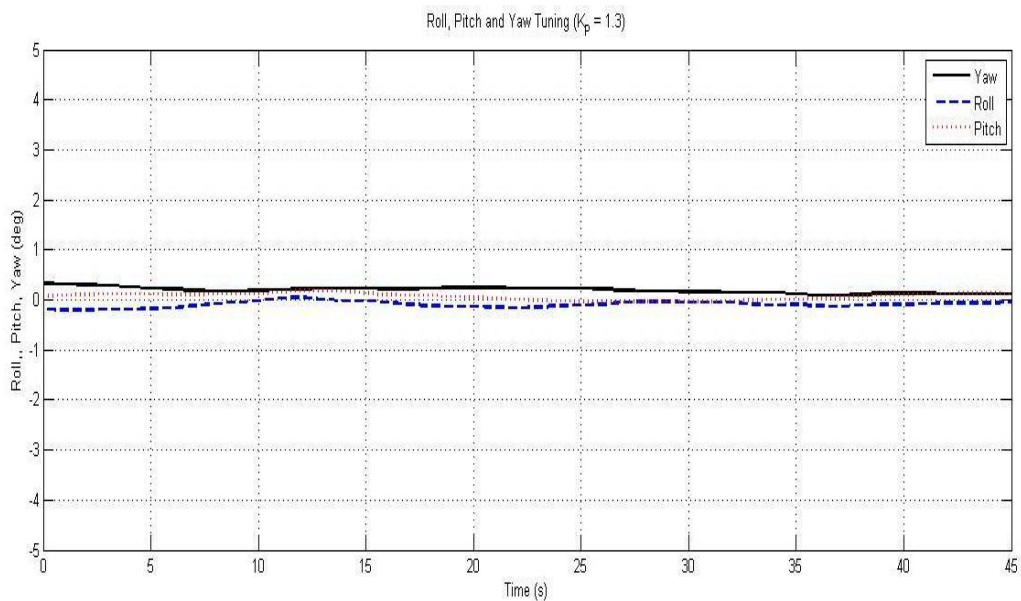


Figure. 5.13. P Tuning Roll, Pitch, Yaw

### 5.3.2. Closed loop Lateral Heading Controller with P = 2.2

In the above section we have achieved attitude stability and the oscillations were damped down. After the attitude stability, later heading controller was designed for way point navigation and loiter operations according to the steer to target algorithm. According to the algorithm the heading difference angle was supposed to get down to zero degrees, when travelling from one way point to another, keeping the servo value positive or negation according to the way point, indicating a turn. It was observed in the open loop flight test and simulation results that there were not many oscillations in the turning situation. Therefore only a proportional controller was used keeping the gain value to 2.2 to achieve a smooth turn. The same effect can be seen in figure 5.14 to 5.15.

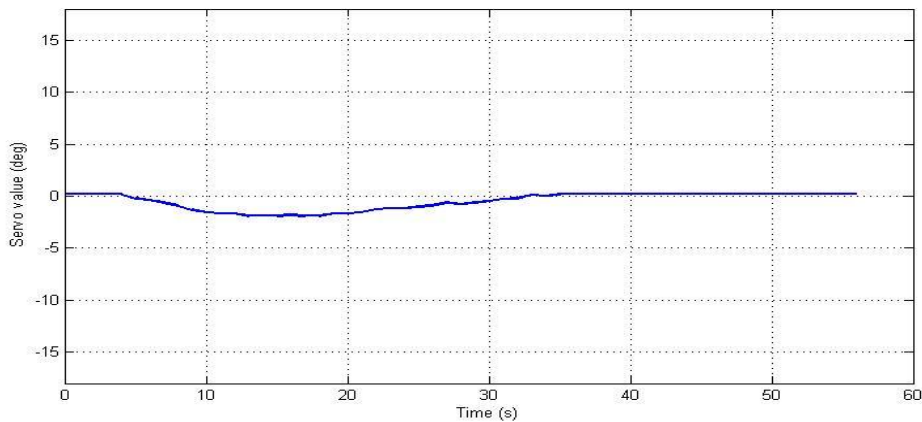


Figure.5.14. Servo Tilt for Heading Control

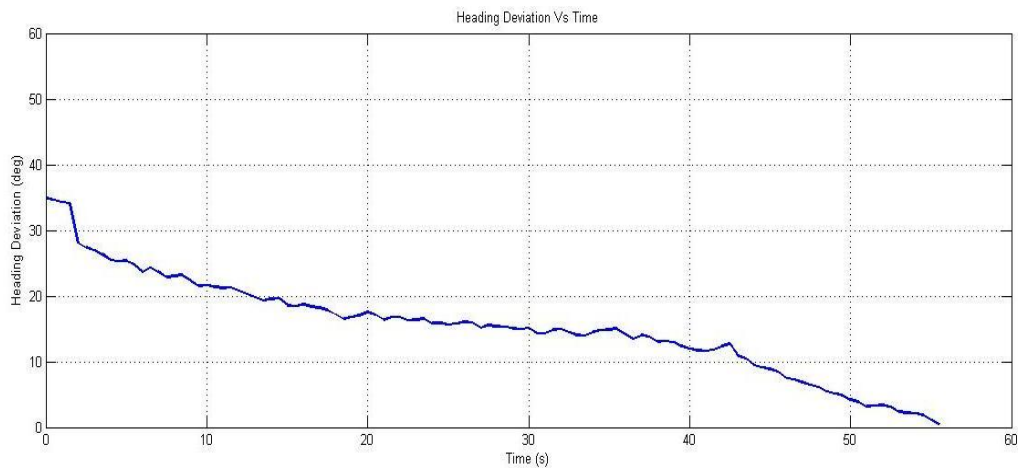


Figure.5.15. Heading Control angle tending to zero

### 5.3.3. Closed loop Longitudinal Altitude Hold Controller With P (Throttle) = 4 and P = 0.35

Once the heading control was achieved, an altitude hold controller was designed to maintain a certain altitude to complete the waypoint navigation task. The P (Throttle) is used to provide the exact signal to be supplied to the motor to eliminate the steady state altitude error which is kept as 4 to achieve throttle control regime. It can be seen from figure 5.16 that the throttle was maintained at 7.5 N to achieve the altitude of 920 m in order to execute proper way point navigation.

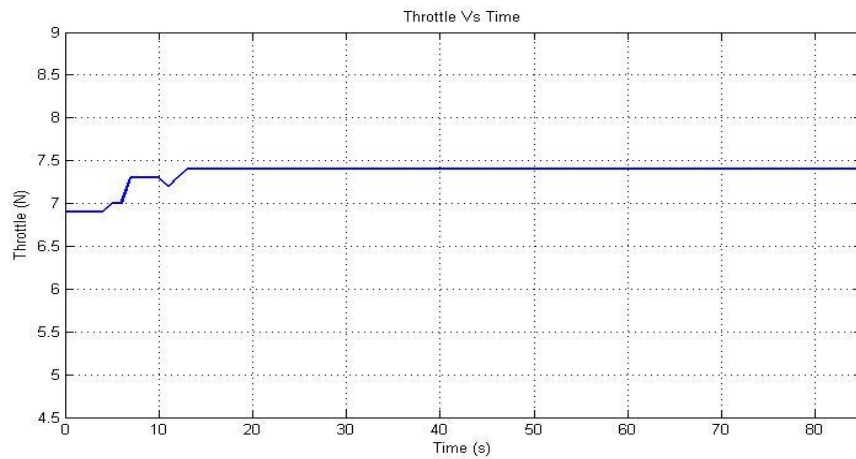


Figure.5.16. Altitude hold with throttle control at 7.5 N

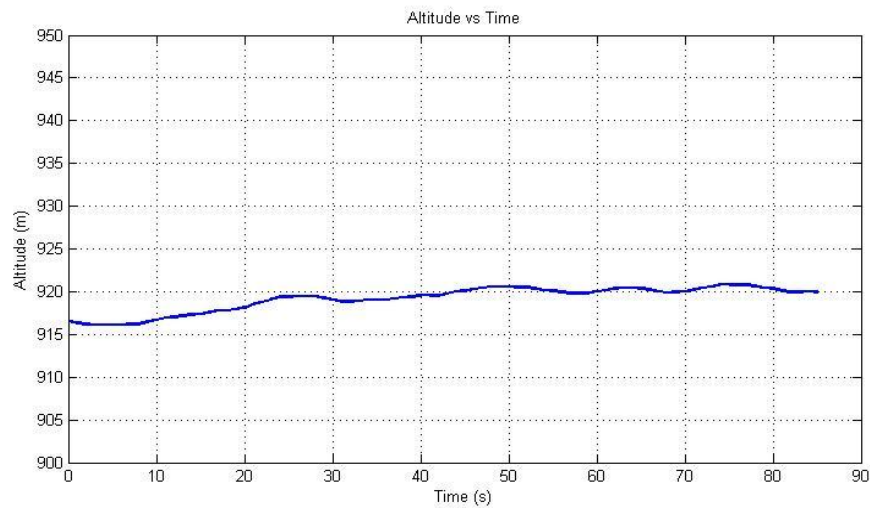


Figure 5.17. Altitude hold at 920 meters

In figure 5.13 it can be seen that due to the throttle hold at 7.5 N, an altitude of approximately 920 m was maintained so that the vehicle can travel to the other way point easily. As discussed in attitude stability a lot of oscillations were observed in take-off mode than in turning flight test. Therefore a PID was implemented keeping the proportional, Integral and derivative coefficients to be 0.35, 0 and 0.02.

A path comprised of four way points was selected to demonstrate the performance of the guidance logic. Each way point have effective radius of 5m. These way points along with the path have been shown in the figure 5.14 and 5.15. Finally, the path shows that the heading angle tracker along with guidance logic provides a reliable means of way point navigation.

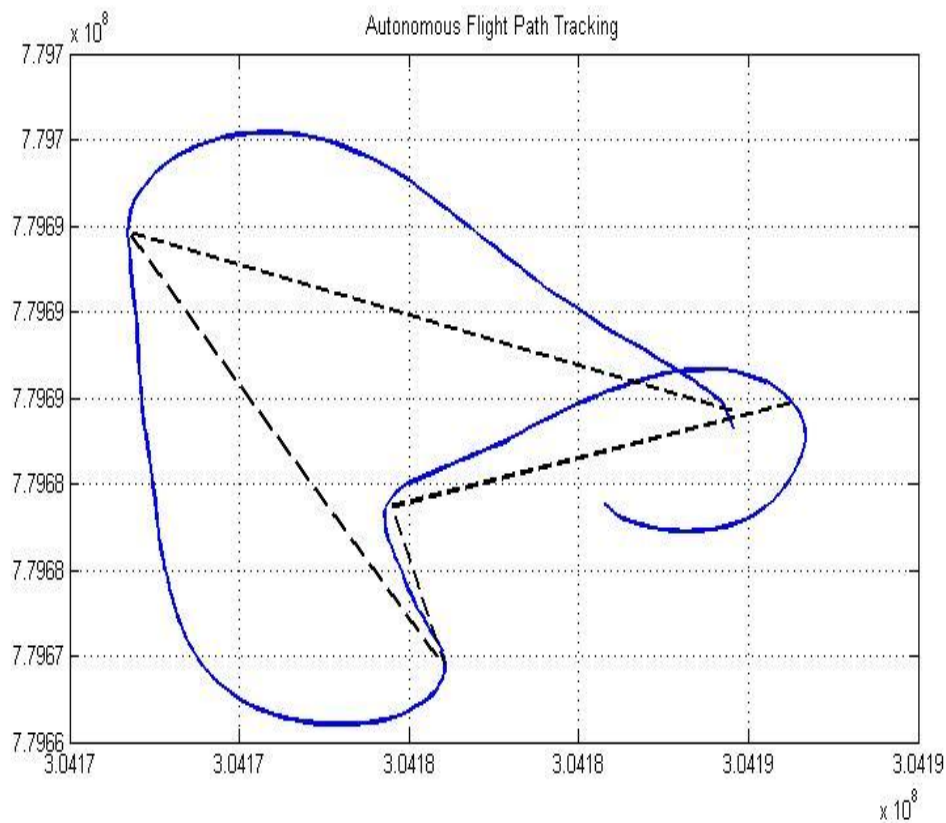


Figure. 5.18. Autonomous Path Covered 2D

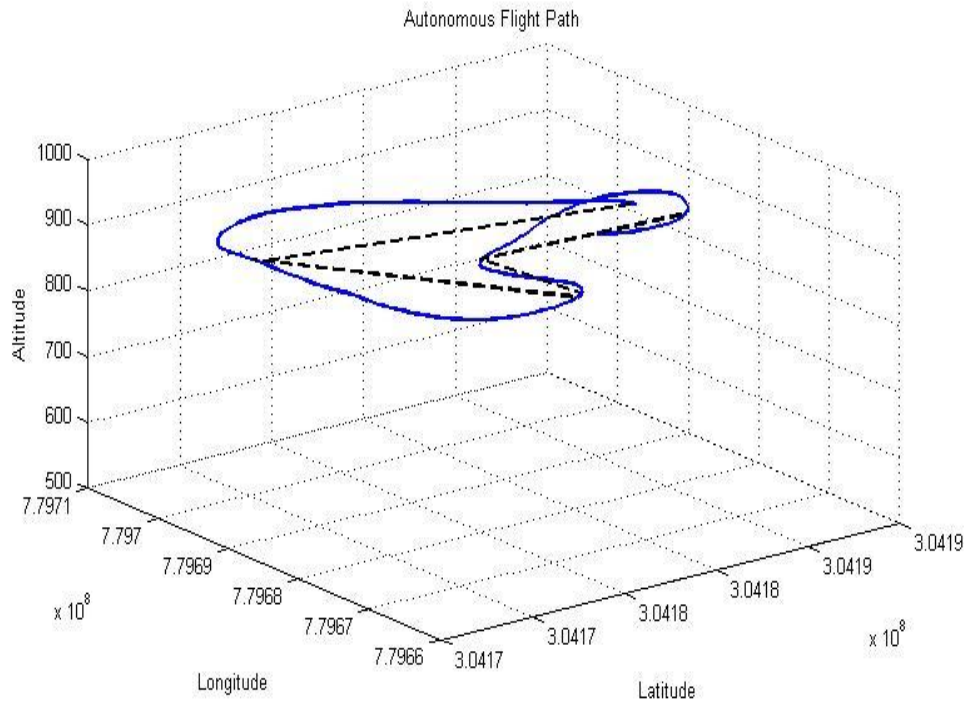


Figure. 5.19. Autonomous Path Covered 3D

#### 5.3.4. Aerial Distance covered by the Vehicle

The complete flight test was observed in mission planner software. The vehicle was successfully tested at University of Petroleum and Energy Studies, Dehradun, Bidholi Campus. The vehicle covered the above way points in the complete mission

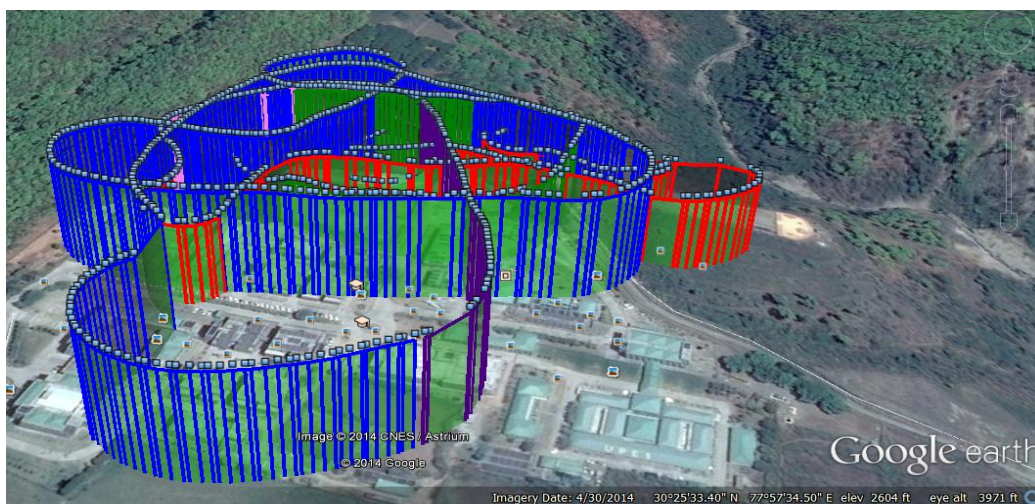


Figure. 5.20. Autonomous, Semi- Autonomous, Take off, Landing Path Covered



The above figure indicates the autonomous mode of the vehicle.

- Red: Semi-Autonomous Mode and take off
- Blue: Autonomous ( the vehicle auto stabilizing itself)
- Violet: Guided Mode (covered the given Way Points with altitude hold)
- Green: Total Path (overall path covered)
- Pink: Semi – Autonomous and Landing Mode

## CHAPTER 6

### CONCLUSION AND FUTURE SCOPE

#### 6.1.CONCLUSION

The initial section of the work discussed in detail about the Powered Parafoil Aerial Vehicles, the terms involved and the aerodynamic parameters that should be considered. The section also explains about different types of Unmanned Aerial Vehicles, their features, advantages and disadvantages. Keeping all the factors in view a Parafoil aerial vehicle is considered to be the most stable Aerial vehicle. Applications that require accurate vertical positioning like crop dusting, proximity sensing of targets and detection of substances and organisms that are altitude specific, high resolution and close range imaging can be performed easily using PAV platform. A benefit of the powered Parafoil for unmanned aircraft use is their unique ability to glide to the ground in a relatively safe manner, even if all control systems are disabled. This is particularly desirable in urban environments where a failure of any large UAV would likely result in collateral damage to structure on the ground. Powered Parafoils, on the other hand, would be unlikely to land with a vertical speed above 10m/s, making severe damage to any ground edifice or even the airframe itself is unlikely. As we can observe clearly from the comparison table discussed in chapter 2, PAV emerges as the most appropriate system for deployment in various fields such as oil and gas pipeline monitoring, regional surveying, etc. These systems can be easily automated as they do not need any high end equipment. A low end GPS and IMU can be used which reduces the complexity in programming and hardware development.

The experimental design section of this work shows that the flight test results and the analytical results of the Unmanned Powered Parafoil Aerial Vehicle match within the range. The section also discussed about the construction of the vehicle. The vehicle shape is in the triac form having a nose fitted with the electronics and control unit. A single servo is used for controlling the direction of the UPPAV. And BLDC motor used is used to take off, land and to maintain a level flight. The total weight of the payload is 3.8 kg. The next section gives the relation between size of the Parafoil and the payload weight. For a 4 kg payload the size of the Parafoil is taken as 2X0.65 m Parafoil. The system performance is also calculated where the lift and drag of the system is calculated. The Parafoil flight velocity is determined and turn performance is also determined. Three types of flight tests were performed and the flight test were compared with the analytical results and concluded the vehicle was performing as desired. It can be observed that during the level flight, while the vehicle is turning there are less number of oscillations, while the vehicle is climbing up the oscillations are more.

All the observations in this section are done on Payload. A lot of oscillations/vibrations are seen in the graphs as the sensors are placed on the Payload. The vibrations on the Parafoil would be comparatively lesser. Pitch angle, Glide Angle, heading angle, latitude, longitude, altitude and ground speed give the performance analysis of the complete system. The above mentioned graphs helped us in understanding the Parafoil performance.

The mathematical modeling section describes the 9 DOF model. A thrust vector is added on the payload to understand the powered Parafoil performance under various thrust conditions. The direction control simulation was done by a single servo connected to the “fly-bar”. The control effects are observed by tilting the “fly-bar” left and right indirectly controlling the Parafoil. The angle of attack, glide angle and pitch angle results were compared with the 9 DOF simulated results. The resulting glide angles can be used in the dynamic model for closed loop simulations and controlled flight. The estimated glide rates are used to

estimate the lift and drag coefficients needed for the dynamic model. The Control System and algorithm design section provides a comparison of lateral and longitudinal control theoretical results with practical results. The results indicate a small difference as in practical flight tests environmental conditions comes into picture especially wind conditions. Altitude hold using throttle control was successfully tested.

The following conclusions can be further made

- The successful completion of Autonomous Powered Parafoil Aerial Vehicle has produced a prototype capable of autonomous flight. Total flight duration was approximately 10 minutes for a 22.2V, 6000mah battery
- The developed vehicle was successful in carrying a payload of 3 kg with a 2 meter span Parafoil. For a larger payload the Parafoil span must be increased
- The ratio of horizontal base to the vertical base should be maintained 3:2 in order to avoid stall conditions
- The vehicle needs an air strip on 7 meters for a successful take off under zero wing conditions.
- The 9 DOF dynamic model has shown that the Parafoil uses two modes of direction control, skid steering and roll steering. It is observed that the Parafoil changes the direction due to the roll moment.
- The speed of the vehicle is approximately 10 meters/second. The low speed feature would help the vehicle to survey an area more efficiently compared to other conventional models.
- A turn rate of 18 degrees/second was observed when the vehicle takes a turn. It is observed that the PAV maintains a velocity of 10 meters/second for level flight and during the turn the velocity goes up to 12 meters/second, and the vehicle tends to lose the altitude which is then covered up by increasing the speed to 12 meters/second.

- The bank angle is observed to be 10 degrees while the vehicle is taking the turn and the turn indicated to be smooth without any oscillations. The effect of Parafoil deflection due to the canopy tilt is modeled using direction control modeling, which successfully replicates the turn performance.
- The incorporated collision avoidance sensors, GPS, Pressure and remote sensing device with telemetry transmitted the data successfully to the ground station.
- This project has shown that way point navigation has provided means for autonomous navigation.
- The guidance logic developed was able to generate heading and altitude signals, which enabled the PAV to follow desired path specified by the sequence of points.
- During the flight, if the GPS link is lost in the autonomous mode, PAV was rotating around the waypoint maintaining a radius of 2 meters.
- The Parafoil and electronics package was extremely rugged. Flight test landings occurred in muddy fields and hard road tops without sustaining any damage to the Parafoil and the electronics. Similar landings for the conventional fixed wing or rotor craft would have damaged the structure.

## 6.2. RECOMMENDATIONS FOR FUTURE WORK

- There are number of applications where the PAV would provide a unique capability that is not adequately satisfied by other devices currently available. The PAV is superior in terms of cost, ruggedness/durability, ease of use, portability, time to activate and reusability when compared with the competing technologies in variety of mission scenarios.
- There are number of military uses for developed PAV which include airdrop guidance, battle damage assessment, and communication in the rugged terrain. Civilian application include; an aid in search and rescue efforts, evaluating plant health by farmers and land management workers, and as a communications and observation device for forestry firefighting crews.

## 6.3.ADVANTAGES

- *Aerial Surveillance*

The developed prototype was successfully deployed to survey the given area.



Figure 6.1. Aerial Surveillance UPES Dump Area

- *Disaster Management*

The developed vehicle can be used in the case of a disaster such as floods, earthquakes, and draughts. These vehicles can drop packages safely from a low altitude in the affected areas.

- *Coastal Area Surveillance*

The vehicle can be used effectively for surveillance in coastal areas as parachute as a wing is much appropriate in wind conditions to hover around

- *Oil and gas pipeline monitoring*

The vehicle has the ability to hover slowly and in a straight line. This feature can be used in tracking a pipeline by giving the coordinates of the pipeline. This can be used to detect the leaks and thefts near and around the pipelines

#### **6.4.IMPACT OF THE DEVELOPED PROJECT**

The biggest problem oil and gas industry facing today is the safety and security of the pipelines. The development of the major sectors such as transportation, aviation, tourism is directly related to oil and gas in developing countries. Therefore proper and steady flow should be maintained in pipelines for the wealth and wellbeing of these economic sectors. Pipelines all over are facing various threats like natural hazards such as corrosion, earthquakes, and landslides, criminal actions such as oil theft and terrorist activities. Pipeline is an easy target to the terrorist organizations which can be a direct aim to damage western economics. A pipeline distribution system extends hundreds of miles having sensors, valves, pumps and controllers. With advancement in sensor technology, communication and signal processing in combination with automation, robotics and unmanned aerial vehicles offer powerful tool for detection of defects in pipelines and monitoring the complex pipeline system. According to the U.S. Department of Transportation's Office of Pipeline Safety (OPS), the majority of pipeline incidents are caused by "damage by outside force." Property damages alone for more than 300,000 miles of transmission pipe can cost operators millions of dollars annually.

## PUBLICATIONS

### Parachute Aerial Vehicle (Current Work)

#### *Journals*

- ✓ *Vindhya Devalla, Om Prakash, “Longitudinal and Directional Control Modeling for a Small Powered Parafoil Aerial Vehicle”, Aeronautical Journal, (Accepted).*

**Abstract-** The biggest problem oil and gas industry facing today is the safety and security of the pipelines which contributes to the increase in the maintenance cost of pipeline directly affecting the cost of fuel. An unmanned powered parachute aerial vehicle was developed for monitoring the oil and gas pipeline. It is envisioned that the vehicle would follow a planned trajectory to the target, and FLIR based system would be employed for extracting details about pipeline leakages, thefts, internal corrosion, internal waxing, etc. In this paper, a 9DOF parafoil simulation was created in the Matlab/Simulink environment to study the parafoil dynamics and assess the feasibility of the system. Longitudinal dynamics and direction control has been modeled and studied in detail. Thrust, pitch angle, glide angle and angle of attack was studied for the developed model and is validated with Lingards’s model.

- ✓ *Vindhya Devalla, Om Prakash, “Developments in Powered Parachute Aerial Vehicle: A Review”, IEEE Transactions of Aerospace and Electronics System, Volume 29 Issue 11, November 2014.*



**Abstract-** This paper discusses the recent developments made on powered parachute aerial vehicles over a decade. It reviews various modeling techniques and different parachute aerial vehicles developed for various applications focusing on the instrumentation involved. 9 DOF equations for a powered parachute vehicle are discussed in detail. The paper presents the comparison between various UAVs.

✓ *Vindhya Devalla, Om Prakash, “Modelling and Simulation of a Small Powered Parafoil Aerial Vehicle”, IEEE Transactions of Aerospace and Electronics System Society, (Under Review)*

**Abstract -** This Article describes the detailed derivation of the modelling of a small powered Parafoil aerial vehicle. In this model the Parafoil is connected to a payload which has a propulsion system attached. The Parafoil is connected to the payload at two joints. It is assumed to have nine degrees of freedom, modeled as two-body dynamics, consisting of three degrees of freedom for rotational motion of the Parafoil, three degrees of freedom for the rotational motion of the payload and three degrees of freedom for translational motion of the Parafoil. The nine degrees of freedom model incorporates nonlinear aerodynamics to predict all kinds of behavior. The nonlinear simulation demonstrates the validity of the proposed model through comparison with the Lingard’s data and Flight Tests.

### **Conferences**

- ✓ *Vindhya Devalla, Om Prakash “Angle of Attack, Pitch Angle and Glide Angle Modeling at Various Thrust Inputs for a Powered Parachute Aerial Vehicle” in AEDSS, A Doctoral fellows Symposium, held at IIT Kanpur, 2014.*
- ✓ *Vindhya Devalla, Om Prakash “Development of Position Tracking and Guidance System for Unmanned Powered Parafoil Aerial Vehicle” 4<sup>th</sup> International Conference on Reliability, Infocom Technologies and Optimization (ICRITO 2015), 2-4 September 2015 (Accepted)*

### **Awards**

- RnD C3 Award for Paper Publication in SCI listed Journals, UPES, RnD, March 2015, Received the award by Prof. C. N. R. Rao, Bharat Ratna, FRS
- Excellent Performance Award in UPES, Communication Meet, 2014, UPES November 2014
- 4th prize in Innovate India 2014, NRDC, DST, UCOST, March 2014, 4th prize in science model competition

### **Projects**

- Received a grant of 6 lakhs from DST- SERB for “Development of Parachute Aerial Vehicle for Oil and Gas Pipeline Monitoring” for a period of 1 year to do the feasibility study

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Aerodynamic Decelerator Systems Technology Conference Seminar 23-26  
May 2011, Dublin, Ireland.

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## APPENDIX A: OPEN LOOP FLIGHT TEST VALUES

### A.1 TAKE-OFF FLIGHT

| Roll (rad) | Pitch(rad) | Yaw (rad) | Roll Rate (rad/s) | Pitch Rate(rad/sec) | Yaw Rate (rad/s) | Time(s) | Groundspeed (m/s) | horizontal (m) | alt (m) | Heading (deg) |
|------------|------------|-----------|-------------------|---------------------|------------------|---------|-------------------|----------------|---------|---------------|
| -0.3358    | 0.579742   | -2.79052  | 0.69857           | 0.428751            | -0.1159          | 0.252   | 9.87              | 2.48724        | 857.46  | 198           |
| -0.40574   | 0.509943   | -2.92591  | -0.18393          | 0.151788            | 0.063419         | 1.095   | 7.49              | 8.20155        | 859.81  | 192           |
| -0.38815   | 0.517679   | -2.90887  | 0.286983          | -0.16429            | 0.137382         | 1.245   | 7.49              | 9.32505        | 861.35  | 192           |
| -0.34433   | 0.40734    | -2.91592  | -0.18633          | 0.36117             | -0.55516         | 1.655   | 7.2               | 11.916         | 861.76  | 194           |
| -0.41173   | 0.349503   | -2.96857  | -0.52236          | -0.15976            | -0.48891         | 1.655   | 7.2               | 11.916         | 861.76  | 191           |
| -0.45304   | 0.304857   | -2.98989  | -0.07485          | -0.28667            | -0.23403         | 1.86    | 7.17              | 13.3362        | 863.15  | 189           |
| -0.40498   | 0.115397   | -3.02023  | -0.01393          | -0.76637            | -0.74246         | 2.06    | 7.17              | 14.7702        | 863     | 188           |
| -0.45411   | 0.006039   | -3.07115  | -0.60031          | 0.44364             | -0.64588         | 2.092   | 7.14              | 14.93688       | 862.98  | 188           |
| -0.50258   | -0.03636   | -3.08222  | -0.04904          | -0.03418            | -0.011272        | 2.152   | 7.63              | 16.41976       | 864.18  | 185           |
| -0.44475   | -0.03758   | -3.05153  | 0.768542          | -0.0991             | 0.271474         | 2.307   | 7.63              | 17.60241       | 863.8   | 183           |
| -0.35682   | -0.05604   | -3.04394  | 0.437836          | -0.0842             | -0.24334         | 2.477   | 8.17              | 20.23709       | 864.45  | 184           |
| -0.42351   | -0.03941   | -3.10196  | -1.08799          | 0.411724            | -0.49423         | 2.502   | 8.17              | 20.44134       | 864.89  | 185           |
| -0.52627   | -0.01276   | 3.128624  | -0.32202          | 0.115605            | -0.22844         | 2.672   | 8.73              | 23.32656       | 864.99  | 184           |
| -0.47609   | -0.00168   | 3.11297   | 0.971808          | -0.08021            | -0.15129         | 2.707   | 9.34              | 25.28338       | 865.67  | 180           |
| -0.33979   | 0.020741   | 3.07734   | 0.672496          | 0.229742            | -0.48492         | 2.877   | 9.34              | 26.87118       | 866.36  | 178           |
| -0.47404   | 0.159652   | 2.959844  | -0.03042          | 0.605412            | 0.197777         | 3.082   | 10.25             | 31.5905        | 866.06  | 177           |
| -0.3607    | 0.224836   | 2.987146  | 1.30145           | 0.171476            | 0.353685         | 3.13    | 10.25             | 32.0825        | 865.85  | 174           |



|          |          |          |          |          |          |       |       |          |        |     |
|----------|----------|----------|----------|----------|----------|-------|-------|----------|--------|-----|
| 5        |          |          |          |          |          |       |       |          |        |     |
| -0.22977 | 0.27305  | 2.990301 | 0.463643 | 0.479834 | -0.23483 | 3.255 | 11.03 | 35.90265 | 866.72 | 170 |
| -0.30567 | 0.338202 | 2.916661 | -0.64793 | 0.577476 | -0.50753 | 3.387 | 11.03 | 37.35861 | 867.5  | 171 |
| -0.37212 | 0.380667 | 2.847188 | 0.373184 | 0.260072 | -0.24334 | 3.482 | 11.43 | 39.79926 | 866.67 | 169 |
| -0.29377 | 0.400258 | 2.814946 | 0.710542 | 0.163228 | -0.24254 | 3.7   | 11.43 | 42.291   | 868.68 | 164 |
| -0.29443 | 0.424428 | 2.777268 | -0.29408 | 0.231871 | -0.34444 | 3.732 | 11.32 | 42.24624 | 868.02 | 162 |
| -0.3596  | 0.441022 | 2.736303 | -0.05862 | 0.013972 | -0.29682 | 3.837 | 11.26 | 43.20462 | 869.29 | 160 |
| -0.34136 | 0.45397  | 2.656497 | -0.05516 | 0.290669 | -0.47268 | 4.145 | 11.26 | 46.6727  | 868.43 | 157 |
| -0.444   | 0.471072 | 2.585573 | -0.71338 | 0.217237 | -0.43171 | 4.32  | 10.8  | 46.656   | 869.76 | 153 |
| -0.52281 | 0.454657 | 2.551651 | -0.25471 | -0.14806 | -0.31651 | 4.36  | 10.05 | 43.818   | 869.69 | 146 |
| -0.55877 | 0.432708 | 2.536303 | -0.34782 | -0.10496 | -0.26143 | 4.522 | 10.05 | 45.4461  | 871.13 | 145 |
| -0.8321  | 0.380679 | 2.544939 | -0.21373 | 0.236393 | -0.45911 | 5.14  | 10.13 | 52.0682  | 870.41 | 144 |
| -0.94854 | 0.371183 | 2.456577 | -1.14439 | 0.650641 | -0.51951 | 5.172 | 10.18 | 52.65096 | 871.14 | 143 |
| -1.13832 | 0.366533 | 2.377257 | -1.28274 | 0.416513 | -0.27553 | 5.21  | 10.11 | 52.6731  | 871.95 | 138 |
| -1.22481 | 0.356728 | 2.346642 | -0.14349 | 0.132366 | -0.15076 | 5.38  | 10.11 | 54.3918  | 872.25 | 135 |
| -1.21287 | 0.34406  | 2.31764  | 0.098616 | 0.27843  | -0.3612  | 5.457 | 10.72 | 58.49904 | 873.26 | 133 |
| -1.27591 | 0.309047 | 2.237592 | -0.66576 | 0.680439 | -0.60677 | 5.495 | 11.2  | 61.544   | 872.19 | 130 |
| -1.39437 | 0.268805 | 2.1198   | -0.54497 | 0.870402 | -0.50062 | 5.688 | 11.2  | 63.7056  | 872.5  | 124 |
| -1.42509 | 0.239066 | 2.013958 | 0.39846  | 0.696668 | -0.35748 | 5.73  | 11.25 | 64.4625  | 873.43 | 118 |
| -1.37786 | 0.204044 | 1.91962  | 0.611038 | 0.720081 | -0.52509 | 5.895 | 11.25 | 66.31875 | 872.9  | 112 |

|                  |                  |              |                  |                  |                  |       |              |              |        |     |
|------------------|------------------|--------------|------------------|------------------|------------------|-------|--------------|--------------|--------|-----|
| -<br>1.4022<br>7 | 0.1461<br>65     | 1.8051<br>26 | -<br>0.2552<br>4 | 0.7594<br>57     | -<br>0.6671<br>7 | 5.995 | 11.92        | 71.460<br>4  | 873.89 | 106 |
| -<br>1.4466<br>6 | 0.0872<br>19     | 1.6960<br>93 | 0.2321<br>75     | 0.7238<br>06     | -0.449           | 6.173 | 12.65        | 78.088<br>45 | 874.04 | 100 |
| -<br>1.3441<br>1 | 0.0478<br>23     | 1.6081<br>16 | 1.4328<br>81     | 0.6181<br>82     | -<br>0.4798<br>6 | 6.25  | 12.65        | 79.062<br>5  | 874.82 | 94  |
| -<br>1.2460<br>7 | 0.0006<br>17     | 1.4845<br>23 | 0.4003<br>22     | 0.8866<br>32     | -<br>0.7664<br>1 | 6.39  | 12.95        | 82.750<br>5  | 873.46 | 88  |
| -<br>1.2467<br>4 | -0.06            | 1.3642<br>44 | 0.3542<br>95     | 0.6932<br>1      | -<br>0.7142<br>6 | 6.463 | 12.95        | 83.695<br>85 | 874.73 | 81  |
| -<br>1.1265<br>8 | -<br>0.0989<br>8 | 1.2607<br>03 | 1.497            | 0.7222<br>1      | -<br>0.5729<br>8 | 6.68  | 13.39        | 89.445<br>2  | 874.26 | 75  |
| -<br>0.9963<br>1 | -<br>0.1078<br>1 | 1.1214<br>11 | 0.6416<br>34     | 1.0502<br>55     | -<br>0.6075<br>7 | 6.823 | 13.73        | 93.679<br>79 | 873.92 | 68  |
| -<br>0.9912      | -<br>0.0994<br>8 | 0.9908<br>54 | 0.1728<br>45     | 0.8299<br>62     | -<br>0.3492<br>3 | 6.863 | 13.73        | 94.228<br>99 | 873.63 | 60  |
| -<br>0.4970<br>3 | -<br>0.0170<br>1 | 0.7307<br>46 | 0.6514<br>78     | 0.1847<br>79     | -<br>0.1728<br>4 | 7.66  | 13.41        | 102.72<br>06 | 873.76 | 54  |
| -<br>0.4489<br>1 | -<br>0.0023<br>9 | 0.7062<br>67 | 0.1810<br>93     | 0.1916<br>96     | -<br>0.0613<br>6 | 7.69  | 12.94        | 99.508<br>6  | 873.95 | 42  |
| -<br>0.4046<br>1 | 0.0334<br>88     | 0.6914<br>21 | 0.4303<br>86     | 0.3207<br>33     | 0.0793<br>82     | 7.71  | 12.19        | 93.984<br>9  | 875.48 | 41  |
| -<br>0.3499<br>5 | 0.0859<br>2      | 0.6925<br>74 | 0.2752<br>76     | 0.3789<br>99     | 0.2084<br>19     | 7.875 | 12.19        | 95.996<br>25 | 876.12 | 39  |
| -<br>0.3032<br>4 | 0.1102<br>44     | 0.6848<br>1  | 0.3862<br>21     | -<br>0.0746<br>2 | -<br>0.1403<br>8 | 7.925 | 11.65        | 92.326<br>25 | 874.48 | 39  |
| -<br>0.2864<br>8 | 0.0532<br>46     | 0.6423<br>28 | -<br>0.1235<br>4 | -<br>0.5162<br>8 | -<br>0.6397<br>6 | 8.018 | 11.65        | 93.409<br>7  | 876.15 | 39  |
| -<br>0.3364      | -<br>0.0132<br>2 | 0.5605<br>23 | -<br>0.6255<br>9 | -<br>0.1874<br>3 | -<br>0.8012<br>6 | 8.44  | 10.93        | 92.249<br>2  | 876.02 | 38  |
| -<br>0.3829<br>2 | -<br>0.0251<br>2 | 0.4966<br>59 | -<br>0.2560<br>4 | 0.1964<br>85     | -<br>0.2215<br>3 | 8.473 | 10.5         | 88.966<br>5  | 876.19 | 34  |
| -<br>0.3736<br>1 | 0.0166<br>48     | 0.4883<br>39 | 0.2356<br>34     | 0.2483<br>66     | 0.3765<br>66     | 8.645 | 10.5         | 90.772<br>5  | 876.74 | 30  |
| -<br>0.3352      | 0.0350<br>22     | 0.5343<br>83 | 0.1656<br>62     | -<br>0.2935<br>9 | 0.4563<br>82     | 8.713 | 9.77         | 85.126<br>01 | 875.88 | 27  |
| -<br>0.4478<br>2 | -<br>0.1701<br>6 | 0.4872<br>9  | -<br>0.3778<br>9 | -<br>0.0871<br>3 | -<br>0.2140<br>8 | 9.32  | 9.77         | 91.056<br>4  | 876.67 | 29  |
| -<br>0.5173      | -<br>0.3242      | 0.4289<br>78 | -<br>0.3182      | -<br>0.1834      | -<br>0.1760      | 9.598 | 9.3899<br>99 | 90.125<br>21 | 877.23 | 31  |

|                  |                  |                  |                  |                  |                  |        |       |              |        |     |
|------------------|------------------|------------------|------------------|------------------|------------------|--------|-------|--------------|--------|-----|
| 3                | 1                |                  | 9                | 4                | 3                |        |       |              |        |     |
| -<br>0.5001<br>5 | -<br>0.3081<br>5 | 0.4513<br>08     | 0.3130<br>56     | -<br>0.1440<br>7 | 0.1863<br>37     | 9.923  | 8.9   | 88.314<br>7  | 878.2  | 24  |
| -<br>0.4867<br>7 | -<br>0.3343<br>1 | 0.4595<br>2      | -<br>0.0820<br>4 | -<br>0.2930<br>6 | -<br>0.2625      | 9.963  | 8.9   | 88.670<br>7  | 878.65 | 24  |
| -<br>0.3959<br>4 | -<br>0.2747<br>1 | 0.0316<br>16     | 0.3010<br>84     | 0.2709<br>81     | -<br>0.3263<br>5 | 10.903 | 9.17  | 99.980<br>51 | 879.92 | 25  |
| -<br>0.3698      | -<br>0.2584      | -<br>0.0183<br>4 | -<br>0.1826      | 0.2342<br>65     | -<br>0.3409<br>8 | 10.971 | 9.17  | 100.60<br>41 | 879.74 | 26  |
| -<br>0.3869<br>3 | -<br>0.2408<br>1 | -<br>0.0661<br>3 | -<br>0.2323<br>6 | 0.2406<br>5      | -<br>0.2135<br>4 | 11.113 | 10.53 | 117.01<br>99 | 877.85 | 6   |
| -<br>0.3858<br>5 | -<br>0.2171      | -<br>0.0942<br>2 | 0.1387<br>9      | 0.1972<br>83     | -<br>0.0475<br>3 | 11.318 | 10.75 | 121.66<br>85 | 879.81 | 0   |
| -<br>0.3477<br>8 | -<br>0.1926<br>7 | -<br>0.1182<br>5 | 0.3231<br>66     | 0.2172<br>37     | -<br>0.1057<br>9 | 11.351 | 10.78 | 122.36<br>38 | 879.86 | 357 |
| -<br>0.3275<br>4 | -<br>0.1647<br>3 | -<br>0.1560<br>8 | -<br>0.0330<br>8 | 0.3188<br>7      | -<br>0.3098<br>6 | 11.421 | 10.92 | 124.71<br>73 | 879.25 | 355 |
| -<br>0.3311<br>1 | -<br>0.1415<br>7 | -<br>0.2142<br>1 | -<br>0.1094<br>4 | 0.2864<br>12     | -<br>0.4772      | 11.481 | 10.92 | 125.37<br>25 | 878.4  | 353 |
| -<br>0.3361<br>3 | -<br>0.1350<br>5 | -<br>0.2824<br>9 | -<br>0.0575<br>6 | 0.2206<br>96     | -<br>0.5216<br>4 | 11.771 | 10.95 | 128.89<br>25 | 879.87 | 352 |
| -<br>0.3274<br>7 | -<br>0.1234<br>6 | -<br>0.3487<br>9 | -<br>0.0897<br>5 | 0.2680<br>54     | -<br>0.3992<br>5 | 11.936 | 10.95 | 130.69<br>92 | 879.53 | 349 |
| -<br>0.3598<br>5 | -<br>0.1058<br>4 | -<br>0.3927<br>8 | -<br>0.4523<br>8 | 0.1877<br>05     | -<br>0.1733<br>7 | 11.978 | 10.78 | 129.12<br>28 | 879.59 | 345 |
| -<br>0.3849<br>4 | -<br>0.0834<br>4 | -<br>0.4139<br>6 | 0.0470<br>01     | 0.2622<br>01     | 0.0626<br>21     | 12.033 | 10.57 | 127.18<br>88 | 878.88 | 341 |
| -<br>0.3455<br>4 | -<br>0.0564<br>3 | -<br>0.4242<br>9 | 0.3965<br>97     | 0.1890<br>36     | -<br>0.0038<br>9 | 12.093 | 10.57 | 127.82<br>3  | 879.13 | 338 |
| -<br>0.3234<br>1 | -<br>0.0534<br>5 | -<br>0.4595<br>7 | 0.0150<br>75     | 0.0123<br>75     | -<br>0.3372<br>6 | 12.293 | 10.62 | 130.55<br>17 | 879.47 | 336 |
| -<br>0.3313<br>4 | -<br>0.0697<br>7 | -<br>0.5203      | -<br>0.0942<br>7 | 0.0621<br>27     | -<br>0.5626<br>1 | 12.333 | 10.62 | 130.97<br>65 | 878.82 | 335 |
| -<br>0.3163<br>5 | -<br>0.0782<br>9 | -<br>0.5886<br>5 | 0.2970<br>93     | 0.1712<br>1      | -<br>0.4705<br>5 | 12.623 | 10.25 | 129.38<br>58 | 879.24 | 334 |
| -<br>0.2706      | -<br>0.0677<br>8 | -<br>0.6450<br>6 | 0.3939<br>37     | 0.1682<br>83     | -<br>0.3056      | 12.623 | 10.28 | 129.76<br>44 | 879.55 | 332 |
| -<br>0.2289<br>3 | -<br>0.0593<br>6 | -<br>0.6869      | 0.2468<br>08     | 0.0799<br>53     | -<br>0.3029<br>4 | 12.768 | 10.28 | 131.25<br>5  | 880.42 | 328 |

|                  |                  |                  |                  |                  |                  |        |              |              |        |     |
|------------------|------------------|------------------|------------------|------------------|------------------|--------|--------------|--------------|--------|-----|
| -<br>0.2141<br>1 | -<br>0.0645<br>7 | -<br>0.7234<br>7 | 0.1760<br>38     | -<br>0.0411      | -0.246           | 12.813 | 9.88         | 126.59<br>24 | 879.82 | 324 |
| -<br>0.1745<br>7 | -<br>0.0601<br>3 | -<br>0.7593      | 0.4644<br>41     | 0.1935<br>59     | -<br>0.2332<br>3 | 12.998 | 9.46         | 122.96<br>11 | 879.04 | 321 |
| -<br>0.1156<br>8 | -<br>0.0331<br>6 | -<br>0.7908      | 0.3702<br>58     | 0.2906<br>69     | -<br>0.1794<br>9 | 13.071 | 9.46         | 123.65<br>17 | 880.02 | 319 |
| -<br>0.1181<br>5 | -<br>0.0029<br>6 | -<br>0.8110<br>7 | -<br>0.1770<br>2 | 0.1451<br>37     | -<br>0.0754<br>6 | 13.208 | 9.53         | 125.87<br>22 | 880.83 | 317 |
| -<br>0.1269<br>4 | -<br>0.0020<br>8 | -<br>0.8236<br>3 | 0.1566<br>16     | -<br>0.1132      | -<br>0.1034      | 13.311 | 9.53         | 126.85<br>38 | 879.54 | 315 |
| -<br>0.0874<br>8 | -<br>0.0295<br>5 | -<br>0.8368<br>3 | 0.4250<br>65     | -<br>0.2858<br>7 | -<br>0.1329<br>3 | 13.583 | 8.9299<br>99 | 121.29<br>62 | 880.62 | 313 |
| -<br>0.0360<br>3 | -<br>0.0573<br>1 | -<br>0.9120<br>5 | 0.0134<br>78     | 0.0634<br>58     | -<br>0.2875<br>1 | 13.718 | 8.9299<br>99 | 122.50<br>17 | 880.29 | 312 |
| -<br>0.0340<br>9 | -<br>0.0302<br>4 | -<br>0.9335<br>3 | 0.0909           | 0.2877<br>42     | -<br>0.0536<br>4 | 13.796 | 8.6799<br>99 | 119.74<br>93 | 879.71 | 306 |
| 0.0150<br>68     | 0.0031<br>49     | -<br>0.9237<br>4 | 0.0334<br>32     | 0.0230<br>17     | 0.0107<br>4      | 14.123 | 8.7          | 122.87<br>01 | 881.04 | 306 |
| -<br>0.0059      | -<br>0.0088<br>9 | -<br>0.9348<br>3 | -<br>0.2270<br>4 | -<br>0.2151      | -<br>0.1374<br>5 | 14.153 | 8.7          | 123.13<br>11 | 881.3  | 306 |
| -<br>0.0309<br>7 | -<br>0.0290<br>4 | -<br>0.9558<br>2 | -<br>0.1062<br>5 | -<br>0.1770<br>6 | -<br>0.1890<br>7 | 14.298 | 8.48         | 121.24<br>7  | 880.58 | 306 |
| -<br>0.0322<br>9 | -<br>0.0503<br>9 | -<br>0.9799      | 0.0786<br>62     | -<br>0.1967<br>4 | -<br>0.1997<br>1 | 14.508 | 8.48         | 123.02<br>78 | 880.98 | 305 |
| -<br>0.0246<br>2 | -<br>0.0723      | -<br>0.9997      | 0.1217<br>63     | -<br>0.1674<br>8 | -<br>0.1409<br>1 | 14.658 | 8.34         | 122.24<br>77 | 881.18 | 304 |
| 0.0057<br>18     | -<br>0.0813      | -<br>1.0195<br>2 | 0.3082<br>67     | -<br>0.0328<br>5 | -<br>0.1278<br>7 | 14.718 | 8.5          | 125.10<br>3  | 881.1  | 303 |
| 0.0123<br>95     | -<br>0.0776<br>1 | -<br>1.0344<br>4 | -<br>0.0543<br>7 | 0.0038<br>61     | -<br>0.1640<br>6 | 14.778 | 8.5          | 125.61<br>3  | 880.56 | 302 |
| -<br>0.0120<br>6 | -<br>0.0825<br>1 | -<br>1.0417<br>2 | -<br>0.1466<br>9 | -<br>0.0860<br>7 | -<br>0.0887<br>6 | 14.948 | 8.49         | 126.90<br>85 | 880.14 | 301 |
| -<br>0.0174<br>5 | -<br>0.0980<br>1 | -<br>1.0388<br>6 | 0.0395<br>52     | -<br>0.1395<br>4 | -<br>0.0078<br>8 | 14.971 | 8.49         | 127.10<br>38 | 881.18 | 300 |
| 0.0091<br>63     | -<br>0.1107<br>2 | -<br>1.0404<br>7 | 0.1973<br>22     | -<br>0.0599<br>9 | -<br>0.1132<br>4 | 15.228 | 8.54         | 130.04<br>71 | 881.52 | 300 |
| 0.0075<br>5      | -<br>0.1172<br>9 | -<br>1.0559      | -<br>0.2400<br>7 | -<br>0.0591<br>9 | -<br>0.1986<br>4 | 15.361 | 8.62         | 132.41<br>18 | 880.92 | 300 |
| -<br>0.0330      | -<br>0.1260      | -<br>1.0737      | -<br>0.3552      | -<br>0.1108      | -<br>0.1020      | 15.401 | 8.62         | 132.75<br>66 | 880.87 | 300 |

|          |           |          |           |          |          |        |          |          |        |     |
|----------|-----------|----------|-----------|----------|----------|--------|----------|----------|--------|-----|
| 8        | 4         | 9        | 7         | 1        | 7        |        |          |          |        |     |
| -0.05664 | -0.12606  | -1.07257 | 0.007625  | 0.101504 | 0.055704 | 15.556 | 8.69     | 135.1816 | 881.02 | 298 |
| -0.03234 | -0.10458  | -1.05269 | 0.335937  | 0.195687 | 0.185006 | 15.618 | 8.69     | 135.7204 | 880.55 | 298 |
| -0.02478 | -0.08397  | -1.0449  | -0.10172  | 0.054146 | -0.0148  | 15.751 | 8.83     | 139.0813 | 881.45 | 299 |
| -0.04776 | -0.0831   | -1.06454 | -0.25577  | -0.08154 | -0.20503 | 15.83  | 8.929999 | 141.3619 | 880.46 | 300 |
| -0.07404 | -0.09019  | -1.0881  | -0.05596  | -0.08074 | -0.1457  | 15.968 | 8.929999 | 142.5942 | 880.35 | 299 |
| -0.05251 | -0.10168  | -1.09652 | -0.192893 | 0.070839 | 0.003839 | 16.238 | 8.92     | 144.843  | 880.62 | 298 |
| -0.04231 | -0.0958   | -1.09327 | 0.288939  | 0.147463 | 0.090573 | 16.248 | 8.92     | 144.9322 | 880.59 | 297 |
| -0.00418 | -0.07065  | -1.06571 | 0.382856  | 0.146399 | 0.216683 | 16.415 | 9.23     | 151.5105 | 880.82 | 297 |
| 0.029784 | -0.06199  | -1.05169 | 0.212315  | -0.01084 | -0.07571 | 16.448 | 9.469999 | 155.7625 | 880.73 | 298 |
| 0.021614 | -0.06456  | -1.07923 | -0.31554  | -0.00499 | -0.35454 | 16.583 | 9.469999 | 157.041  | 880.8  | 299 |
| -0.05492 | -0.05498  | -1.11399 | -0.57388  | 0.105426 | -0.18506 | 16.69  | 9.49     | 158.3881 | 880.39 | 298 |
| -0.091   | -0.04271  | -1.11077 | -0.06651  | 0.09505  | 0.070087 | 16.883 | 9.559999 | 161.4015 | 879.94 | 296 |
| -0.09216 | -0.02583  | -1.09834 | -0.04762  | 0.17939  | 0.046674 | 17.085 | 9.559999 | 163.3326 | 879.52 | 296 |
| -0.12849 | -9.76E-05 | -1.10075 | -0.52998  | 0.227013 | -0.06693 | 17.123 | 9.45     | 161.8124 | 880.41 | 296 |
| -0.19705 | 0.027998  | -1.11025 | -0.48555  | 0.255747 | -0.01718 | 17.333 | 9.45     | 163.7969 | 880.84 | 297 |
| -0.22456 | 0.048017  | -1.11438 | -0.03831  | 0.084674 | 0.033903 | 17.35  | 9.62     | 166.907  | 881.98 | 296 |
| -0.22516 | 0.050043  | -1.13017 | -0.00718  | -0.00233 | -0.19783 | 17.523 | 9.4      | 164.7162 | 881.33 | 296 |
| -0.23862 | 0.046656  | -1.16944 | -0.14979  | 0.039977 | -0.3258  | 17.615 | 9.4      | 165.581  | 881.1  | 295 |
| -0.26789 | 0.045458  | -1.20758 | -0.0713   | 0.044766 | -0.22922 | 17.718 | 9.44     | 167.2579 | 881.31 | 293 |

|                  |                  |                  |                  |                  |                   |        |              |              |        |     |
|------------------|------------------|------------------|------------------|------------------|-------------------|--------|--------------|--------------|--------|-----|
| -<br>0.2447<br>1 | 0.0432<br>98     | -<br>1.2308<br>2 | 0.3887<br>09     | -<br>0.0174<br>9 | -<br>0.1613<br>8  | 17.813 | 9.44         | 168.15<br>47 | 879.89 | 291 |
| -<br>0.1885      | 0.0438<br>54     | -<br>1.2558<br>3 | 0.5212<br>04     | 0.1046<br>28     | -<br>0.2571<br>6  | 17.925 | 9.49         | 170.10<br>83 | 880.57 | 289 |
| -<br>0.1553      | 0.0506<br>36     | -<br>1.3002<br>8 | 0.1218<br>56     | 0.0977<br>11     | -<br>0.4157<br>3  | 18.028 | 9.3          | 167.66<br>04 | 881.67 | 288 |
| -<br>0.1891      | 0.0434<br>84     | -<br>1.3509<br>6 | -<br>0.3570<br>4 | -<br>0.0209<br>5 | -<br>0.4657<br>5  | 18.268 | 9.3          | 169.89<br>24 | 882.29 | 286 |
| -<br>0.2087<br>2 | 0.0354<br>84     | -<br>1.3937<br>9 | 0.0332<br>6      | 0.0788<br>21     | -<br>0.3223<br>4  | 18.318 | 9.3099<br>99 | 170.54<br>06 | 881.87 | 283 |
| -<br>0.1889<br>1 | 0.0476<br>44     | -<br>1.4222      | 0.1599<br>02     | 0.2046<br>65     | -<br>0.1935<br>7  | 18.42  | 9.3099<br>99 | 171.49<br>02 | 881.58 | 280 |
| -<br>0.2217<br>1 | 0.0643<br>2      | -<br>1.4411<br>1 | -<br>0.5613<br>7 | 0.1251<br>14     | -<br>0.0924<br>7  | 18.675 | 9.29         | 173.49<br>08 | 881.26 | 279 |
| -<br>0.3129<br>2 | 0.0651<br>78     | -<br>1.4432<br>5 | -<br>0.5802<br>6 | -<br>0.0515<br>5 | -<br>0.0208<br>67 | 18.705 | 9.21         | 172.27<br>31 | 881.61 | 277 |
| -<br>0.3198<br>1 | 0.0497<br>45     | -<br>1.4334<br>7 | 0.2969<br>2      | -<br>0.2090<br>5 | 0.0025<br>09      | 18.775 | 9.21         | 172.91<br>78 | 881.26 | 277 |
| -<br>0.2855<br>7 | 0.0134<br>92     | -<br>1.4495<br>9 | 0.1622<br>96     | -<br>0.2308<br>7 | -0.387            | 18.845 | 9.1399<br>99 | 172.24<br>33 | 881.28 | 277 |
| -<br>0.3216<br>9 | -<br>0.0215<br>8 | -<br>1.5083<br>5 | -<br>0.5443<br>5 | -<br>0.0438<br>3 | -<br>0.6666<br>2  | 19.058 | 9.1399<br>99 | 174.19<br>01 | 881.3  | 277 |
| -<br>0.3753<br>1 | -<br>0.0330<br>9 | -<br>1.5750<br>9 | -<br>0.2431<br>7 | 0.1506<br>56     | -<br>0.4750<br>6  | 19.098 | 9.0999<br>99 | 173.79<br>18 | 881.83 | 274 |
| -<br>0.3741<br>2 | -<br>0.0322<br>2 | -<br>1.6177<br>9 | 0.1742<br>69     | 0.1312<br>34     | -<br>0.2223<br>1  | 19.395 | 9.19         | 178.24<br>01 | 881.85 | 270 |
| -<br>0.3601<br>7 | -<br>0.0171<br>4 | -<br>1.6423<br>3 | 0.0925<br>9      | 0.1535<br>82     | -<br>0.0802<br>3  | 19.395 | 9.19         | 178.24<br>01 | 881.21 | 267 |
| -<br>0.3433<br>7 | -<br>0.0197<br>7 | -<br>1.6656<br>5 | 0.2335<br>99     | -<br>0.0002      | -<br>0.2813<br>7  | 19.478 | 9.17         | 178.61<br>33 | 882.17 | 266 |
| -<br>0.3361<br>3 | -<br>0.0183<br>3 | -<br>1.7302      | -<br>0.0750<br>2 | 0.3390<br>23     | -<br>0.5540<br>8  | 19.673 | 9.17         | 180.40<br>14 | 881.52 | 265 |
| -<br>0.3904      | 0.0092<br>15     | -<br>1.8098<br>9 | -<br>0.6071<br>3 | 0.4946<br>65     | -<br>0.4516<br>5  | 19.733 | 9.42         | 185.88<br>49 | 882.56 | 262 |
| -<br>0.4596      | 0.0391<br>88     | -<br>1.8662<br>2 | -<br>0.2833<br>5 | 0.3334<br>35     | -<br>0.2180<br>5  | 19.815 | 9.6399<br>99 | 191.01<br>66 | 882.92 | 257 |
| -<br>0.4590<br>9 | 0.0487<br>6      | -<br>1.9091<br>1 | 0.1234<br>52     | 0.1328<br>3      | -<br>0.3029<br>2  | 19.998 | 9.6399<br>99 | 192.78<br>07 | 882.04 | 253 |
| -<br>0.4955      | 0.0321<br>83     | -<br>1.9663      | -<br>0.5720      | 0.1581<br>05     | -<br>0.5676       | 20.11  | 9.66         | 194.26<br>26 | 882.73 | 251 |

|          |          |          |          |          |          |        |          |          |        |     |
|----------|----------|----------|----------|----------|----------|--------|----------|----------|--------|-----|
| 2        |          | 5        | 2        |          | 5        |        |          |          |        |     |
| -0.60731 | 0.027748 | -2.04064 | -0.9389  | 0.324922 | -0.42664 | 20.285 | 9.66     | 195.9531 | 882.6  | 248 |
| -0.68935 | 0.030871 | -2.09497 | -0.20752 | 0.263197 | -0.2702  | 20.355 | 9.719999 | 197.8506 | 882.2  | 244 |
| -0.66726 | 0.025511 | -2.14585 | 0.429149 | 0.252289 | -0.43888 | 20.493 | 9.76     | 200.0117 | 882.24 | 240 |
| -0.67433 | 0.00902  | -2.22647 | -0.52146 | 0.349931 | -0.71052 | 20.535 | 9.76     | 200.4216 | 882.32 | 238 |
| -0.75498 | -0.00359 | -2.3105  | -0.52732 | 0.436399 | -0.46389 | 20.688 | 9.91     | 205.0181 | 882.05 | 234 |
| -0.73124 | 0.013849 | -2.35699 | 0.851113 | 0.371747 | -0.02809 | 20.942 | 9.91     | 207.5352 | 881.25 | 229 |
| -0.59131 | 0.045311 | -2.37932 | 1.135791 | 0.365894 | -0.05656 | 20.972 | 9.8      | 205.5256 | 881.88 | 225 |
| -0.51782 | 0.044336 | -2.42851 | 0.503645 | 0.245371 | -0.43967 | 21.02  | 10.37    | 217.9774 | 881.59 | 224 |
| -0.41151 | 0.031739 | -2.50233 | 1.237424 | 0.186573 | -0.60915 | 21.255 | 10.37    | 220.4144 | 882.14 | 222 |
| -0.2209  | 0.029877 | -2.58625 | 1.644222 | 0.230472 | -0.67221 | 21.3   | 10.4     | 221.52   | 882.89 | 218 |
| -0.05502 | 0.056009 | -2.66756 | 1.148828 | 0.342747 | -0.53785 | 21.455 | 10.4     | 223.132  | 882.03 | 213 |
| 0.048819 | 0.09183  | -2.70255 | 0.844461 | 0.198014 | -0.01425 | 21.512 | 10.47    | 225.2306 | 881.38 | 208 |
| 0.178362 | 0.099962 | -2.68177 | 1.306864 | 0.021353 | 0.279738 | 21.762 | 10.44    | 227.1953 | 881.39 | 205 |
| 0.3224   | 0.093188 | -2.65808 | 0.845259 | 0.031995 | 0.092702 | 21.797 | 10.44    | 227.5607 | 881.22 | 205 |
| 0.320393 | 0.114596 | -2.66828 | -0.58452 | 0.229674 | -0.13025 | 21.882 | 10.48    | 229.3234 | 881.94 | 207 |
| 0.234631 | 0.146031 | -2.67141 | -0.57627 | 0.244041 | 0.028582 | 22.022 | 10.55    | 232.3321 | 881.27 | 207 |
| 0.189856 | 0.171846 | -2.66367 | -0.35944 | 0.119261 | 0.025656 | 22.342 | 10.55    | 235.7081 | 881.14 | 206 |
| -0.02153 | 0.147798 | -2.6919  | -1.50294 | -0.32585 | -0.0664  | 22.555 | 10.11    | 228.0311 | 882.67 | 207 |
| -0.08447 | 0.134937 | -2.69566 | -1.52263 | -0.30137 | -0.03527 | 22.592 | 10.11    | 228.4051 | 881.95 | 207 |

|          |          |          |          |          |          |        |       |          |        |     |
|----------|----------|----------|----------|----------|----------|--------|-------|----------|--------|-----|
| -0.20966 | 0.107085 | -2.6733  | -0.54887 | -0.1883  | 0.357692 | 22.622 | 10.13 | 229.1609 | 881.82 | 205 |
| -0.20379 | 0.109796 | -2.62555 | 0.361305 | -0.00312 | 0.392279 | 22.682 | 9.82  | 222.7372 | 882.52 | 206 |
| -0.19011 | 0.125072 | -2.60192 | -0.18677 | 0.083876 | 0.074876 | 22.705 | 9.82  | 222.9631 | 882.98 | 209 |
| -0.25946 | 0.108705 | -2.603   | 0.064122 | -0.02308 | 0.011821 | 23.002 | 9.79  | 225.1896 | 882.12 | 210 |
| -0.24888 | 0.112418 | -2.60448 | 0.366627 | 0.153582 | 0.000114 | 23.057 | 9.79  | 225.728  | 883.49 | 211 |
| -0.15996 | 0.149208 | -2.60666 | 0.87825  | 0.396757 | 0.020867 | 23.082 | 9.66  | 222.9721 | 883.25 | 210 |
| -0.07145 | 0.179999 | -2.61883 | 0.659819 | 0.089463 | -0.14089 | 23.23  | 9.57  | 222.3111 | 882.78 | 210 |
| -0.04003 | 0.166261 | -2.65734 | 0.154847 | -0.24444 | -0.36438 | 23.425 | 9.57  | 224.1773 | 884.28 | 209 |
| -0.01694 | 0.139827 | -2.70867 | 0.393764 | -0.17047 | -0.40136 | 23.465 | 9.23  | 216.582  | 884.79 | 207 |
| 0.04832  | 0.12791  | -2.75327 | 0.621241 | -0.00073 | -0.31569 | 23.572 | 9.23  | 217.5696 | 884.15 | 204 |
| 0.076369 | 0.135439 | -2.77805 | 0.048159 | 0.068445 | -0.10418 | 23.712 | 9.38  | 222.4186 | 883.52 | 202 |
| 0.059714 | 0.148264 | -2.77514 | -0.15324 | 0.017894 | 0.145114 | 23.89  | 9.03  | 215.7267 | 883.94 | 200 |
| 0.053768 | 0.137182 | -2.75903 | -0.00213 | -0.19601 | 0.139261 | 23.955 | 9.03  | 216.3137 | 883.78 | 201 |
| 0.039739 | 0.095419 | -2.75907 | -0.21816 | -0.37188 | -0.08077 | 24.077 | 9.08  | 218.6192 | 884.79 | 201 |
| -0.01521 | 0.045838 | -2.78119 | -0.54807 | -0.39928 | -0.19118 | 24.242 | 9.08  | 220.1174 | 884.72 | 201 |
| -0.08122 | 0.018496 | -2.79256 | -0.48342 | -0.13083 | 0.031243 | 24.317 | 8.98  | 218.3667 | 885.7  | 200 |
| -0.10211 | 0.045519 | -2.76177 | 0.079021 | 0.370949 | 0.373123 | 24.445 | 9.16  | 223.9162 | 885.65 | 200 |
| -0.08908 | 0.078907 | -2.71953 | 0.059599 | 0.259472 | 0.416756 | 24.61  | 9.16  | 225.4276 | 884.61 | 201 |
| -0.10565 | 0.091093 | -2.68551 | -0.36502 | -0.06006 | 0.151234 | 24.717 | 9.15  | 226.1606 | 884.67 | 204 |
| -0.1642  | 0.075135 | -2.6811  | -0.4017  | -0.1558  | -0.0134  | 24.78  | 8.96  | 222.0288 | 885.6  | 206 |



|          |          |          |          |          |          |        |          |          |        |     |
|----------|----------|----------|----------|----------|----------|--------|----------|----------|--------|-----|
| 4        |          | 7        | 4        | 4        | 5        |        |          |          |        |     |
| -0.17566 | 0.075458 | -2.68748 | 0.151654 | 0.081215 | -0.04831 | 25.022 | 8.96     | 224.1971 | 885.91 | 206 |
| -0.13957 | 0.07915  | -2.69357 | 0.38392  | -0.01084 | -0.03128 | 25.172 | 9.09     | 228.8135 | 885.47 | 205 |
| -0.10274 | 0.067239 | -2.70847 | 0.249828 | -0.10768 | -0.20448 | 25.182 | 9.09     | 228.9044 | 884.98 | 205 |
| -0.07292 | 0.052223 | -2.73235 | 0.269517 | -0.11274 | -0.16324 | 25.395 | 9.04     | 229.5708 | 885.77 | 204 |
| -0.04297 | 0.047981 | -2.74645 | 0.272443 | 0.03439  | -0.05629 | 25.472 | 9.11     | 232.0499 | 884.96 | 203 |
| 0.007204 | 0.048985 | -2.74437 | 0.459214 | -0.00711 | 0.0935   | 25.55  | 9.11     | 232.7605 | 886.02 | 202 |
| 0.046635 | 0.053751 | -2.73701 | 0.225351 | 0.072436 | 0.054656 | 25.592 | 9.099999 | 232.8872 | 885.73 | 202 |
| 0.060102 | 0.068205 | -2.7408  | 0.060397 | 0.147729 | -0.05203 | 25.755 | 9.099999 | 234.3705 | 886.54 | 203 |
| 0.03425  | 0.086458 | -2.75131 | -0.40387 | 0.108087 | -0.07757 | 25.853 | 9.16     | 236.8135 | 885.93 | 202 |
| -0.02633 | 0.082322 | -2.76644 | -0.49486 | -0.14733 | -0.09114 | 26.173 | 9.07     | 237.3891 | 885.77 | 202 |
| -0.08557 | 0.057393 | -2.76852 | -0.45814 | -0.23911 | 0.02805  | 26.203 | 9.07     | 237.6612 | 886.69 | 201 |
| -0.11857 | 0.030219 | -2.76205 | -0.11919 | -0.17712 | 0.040023 | 26.381 | 9.21     | 242.969  | 886.07 | 201 |
| -0.12605 | 0.018312 | -2.75154 | -0.06491 | -0.04809 | 0.087913 | 26.441 | 9.21     | 243.5216 | 885.52 | 201 |
| -0.13382 | 0.018997 | -2.74457 | -0.09205 | -0.02015 | 0.037894 | 26.506 | 9.16     | 242.795  | 886.55 | 202 |
| -0.15154 | 0.011779 | -2.73417 | -0.15032 | -0.10822 | 0.100151 | 26.563 | 9.2      | 244.3796 | 885.49 | 203 |
| -0.14797 | 0.003899 | -2.72434 | 0.201939 | -0.03957 | 0.055454 | 26.768 | 9.2      | 246.2656 | 886.66 | 203 |
| -0.10692 | 0.001316 | -2.71476 | 0.387645 | -0.01137 | 0.084188 | 26.888 | 9.37     | 251.9406 | 886.11 | 204 |
| -0.06283 | -0.002   | -2.71999 | 0.357581 | -0.03851 | -0.11934 | 26.973 | 9.37     | 252.737  | 885.51 | 204 |
| -0.0258  | -0.00588 | -2.74483 | 0.174269 | 0.000867 | -0.22364 | 27.153 | 9.3      | 252.5229 | 885.9  | 203 |

|          |          |          |          |          |          |        |          |          |        |     |
|----------|----------|----------|----------|----------|----------|--------|----------|----------|--------|-----|
| -0.00123 | -0.0047  | -2.77135 | 0.206728 | -0.00711 | -0.17362 | 27.216 | 9.45     | 257.1912 | 886.47 | 202 |
| 0.016214 | -0.00967 | -2.78885 | 0.144205 | -0.05048 | -0.10258 | 27.406 | 9.45     | 258.9867 | 886.29 | 200 |
| 0.042987 | -0.01274 | -2.7983  | 0.206195 | 0.01683  | -0.06667 | 27.468 | 9.69     | 266.1649 | 886.23 | 199 |
| 0.035712 | -0.00492 | -2.80137 | -0.17107 | 0.072702 | 0.041885 | 27.626 | 9.969999 | 275.4312 | 885.73 | 199 |
| 0.011604 | -0.00193 | -2.79528 | -0.17958 | -0.0151  | 0.082059 | 27.656 | 9.969999 | 275.7303 | 885.68 | 199 |
| -0.02025 | -0.00095 | -2.78768 | -0.34214 | 0.003793 | 0.058913 | 27.788 | 10       | 277.88   | 886.71 | 200 |
| -0.09151 | -0.0049  | -2.78146 | -0.70052 | -0.06671 | 0.060775 | 27.988 | 10       | 279.88   | 887.27 | 200 |
| -0.15086 | -0.01355 | -2.76497 | -0.24237 | -0.1013  | 0.165867 | 28.051 | 10.07    | 282.4736 | 885.84 | 200 |
| -0.13034 | -0.00861 | -2.74416 | 0.318737 | 0.103032 | 0.140592 | 28.361 | 10.29    | 291.8347 | 885.52 | 202 |
| -0.11437 | 0.01646  | -2.73879 | -0.06624 | 0.285546 | 0.040555 | 28.361 | 10.29    | 291.8347 | 885.96 | 202 |
| -0.14691 | 0.058064 | -2.7325  | -0.34853 | 0.318004 | 0.183692 | 28.391 | 10.39    | 294.9825 | 885    | 203 |
| -0.14466 | 0.091069 | -2.7069  | 0.268984 | 0.141078 | 0.273353 | 28.601 | 10.39    | 297.1644 | 886.05 | 203 |
| -0.09876 | 0.095409 | -2.68897 | 0.350929 | -0.00525 | 0.026986 | 28.631 | 10.42    | 298.335  | 885.92 | 205 |
| -0.08315 | 0.100645 | -2.70739 | 0.035122 | 0.105959 | -0.20475 | 28.831 | 10.43    | 300.7073 | 886.05 | 205 |
| -0.0717  | 0.118734 | -2.73364 | 0.220829 | 0.159702 | -0.12786 | 28.946 | 10.43    | 301.9068 | 886.37 | 204 |
| -0.03751 | 0.13324  | -2.74853 | 0.337139 | 0.14412  | -0.09216 | 29.021 | 10.58    | 307.0422 | 886.26 | 203 |
| 0.001353 | 0.149217 | -2.76231 | 0.322772 | 0.155294 | -0.09163 | 29.273 | 10.58    | 309.7083 | 886.19 | 202 |
| 0.017883 | 0.161387 | -2.77932 | -0.02017 | 0.043817 | -0.15628 | 29.348 | 10.44    | 306.3931 | 886.67 | 201 |
| -0.01524 | 0.160074 | -2.80553 | -0.33864 | -0.05915 | -0.19619 | 29.468 | 10.21    | 300.8683 | 886.57 | 200 |
| -0.0494  | 0.15012  | -2.8189  | -0.1840  | -0.0916  | -0.0482  | 29.528 | 10.21    | 301.4809 | 886.36 | 198 |

|          |          |          |          |          |          |        |       |          |        |     |
|----------|----------|----------|----------|----------|----------|--------|-------|----------|--------|-----|
| 8        |          | 4        | 6        |          | 6        |        |       |          |        |     |
| -0.06597 | 0.142705 | -2.81415 | -0.15426 | -0.02482 | 0.081838 | 29.573 | 10.22 | 302.2361 | 886.79 | 198 |
| -0.09438 | 0.142812 | -2.79448 | -0.35221 | 0.000716 | 0.225508 | 29.683 | 10.22 | 303.3603 | 887    | 199 |
| -0.1307  | 0.153539 | -2.76494 | -0.21067 | 0.110863 | 0.255572 | 29.858 | 9.91  | 295.8928 | 887.28 | 200 |
| -0.1285  | 0.172784 | -2.74332 | 0.065763 | 0.110065 | 0.145957 | 29.981 | 9.83  | 294.7132 | 887.59 | 202 |

## A.2 LANDING FLIGHT

| Roll_Speed(rad/s) | Pitch_Speed(rad/s) | Yaw_Speed(rad/s) | Roll(deg) | Pitch(deg)  | Yaw(deg)    | alt(m) | Ground speed(m/s) | horizontal(m) | Heading(deg) |
|-------------------|--------------------|------------------|-----------|-------------|-------------|--------|-------------------|---------------|--------------|
| 0.3239237         | -0.2187901         | -0.3107379       | -5.78783  | 6.869368621 | -19.2414296 | 882.62 | 7.86              | 4.56666       | 340          |
| 0.2361257         | -0.2592304         | -0.1127931       | -4.00218  | 5.075503082 | -19.7362933 | 882.66 | 7.65              | 4.44465       | 340          |
| 0.1297037         | -0.2807809         | -0.03217849      | -2.8487   | 3.025472124 | -19.4019323 | 882.29 | 7.64              | 5.12644       | 340          |
| -0.1368833        | -0.2014966         | 0.04364715       | -2.09002  | 1.223529599 | -18.7887872 | 882.57 | 7.64              | 6.27244       | 342          |
| -0.2512869        | 0.2227809          | 0.1096288        | -2.96255  | 0.40577736  | -17.3302372 | 882.31 | 7.57              | 6.51777       | 343          |
| -0.2608649        | -0.2504506         | 0.06652787       | -4.51146  | -2.28245243 | -15.8175427 | 882.1  | 7.57              | 7.57757       | 345          |
| -0.09298421       | -0.1376434         | 0.02661963       | -5.74928  | -3.58632332 | -14.0837552 | 881.85 | 7.68              | 8.37888       | 346          |
| -0.3569107        | -0.00674437        | 0.001078365      | -7.84074  | 3.77305141  | -13.1309264 | 881.91 | 7.75              | 9.23025       | 347          |
| -0.901525         | -0.03148748        | -0.02605923      | -13.1131  | 3.68624945  | -12.6808738 | 881.34 | 7.81              | 10.47321      | 347          |
| -0.54926          | -0.06953           | -0.04734         | -18.457   | -4.03449    | -12.4956    | 880.7  | 7.81              | 11.72281      | 347          |

|                     |                     |                     |              |                     |                     |        |              |              |     |
|---------------------|---------------------|---------------------|--------------|---------------------|---------------------|--------|--------------|--------------|-----|
| 83                  | 333                 | 363                 |              | 435                 | 652                 |        |              |              |     |
| 0.1108138           | -<br>0.00674<br>437 | -<br>0.23650<br>87  | -<br>16.2324 | -<br>4.32824<br>58  | -<br>12.9974<br>101 | 880.69 | 8.05999<br>9 | 14.7578<br>6 | 345 |
| -<br>0.47051<br>61  | 0.05737<br>485      | -<br>0.27189<br>39  | -<br>17.3391 | -<br>4.85408<br>984 | -<br>14.6888<br>846 | 880.58 | 8.26         | 15.3718<br>6 | 344 |
| 0.01210746          | 0.10845<br>74       | -<br>0.05771<br>976 | -<br>19.5798 | -<br>4.42981<br>804 | -<br>15.3540<br>256 | 880.04 | 8.25         | 15.8482<br>5 | 346 |
| 0.7929786           | -<br>0.09560<br>67  | -<br>0.11093<br>07  | -<br>10.3171 | -<br>3.32323<br>485 | -<br>13.1664<br>498 | 879.55 | 8.25         | 18.4057<br>5 | 346 |
| 0.1297037           | 0.09355<br>831      | -<br>0.14738<br>03  | -<br>9.83726 | -<br>4.15233<br>801 | -<br>15.9070<br>387 | 879.01 | 8.7          | 23.0637      | 344 |
| 0.8637491           | 0.16858<br>58       | 0.18013<br>33       | -<br>5.44764 | -<br>2.88756<br>519 | -<br>15.0140<br>038 | 878.45 | 8.7          | 23.0637      | 346 |
| 0.5490062           | 0.19013<br>62       | 0.24717<br>91       | 0.48583<br>3 | -<br>1.17479<br>553 | -<br>12.6357<br>763 | 878.08 | 8.78         | 24.1537<br>8 | 348 |
| -<br>0.31035<br>11  | 0.18268<br>67       | 0.15379<br>39       | 1.16375<br>7 | -<br>0.22019<br>691 | -<br>10.7986<br>444 | 877.92 | 8.96         | 25.0969<br>6 | 352 |
| -<br>0.03684<br>664 | 0.18987<br>02       | 0.22669<br>29       | 0.05139<br>3 | 0.49269<br>1622     | -<br>8.75476<br>646 | 872.44 | 8.96         | 25.8137<br>6 | 311 |
| 0.5194741           | 0.11058<br>58       | 0.27697<br>73       | 2.40887<br>2 | 1.44019<br>3016     | -<br>6.24742<br>866 | 871.91 | 9.02         | 26.7082<br>2 | 312 |
| -<br>0.15902<br>81  | -<br>0.01728<br>065 | -<br>0.03969<br>025 | 0.92628<br>1 | -<br>0.46357<br>946 | -<br>48.6446<br>783 | 870.96 | 8.88999<br>9 | 51.1441<br>6 | 313 |
| -<br>0.11619<br>32  | 0.04337<br>987      | -<br>0.09316<br>728 | 0.20885      | -<br>0.43119<br>767 | -<br>48.3192<br>612 | 871.08 | 9.08         | 53.8716<br>4 | 314 |
| 0.2517607           | -<br>0.02499<br>624 | -<br>0.01042<br>421 | 0.76858<br>5 | -<br>0.36433<br>722 | -<br>47.5197<br>845 | 870.48 | 9.29         | 55.1175<br>7 | 315 |
| 0.00699019          | -<br>0.28067<br>5   | 0.01006<br>201      | 1.56144<br>8 | -<br>1.59418<br>86  | -<br>46.7459<br>535 | 870.69 | 9.29         | 57.0684<br>7 | 318 |
| -<br>0.56901<br>86  | -<br>0.23411<br>54  | -<br>0.03436<br>915 | -<br>0.25471 | -<br>3.51527<br>655 | -<br>46.5429<br>946 | 870.17 | 9.19         | 56.7298<br>7 | 319 |
| -<br>0.21330<br>33  | -<br>0.02419<br>807 | 0.05848<br>4        | -<br>3.16055 | -<br>4.57882<br>087 | -<br>45.5521<br>157 | 869.32 | 9.46         | 59.3425<br>8 | 319 |
| 0.1772653           | 0.15139<br>82       | 0.25110<br>77       | -<br>3.25567 | -<br>3.85434<br>094 | -<br>43.2645<br>53  | 869.62 | 9.46         | 59.6263<br>8 | 319 |
| -<br>0.25028<br>49  | 0.03406<br>794      | 0.16783<br>26       | -<br>4.02412 | -<br>3.16085<br>747 | -<br>40.9967<br>402 | 868.94 | 9.48         | 60.1316<br>4 | 321 |
| -<br>0.63287<br>17  | -<br>0.09869<br>344 | -<br>0.05299<br>299 | -<br>7.20355 | -<br>3.58291<br>078 | -<br>40.3456<br>597 | 869.05 | 9.48         | 60.7004<br>4 | 323 |

|                     |                     |                     |                   |                     |                     |        |              |              |     |
|---------------------|---------------------|---------------------|-------------------|---------------------|---------------------|--------|--------------|--------------|-----|
| 0.03439<br>385      | 0.05455<br>417      | -<br>0.03011<br>227 | -<br>10.3945      | -<br>4.07159<br>107 | -<br>40.4104<br>612 | 868.24 | 9.46         | 63.8833<br>8 | 325 |
| -<br>0.25533<br>99  | 0.06386<br>609      | 0.12686<br>01       | -<br>11.3728      | -<br>3.50637<br>795 | -<br>39.7179<br>328 | 868.24 | 9.63999<br>9 | 66.5449<br>1 | 325 |
| 0.01843<br>056      | 0.06493<br>031      | 0.20135<br>55       | -11.666           | -<br>2.90758<br>606 | -<br>38.0922<br>338 | 868.08 | 9.63999<br>9 | 66.8341<br>1 | 324 |
| 0.68489<br>81       | 0.10137<br>98       | 0.17448<br>39       | -<br>8.87666      | -<br>2.00107<br>744 | -<br>35.8029<br>58  | 867.49 | 9.75         | 69.0592<br>5 | 323 |
| 0.41059<br>54       | 0.10882<br>94       | 0.00686<br>9356     | -<br>4.92569      | -<br>0.99599<br>431 | -<br>34.1930<br>727 | 867.23 | 9.75         | 69.7417<br>5 | 322 |
| -<br>0.03318<br>409 | 0.06173<br>765      | -<br>0.20384<br>61  | -<br>4.60383      | -<br>0.38838<br>122 | -<br>34.4451<br>226 | 867.2  | 9.76         | 74.9860<br>8 | 322 |
| 0.26559<br>55       | -<br>0.04415<br>219 | -<br>0.27887<br>36  | -<br>3.92235      | -<br>0.59366<br>907 | -<br>35.7205<br>839 | 867.25 | 9.71999<br>9 | 75.2619<br>5 | 329 |
| 0.66840<br>27       | -<br>0.07155<br>584 | -<br>0.29031<br>39  | -<br>0.35929<br>5 | -<br>1.34640<br>727 | -<br>36.9368<br>071 | 866.9  | 9.57         | 74.4833<br>1 | 333 |
| 0.30390<br>74       | -<br>0.06250<br>998 | -<br>0.20836<br>9   | 3.99801<br>1      | -<br>2.00194<br>089 | -<br>37.5538<br>139 | 865.87 | 9.57         | 74.7704<br>1 | 334 |
| -<br>0.11991<br>8   | 0.02555<br>419      | 0.12153<br>9        | 3.68381<br>2      | -<br>2.16195<br>311 | -<br>36.9148<br>285 | 866.02 | 9.58         | 75.4233<br>4 | 335 |
| 0.37042<br>11       | 0.12452<br>66       | 0.51263<br>96       | 4.22325<br>2      | -<br>1.84277<br>895 | -<br>33.7591<br>775 | 864.89 | 9.67         | 77.0989<br>1 | 338 |
| -<br>0.28061<br>51  | 0.11627<br>89       | 0.19523<br>62       | 7.07050<br>5      | -<br>1.01117<br>998 | -<br>26.2021<br>105 | 864.39 | 9.92         | 81.6713<br>6 | 339 |
| -<br>0.31600<br>04  | -<br>0.02818<br>89  | -<br>0.09449<br>755 | -<br>0.46228      | -<br>1.19132<br>364 | -<br>24.5920<br>017 | 864.06 | 9.74         | 82.1471<br>6 | 340 |
| 0.16795<br>34       | 0.03167<br>345      | 0.05209<br>868      | -<br>11.4083      | -<br>1.79396<br>523 | -<br>21.7140<br>863 | 863.74 | 9.74         | 91.8871<br>6 | 339 |
| -<br>0.19627<br>57  | 0.08594<br>865      | 0.07763<br>995      | -<br>11.7917      | -<br>1.15553<br>269 | -<br>20.7395<br>023 | 863.87 | 9.53         | 89.9060<br>2 | 338 |
| -<br>0.01243<br>181 | 0.20354<br>49       | 0.06407<br>115      | -<br>12.6184      | 0.21746<br>997      | -<br>20.2158<br>704 | 863.28 | 9.53         | 90.4778<br>2 | 338 |
| 0.26399<br>92       | -<br>0.04787<br>696 | -<br>0.18096<br>54  | -<br>7.92865      | 1.70679<br>8299     | -<br>19.9677<br>568 | 862.9  | 9.48         | 95.1223<br>2 | 339 |
| 0.27277<br>9        | 0.06253<br>582      | -<br>0.21661<br>67  | -<br>5.05246      | 1.60876<br>9804     | -<br>20.7351<br>764 | 862.96 | 9.42999<br>9 | 96.9781<br>1 | 341 |
| -<br>0.02280<br>795 | 0.10510<br>46       | -<br>0.17591<br>03  | -<br>3.96255      | 2.13235<br>7545     | -<br>21.6766<br>32  | 862.49 | 9.42999<br>9 | 97.4496<br>1 | 343 |
| 0.09452<br>225      | 0.04604<br>041      | -<br>0.03224        | -<br>3.77261      | 2.76154<br>8283     | -<br>21.3272        | 862.7  | 9.28         | 97.3843<br>2 | 344 |

|             |             |             |          |             |             |        |          |          |     |
|-------------|-------------|-------------|----------|-------------|-------------|--------|----------|----------|-----|
|             |             | 071         |          |             | 997         |        |          |          |     |
| 0.4590174   | -0.06543658 | 0.1356399   | -1.81065 | 2.653077632 | -19.7296069 | 862.49 | 9.28     | 98.96192 | 345 |
| 0.3217331   | -0.1678677  | 0.1321812   | 0.754471 | 1.724754797 | -17.7515102 | 861.77 | 9.38     | 100.0283 | 346 |
| -0.07814736 | -0.1268953  | 0.04145649  | 0.785157 | 0.746821838 | -16.3373128 | 862.07 | 9.3      | 100.0122 | 346 |
| 0.08760483  | -0.03351    | 0.07843812  | 0.8612   | 0.257458299 | -15.2828356 | 861.93 | 9.3      | 101.3607 | 346 |
| 0.132036    | -0.01089533 | 0.07763995  | 2.112631 | 0.127549114 | -14.1608009 | 862.02 | 9.349999 | 102.1861 | 346 |
| -0.1542391  | -0.0553265  | -0.02026824 | 2.829407 | -0.66520114 | -13.3899148 | 861.83 | 9.349999 | 103.8691 | 347 |
| -0.551459   | -0.2067117  | -0.1240297  | 0.039765 | -1.9504847  | -13.3375694 | 861.37 | 9.8      | 109.1622 | 348 |
| -0.4724407  | -0.3990694  | -0.2216718  | -3.69441 | -4.23447724 | -13.4977627 | 861.34 | 9.86     | 112.4927 | 350 |
| 0.02029294  | -0.2931796  | -0.1479746  | -4.95314 | -6.95463047 | -13.292512  | 861.15 | 9.86     | 112.8871 | 354 |
| 0.04104522  | 0.0968569   | 0.03241063  | -4.45507 | -7.47367867 | -12.408186  | 861.21 | 10.15    | 117.5269 | 356 |
| -0.4455692  | 0.2458476   | 0.2452545   | -6.91682 | -5.77902421 | -10.6642572 | 860.32 | 10.15    | 118.6434 | 355 |
| -0.2133033  | 0.09047158  | 0.412337    | -10.4803 | -4.07199615 | -8.05635383 | 860.25 | 10.17    | 119.4873 | 353 |
| 0.4241642   | 0.1053707   | 0.2550986   | -9.53377 | -2.79033311 | -4.90715089 | 859.97 | 10.16    | 120.8938 | 352 |
| 0.00406359  | 0.2735173   | -0.01494714 | -7.88369 | -1.03737848 | -3.56905036 | 860.1  | 10.05    | 120.188  | 349 |
| -0.1843033  | 0.3855264   | -0.3033506  | -9.40889 | 1.294386143 | -5.16221623 | 859.8  | 10.05    | 120.8915 | 348 |
| 0.2951276   | 0.2522329   | -0.2802038  | -9.35033 | 3.389559301 | -6.60609451 | 859.93 | 10.15    | 122.9064 | 349 |
| 0.6811733   | 0.0614716   | -0.2118278  | -5.82287 | 4.342923829 | -7.72723541 | 859.07 | 10.15    | 123.3124 | 351 |
| 0.3669624   | -0.1503081  | -0.1673966  | -2.11543 | 3.795675223 | -9.15483997 | 859.07 | 10.46    | 128.1245 | 359 |
| -0.2287344  | -0.1755833  | -0.1806993  | -2.0923  | 2.510134402 | -11.0667027 | 859    | 10.24    | 126.1466 | 298 |

|                     |                     |                     |              |                     |                     |        |              |              |     |
|---------------------|---------------------|---------------------|--------------|---------------------|---------------------|--------|--------------|--------------|-----|
| 0.95520<br>98       | -<br>0.22639<br>98  | 0.24871<br>32       | 2.45812<br>4 | -<br>2.13688<br>162 | -<br>11.4165<br>221 | 858.23 | 10.16        | 130.241      | 298 |
| -<br>0.04143<br>179 | 0.12479<br>27       | 0.31442<br>88       | 5.60851<br>2 | -<br>2.54263<br>944 | -<br>10.0934<br>136 | 858.62 | 10.16        | 130.545<br>8 | 296 |
| -<br>0.41044<br>99  | 0.38871<br>91       | 0.47299<br>75       | 3.26489<br>1 | -<br>1.13370<br>414 | -<br>7.91075<br>379 | 858.41 | 9.91         | 128.126<br>4 | 294 |
| 0.47764<br>13       | 0.48689<br>34       | 0.36418<br>1        | 11.1843<br>3 | 5.25286<br>2168     | 0.75203<br>5754     | 857.81 | 9.9          | 130.076<br>1 | 295 |
| -<br>0.68581<br>67  | 0.11574<br>68       | -<br>0.12509<br>39  | 9.27101<br>9 | 6.40616<br>6621     | -<br>61.1453<br>683 | 857.89 | 9.71         | 127.968<br>1 | 297 |
| -<br>0.13614<br>73  | -<br>0.14232<br>64  | -<br>0.33048<br>82  | 5.99673<br>7 | 6.00764<br>5827     | -<br>62.4549<br>207 | 858.3  | 9.71         | 130.502<br>4 | 299 |
| 0.73065<br>95       | -<br>0.16414<br>29  | -<br>0.27248<br>83  | 8.94429<br>5 | 4.85504<br>0382     | -<br>64.2854<br>062 | 857.66 | 9.59999<br>9 | 129.216      | 301 |
| 0.23845<br>79       | -<br>0.08166<br>593 | -<br>0.17830<br>48  | 12.0941<br>9 | 4.23019<br>8394     | -<br>65.4200<br>346 | 856.99 | 9.59999<br>9 | 129.984      | 304 |
| -<br>0.65202<br>77  | -<br>0.06277<br>603 | -<br>0.01867<br>191 | 8.96822<br>2 | 4.04589<br>6206     | -<br>65.6571<br>818 | 857.48 | 9.91         | 136.361<br>6 | 309 |
| -<br>0.41444<br>07  | -<br>0.30994<br>1   | 0.23886<br>92       | 4.66524<br>8 | 2.48925<br>5247     | -<br>64.1691<br>531 | 857.23 | 9.88999<br>9 | 136.679<br>8 | 312 |
| 0.31454<br>96       | -<br>0.50256<br>47  | 0.37828<br>2        | 4.73505<br>4 | -<br>0.94861<br>356 | -<br>61.5550<br>332 | 857.11 | 9.88999<br>9 | 137.767<br>7 | 311 |
| -<br>0.17392<br>71  | -<br>0.21070<br>26  | 0.22929<br>12       | 5.90341<br>3 | -<br>3.53052<br>239 | -<br>59.3466<br>819 | 856.85 | 9.83         | 138.799<br>6 | 308 |
| -<br>1.16790<br>8   | 0.19396<br>69       | 0.19763<br>07       | 0.16363<br>8 | -<br>3.32623<br>601 | -<br>57.4979<br>763 | 856.71 | 9.83         | 139.684<br>3 | 306 |
| -<br>0.94974<br>31  | 0.30624<br>21       | 0.49082<br>32       | -<br>7.75043 | -<br>0.88986<br>362 | -<br>53.7050<br>014 | 856.95 | 9.77         | 139.417<br>9 | 307 |
| 0.12565<br>07       | 0.10803<br>12       | 0.47964<br>89       | -<br>9.86155 | 0.99330<br>9427     | -<br>49.2310<br>834 | 856.92 | 10.02        | 143.686<br>8 | 308 |
| 0.18145<br>71       | 0.02774<br>776      | -<br>0.09935<br>167 | -<br>7.85595 | 1.32911<br>7126     | -<br>47.2734<br>241 | 856.29 | 10.02        | 146.091<br>6 | 308 |
| -<br>0.67311<br>12  | -<br>0.05446<br>32  | -<br>0.57133<br>3   | -<br>10.1299 | 0.90941<br>6374     | -<br>49.4305<br>472 | 855.95 | 10.01        | 146.946<br>8 | 310 |
| -<br>0.62921<br>21  | -<br>0.09463<br>748 | -<br>0.43537<br>9   | -<br>15.3103 | -<br>0.51132<br>22  | -<br>52.4578<br>499 | 855.61 | 10.01        | 147.247<br>1 | 313 |
| 0.26286<br>98       | -<br>0.07574<br>759 | -<br>0.09722<br>323 | -<br>15.5277 | -<br>0.98741<br>942 | -<br>53.0894<br>442 | 855.93 | 9.8          | 145.824      | 316 |
| 0.77715<br>4        | -<br>0.31253<br>64  | -<br>0.10014<br>98  | -<br>11.6477 | -<br>2.49792<br>696 | -<br>52.3559<br>78  | 855.6  | 9.88999<br>9 | 148.152<br>2 | 315 |

|                     |                     |                      |              |                     |                     |        |              |              |     |
|---------------------|---------------------|----------------------|--------------|---------------------|---------------------|--------|--------------|--------------|-----|
| 0.68430<br>08       | 0.05967<br>434      | -<br>0.00889<br>3008 | -<br>6.24169 | -<br>3.49594<br>037 | -<br>51.7204<br>246 | 855.14 | 9.88999<br>9 | 151.613<br>7 | 311 |
| 0.06891<br>585      | 0.60402<br>26       | 0.13477<br>66        | -<br>4.24154 | -<br>0.85436<br>258 | -<br>51.0075<br>104 | 855.47 | 9.84999<br>9 | 151.69       | 309 |
| 0.05587<br>916      | 0.56943<br>55       | 0.42158<br>38        | -<br>4.44216 | 3.78160<br>2807     | -<br>48.5290<br>21  | 855.15 | 9.84999<br>9 | 152.084      | 309 |
| 0.53424<br>58       | 0.06818<br>81       | 0.32314<br>35        | -<br>1.74698 | 6.07261<br>3511     | -<br>45.1949<br>281 | 854.89 | 9.42         | 145.444<br>8 | 312 |
| 0.72926<br>41       | -<br>0.39208<br>68  | -<br>0.04667<br>28   | 3.86581<br>6 | 4.48211<br>9342     | -<br>43.5591<br>164 | 854.53 | 9.71         | 151.961<br>5 | 313 |
| -<br>0.37379<br>95  | -<br>0.38649<br>97  | -<br>0.55430<br>55   | 4.57840<br>6 | 1.67137<br>8622     | -<br>45.6697<br>955 | 854.19 | 9.71         | 153.612<br>2 | 315 |
| -<br>0.47702<br>88  | -<br>0.11219<br>71  | -<br>0.58064<br>49   | 1.24672<br>6 | 0.03288<br>7525     | -<br>49.2533<br>428 | 854.5  | 9.66         | 153.111      | 317 |
| 0.14075<br>07       | 0.03466<br>518      | -<br>0.14298<br>47   | 0.04315<br>4 | -<br>0.07161<br>961 | -<br>50.7324<br>047 | 853.6  | 9.66         | 153.690<br>6 | 318 |
| 0.02129<br>203      | -<br>0.08638<br>978 | 0.19118<br>03        | 0.58777<br>7 | -<br>0.27228<br>14  | -<br>49.3338<br>319 | 853.91 | 9.75         | 158.242<br>5 | 318 |
| -<br>0.90936<br>79  | -<br>0.24602<br>27  | 0.18346<br>47        | -<br>2.82877 | -<br>1.36207<br>652 | -<br>47.2544<br>077 | 853.88 | 9.67         | 157.524<br>3 | 318 |
| -<br>0.90723<br>95  | -<br>0.20957<br>32  | 0.09885<br>922       | -<br>9.19266 | -<br>2.78839<br>88  | -<br>45.9545<br>383 | 853.17 | 9.67         | 158.201<br>2 | 317 |
| -<br>0.03431<br>344 | -<br>0.09197<br>694 | 0.11535<br>46        | -<br>11.6659 | -<br>3.71471<br>285 | -<br>44.2112<br>111 | 853.05 | 9.9          | 162.162      | 317 |
| 0.18278<br>73       | 0.02136<br>244      | 0.04192<br>347       | -<br>10.5663 | -<br>3.71991<br>817 | -<br>42.5301<br>644 | 852.95 | 9.9          | 163.647      | 316 |
| -<br>0.11386<br>38  | 0.04903<br>214      | -<br>0.06928<br>746  | -<br>10.7636 | -<br>3.19082<br>545 | -<br>41.5841<br>022 | 852.77 | 9.96         | 165.734<br>4 | 316 |
| -<br>0.13035<br>92  | 0.06100<br>462      | -<br>0.10281<br>04   | -<br>12.5097 | -<br>2.83767<br>088 | -<br>41.8082<br>777 | 853.32 | 10.21        | 173.365<br>8 | 316 |
| 0.49859<br>45       | 0.04158<br>261      | -<br>0.10573<br>7    | -<br>10.6956 | -<br>2.51863<br>137 | -<br>42.0068<br>305 | 852.9  | 10.21        | 173.672<br>1 | 319 |
| 0.65131             | -<br>0.03211<br>46  | -<br>0.20577<br>36   | -<br>5.56217 | -<br>2.66593<br>71  | -<br>42.3388<br>079 | 852.61 | 9.88999<br>9 | 168.525<br>6 | 324 |
| -<br>0.01675<br>382 | -<br>0.12204<br>11  | -<br>0.28904<br>88   | -<br>3.77198 | -<br>3.31875<br>833 | -<br>43.0162<br>904 | 852.81 | 9.88999<br>9 | 171.690<br>4 | 329 |
| -<br>0.08938<br>68  | -<br>0.35989<br>42  | -<br>0.19087<br>45   | -<br>4.79753 | -<br>5.16924<br>07  | -<br>43.7800<br>89  | 852.04 | 9.8          | 171.206      | 330 |
| 0.85430<br>99       | -<br>0.46578        | -<br>0.07354         | -<br>1.70377 | -<br>8.51280        | -<br>43.7494        | 851.34 | 10.9         | 190.423      | 327 |



|                     |                     |                    |              |                     |                     |        |              |              |     |
|---------------------|---------------------|--------------------|--------------|---------------------|---------------------|--------|--------------|--------------|-----|
|                     | 4                   | 435                |              | 065                 | 873                 |        |              |              |     |
| 1.09828<br>2        | 0.21079<br>35       | 0.13318<br>03      | 5.88688<br>9 | -<br>9.64473<br>607 | -<br>42.6382<br>128 | 850.95 | 10.9         | 190.75       | 324 |
| -<br>0.29132<br>25  | 0.99938<br>01       | 0.38566<br>64      | 7.33072<br>6 | -<br>4.95337<br>827 | -<br>39.0592<br>262 | 851.18 | 11.2         | 197.008      | 328 |
| -<br>1.23741<br>4   | 0.52819<br>7        | 0.63362<br>96      | 0.18145<br>5 | 0.87812<br>4284     | -<br>33.7259<br>058 | 851.83 | 11.2         | 198.912      | 333 |
| 0.57628<br>25       | -<br>0.52245<br>37  | 0.34469<br>39      | -<br>1.96149 | 0.66475<br>9958     | -<br>29.8375<br>85  | 851.19 | 11.05        | 198.237      | 333 |
| 0.67738<br>34       | -<br>0.38836<br>21  | -<br>0.51253<br>49 | 4.69174      | -<br>3.12871<br>11  | -<br>30.3844<br>16  | 850.58 | 10.61        | 190.873<br>9 | 330 |
| -<br>1.33745        | 0.45928<br>87       | -<br>0.72085<br>58 | 0.94921<br>7 | -<br>2.24976<br>634 | -<br>34.6229<br>916 | 850.33 | 10.61        | 191.722<br>7 | 329 |
| -<br>0.94794<br>59  | 0.68197<br>67       | 0.20182<br>24      | -8.2488      | 1.53844<br>0381     | -<br>35.0020<br>261 | 850.84 | 9.80999<br>9 | 179.032<br>5 | 329 |
| 0.76491<br>54       | 0.32173<br>84       | 0.77011<br>57      | -<br>6.62021 | 5.07920<br>8973     | -<br>30.0986<br>074 | 850.14 | 9.80999<br>9 | 179.621<br>1 | 328 |
| -<br>0.08991<br>891 | 0.07084<br>864      | 0.15366<br>65      | -<br>2.79808 | 6.29921<br>259      | -<br>26.0530<br>785 | 850.6  | 10.06        | 187.085<br>8 | 325 |
| -<br>1.48723<br>9   | 0.22037<br>15       | -<br>0.35503<br>04 | -<br>9.63971 | 6.92555<br>8592     | -<br>27.5168<br>023 | 849.84 | 9.4          | 174.999<br>8 | 324 |
| -<br>0.25460<br>69  | 0.32040<br>81       | -<br>0.15814<br>98 | -<br>15.8085 | 8.22920<br>9463     | -<br>29.7228<br>846 | 849.43 | 9.4          | 175.751<br>8 | 322 |
| 1.18820<br>9        | 0.19243<br>57       | 0.02196<br>936     | -<br>10.7084 | 10.2389<br>0477     | -<br>30.0644<br>362 | 849.47 | 8.92         | 168.677<br>2 | 330 |
| 0.37142<br>02       | -<br>0.04009<br>624 | -<br>0.26430<br>57 | -<br>4.52163 | 10.8253<br>0415     | -<br>30.4366<br>01  | 848.78 | 8.92         | 168.855<br>6 | 336 |
| -<br>0.56402<br>87  | -<br>0.21489<br>43  | -<br>0.43298<br>45 | -<br>6.50585 | 9.72248<br>6446     | -<br>32.8566<br>314 | 848.47 | 8.51         | 162.455<br>9 | 333 |
| 0.11042<br>04       | -<br>0.20052<br>73  | -<br>0.21162<br>68 | -<br>8.59923 | 7.68692<br>7828     | -<br>34.5151<br>666 | 848.12 | 7.79         | 149.645<br>9 | 330 |
| 2.50252             | -<br>1.72981<br>1   | -<br>0.68573<br>66 | -<br>0.08057 | 1.62224<br>1761     | -<br>36.3111<br>716 | 848.75 | 7.79         | 150.580<br>7 | 330 |
| -<br>2.46206<br>4   | 1.27394<br>9        | 0.73606<br>07      | 3.15800<br>7 | 0.16345<br>2311     | -<br>35.2979<br>359 | 848.64 | 7.04         | 136.576      | 336 |
| -<br>0.06251<br>526 | -<br>0.59003<br>16  | 0.78448<br>27      | 0.13827      | -<br>5.08635<br>204 | -<br>27.3566<br>434 | 848.58 | 7.04         | 138.969<br>6 | 322 |
| 1.18980<br>5        | 0.73279<br>32       | 0.03713<br>449     | 4.20962<br>9 | -<br>3.12336<br>827 | -<br>23.7491<br>751 | 848.32 | 6.51         | 128.637<br>6 | 307 |

|                    |                    |                    |              |                     |                     |        |      |              |     |
|--------------------|--------------------|--------------------|--------------|---------------------|---------------------|--------|------|--------------|-----|
| 0.83675<br>02      | 0.38931<br>63      | -<br>0.69877<br>33 | 4.14922<br>1 | -<br>4.00781<br>571 | -<br>30.8181<br>221 | 849.18 | 6.1  | 121.268      | 319 |
| -<br>0.76782<br>67 | -<br>0.69326<br>09 | 0.98455<br>59      | 5.00655<br>3 | -<br>5.52770<br>601 | -<br>27.1172<br>674 | 848.44 | 6.1  | 121.878      | 325 |
| -<br>0.18649<br>68 | 0.94430<br>69      | 0.59451<br>94      | 2.84668<br>4 | -<br>3.91563<br>769 | -<br>22.3845<br>386 | 848.87 | 5.31 | 106.890<br>3 | 339 |
| -<br>1.13844<br>1  | 1.26783            | -<br>2.60931<br>3  | 3.45946<br>5 | -<br>4.94779<br>022 | -<br>45.3721<br>554 | 848.72 | 5.31 | 107.739<br>9 | 337 |
| 1.97307<br>1       | -<br>3.50492<br>9  | 3.84624<br>2       | 11.7609<br>6 | -<br>8.50021<br>277 | -<br>45.9827<br>278 | 848.94 | 4.29 | 87.7305      | 338 |
| 0.50923<br>67      | -<br>0.56342<br>61 | 1.29929<br>9       | 25.5960<br>6 | -<br>13.4424<br>321 | -<br>38.7773<br>653 | 848.7  | 4.04 | 82.7392      | 341 |
| -<br>0.76756<br>07 | 2.21312<br>3       | 1.23837<br>2       | 23.4292<br>4 | -<br>13.2170<br>764 | -<br>29.7890<br>727 | 848.07 | 4.04 | 83.4664      | 343 |
| -<br>3.01306<br>4  | 0.30098<br>61      | 0.09726<br>289     | 3.51325      | -<br>7.00351<br>523 | -<br>18.7908<br>556 | 848.18 | 4.13 | 85.491       | 345 |
| -<br>0.63905<br>61 | 1.61689<br>4       | 0.63815<br>25      | 4.17923<br>2 | -<br>9.21643<br>293 | -<br>21.5803<br>465 | 848.08 | 4.13 | 86.2344      | 346 |
| 1.12675            | 0.01923<br>4       | 0.21432<br>7       | 11.7107<br>9 | -<br>7.67830<br>481 | -<br>22.0124<br>713 | 848.5  | 3.85 | 80.696       | 348 |
| -<br>0.58637<br>73 | 0.19828<br>89      | 0.39391<br>41      | 5.69472<br>3 | -<br>10.1216<br>375 | -<br>17.3895<br>326 | 848.22 | 3.13 | 66.6064      | 349 |
| 0.47624<br>59      | 0.07324<br>314     | 0.43568<br>47      | 8.90809      | -<br>9.17658<br>372 | -<br>15.6197<br>806 | 848.33 | 3.13 | 66.7003      | 350 |
| 0.40760<br>37      | 0.30604<br>12      | 0.09806<br>105     | 8.62396<br>6 | -<br>9.77911<br>186 | -<br>14.7951<br>224 | 848.37 | 2.09 | 44.7051      | 350 |
| -<br>0.13594<br>64 | 0.68623<br>36      | 0.36464<br>8       | 8.82611<br>1 | -<br>10.2897<br>376 | -<br>13.1663<br>982 | 848.16 | 2.09 | 44.7678      | 350 |
| -<br>0.21815<br>74 | 0.16503<br>21      | 0.14568<br>49      | 7.56385<br>6 | -<br>10.7445<br>973 | -<br>11.2951<br>295 | 848.77 | 1.92 | 41.6448      | 351 |
| -<br>0.21123<br>99 | 0.84799<br>5       | 0.23880<br>41      | 5.90497<br>2 | -<br>11.2609<br>583 | -<br>10.1682<br>877 | 848.18 | 1.51 | 32.7821      | 351 |
| -<br>0.48181<br>78 | 0.79771<br>06      | 0.02329<br>963     | 6.47022<br>9 | -<br>10.9354<br>667 | -<br>9.14487<br>623 | 848.26 | 1.51 | 33.069       | 350 |
| 0.17693<br>41      | -<br>0.59402<br>25 | 0.12945<br>55      | 8.64448<br>4 | -<br>12.0772<br>628 | -<br>9.26481<br>922 | 849    | 1.21 | 26.5837      | 351 |
| 0.06918<br>19      | 0.62716<br>94      | 0.26434<br>53      | 9.31367      | -<br>11.4541<br>654 | -<br>8.45684<br>56  | 848.61 | 1.21 | 26.8741      | 352 |
| -<br>0.51800       | -<br>0.63579       | -<br>0.16639       | 7.68055<br>1 | -<br>12.1797        | -<br>8.55038        | 848.26 | 1.03 | 22.9072      | 353 |

|                     |                     |                     |              |                     |                     |        |      |         |     |
|---------------------|---------------------|---------------------|--------------|---------------------|---------------------|--------|------|---------|-----|
| 12                  | 31                  | 75                  |              | 305                 | 096                 |        |      |         |     |
| 0.52786<br>05       | -<br>0.38383<br>92  | -<br>0.25153<br>51  | 8.46615      | -<br>12.1308<br>343 | -<br>9.43203<br>695 | 848.38 | 1.03 | 22.9381 | 355 |
| 0.05933<br>788      | -<br>0.52883<br>9   | 0.03367<br>577      | 8.17319<br>7 | -<br>11.7787<br>002 | -<br>8.87219<br>989 | 848.74 | 1.01 | 22.6644 | 358 |
| 0.06678<br>741      | -<br>0.32477<br>5   | 0.06533<br>63       | 8.21172<br>3 | -<br>11.8802<br>283 | -<br>8.56672<br>171 | 848.87 | 0.39 | 8.7789  | 358 |
| -<br>0.00797<br>4   | -<br>0.33302<br>27  | -<br>0.08046<br>177 | 8.05338<br>6 | -<br>11.2759<br>756 | -<br>7.35014<br>324 | 848.63 | 0.39 | 8.8647  | 359 |
| -<br>0.17638<br>67  | 0.43135<br>3        | 0.43648<br>29       | 6.49881<br>4 | -<br>10.0490<br>151 | -<br>5.97167<br>554 | 847.86 | 1.07 | 24.3425 | 359 |
| -<br>0.24556<br>1   | -<br>0.39182<br>08  | 0.32101<br>51       | 5.73289      | -<br>11.4087<br>413 | -<br>3.98646<br>272 | 848.41 | 0.65 | 14.859  | 0   |
| -<br>0.21150<br>6   | -<br>0.19653<br>65  | -<br>0.12382<br>87  | 4.81293<br>5 | -<br>12.0233<br>131 | -<br>1.87563<br>922 | 848.26 | 0.19 | 4.3833  | 1   |
| 0.03486<br>083      | -<br>0.04648<br>156 | -<br>0.09562<br>69  | 3.50468<br>1 | -<br>11.6545<br>173 | -<br>0.94733<br>014 | 848.1  | 0.19 | 4.4156  | 2   |
| 0.45629<br>17       | 0.13071<br>1        | 0.02755<br>651      | 5.89756<br>9 | -<br>10.8749<br>739 | -<br>0.85364<br>18  | 848.09 | 0.2  | 4.648   | 2   |
| 0.02022<br>781      | -<br>0.16966<br>5   | -<br>0.04214<br>987 | 7.36129<br>9 | -<br>11.9235<br>955 | -<br>0.20732<br>002 | 848.39 | 0.09 | 2.1042  | 3   |
| -<br>0.12583<br>63  | 0.09106<br>882      | 0.08183<br>171      | 6.45419<br>2 | -<br>11.8966<br>321 | 1.52771<br>8622     | 848.43 | 0.09 | 2.13138 | 3   |
| 0.26499<br>83       | 0.00247<br>2541     | 0.09885<br>922      | 6.96019<br>4 | -<br>11.0907<br>727 | 2.13141<br>4457     | 848.2  | 0.06 | 1.42272 | 4   |
| -<br>0.16175<br>37  | -<br>0.00417<br>883 | -<br>0.11558<br>1   | 7.15533<br>2 | -<br>11.1429<br>233 | 2.57261<br>0866     | 848.25 | 0.06 | 1.43124 | 4   |
| 0.05215<br>44       | 0.02428<br>904      | -<br>0.10094<br>8   | 6.87030<br>8 | -<br>11.0996<br>994 | 3.05588<br>014      | 847.59 | 0.03 | 0.71802 | 5   |
| -<br>0.01861<br>62  | -<br>0.02067<br>423 | 0.20554<br>72       | 7.19908<br>3 | -<br>11.1059<br>733 | 3.66059<br>584      | 848.11 | 0.11 | 2.65914 | 6   |
| 0.01889<br>754      | 0.01311<br>473      | 0.03074<br>917      | 6.66374      | -<br>10.9812<br>747 | 3.99266<br>9        | 848.47 | 0.11 | 2.66024 | 6   |
| -<br>0.05533<br>177 | -<br>0.00258<br>25  | -<br>0.01501<br>227 | 6.69296<br>1 | -<br>10.9330<br>603 | 4.38949<br>212      | 848.57 | 0.03 | 0.73452 | 7   |
| -<br>0.02792<br>812 | -<br>0.00072<br>012 | -<br>0.00357<br>191 | 6.41051<br>5 | -<br>10.9462<br>785 | 5.00264<br>7488     | 848.31 | 0.03 | 0.73632 | 7   |
| 0.01650<br>304      | -<br>0.00018<br>801 | 0.01771<br>248      | 6.02667<br>4 | -<br>10.9085<br>893 | 5.62923<br>1268     | 848.27 | 0.01 | 0.24594 | 8   |

|                     |                     |                 |              |                     |                 |        |      |         |    |
|---------------------|---------------------|-----------------|--------------|---------------------|-----------------|--------|------|---------|----|
| -<br>0.02074<br>464 | 7.80E-<br>05        | 0.00813<br>4504 | 5.97867<br>7 | -<br>10.8647<br>867 | 6.26501<br>2739 | 848.53 | 0.04 | 0.98696 | 9  |
| 0.02368<br>652      | 0.00194<br>0432     | 0.01398<br>771  | 5.69302<br>3 | -<br>10.8938<br>586 | 6.89762<br>69   | 848.27 | 0.04 | 0.99216 | 9  |
| -<br>0.02101<br>07  | -<br>0.00072<br>012 | 0.00946<br>4778 | 5.55356<br>8 | -<br>10.8737<br>821 | 7.51983<br>0417 | 847.94 | 0.04 | 0.99576 | 10 |
| 0.01836<br>543      | 0.00140<br>8323     | 0.01292<br>349  | 5.42686<br>4 | -<br>10.8059<br>324 | 8.12181<br>9984 | 847.95 | 0.04 | 1.00256 | 10 |
| -<br>0.01196<br>483 | 0.00034<br>41       | 0.01079<br>505  | 5.27112<br>2 | -<br>10.7473<br>819 | 8.72499<br>5573 | 848.54 | 0.08 | 2.01072 | 11 |
| 0.00798<br>929      | 0.00194<br>0432     | 0.01185<br>927  | 5.16046      | -<br>10.6903<br>554 | 9.32686<br>4818 | 848.29 | 0.09 | 2.28546 | 12 |
| -<br>0.00105<br>658 | 0.00061<br>0157     | 0.01185<br>927  | 4.95413<br>9 | -<br>10.6727<br>656 | 9.92189<br>8677 | 847.99 | 0.09 | 2.29626 | 12 |
| -<br>0.00185<br>474 | 0.00167<br>4375     | 0.01185<br>927  | 4.82423<br>9 | -<br>10.6285<br>906 | 10.5169<br>8983 | 848.32 | 0.05 | 1.2787  | 13 |
| 0.00532<br>874      | 0.00167<br>4375     | 0.01159<br>322  | 4.65099<br>9 | -<br>10.5666<br>481 | 11.0970<br>0074 | 848.49 | 0.05 | 1.2812  | 13 |
| -<br>0.00504<br>74  | 0.00061<br>0157     | 0.01185<br>927  | 4.52990<br>3 | -<br>10.4660<br>711 | 11.6793<br>7796 | 848.31 | 0.08 | 2.06832 | 14 |
| 0.00559<br>479      | 0.00061<br>0157     | 0.01185<br>927  | 4.42446<br>5 | -<br>10.3691<br>152 | 12.2531<br>4362 | 848.26 | 0.07 | 1.80978 | 14 |
| -<br>0.00158<br>869 | 0.00140<br>8323     | 0.01079<br>505  | 4.35844<br>8 | -<br>10.3438<br>133 | 12.8099<br>6693 | 847.94 | 0.07 | 1.82588 | 15 |
| 0.00080<br>581      | 0.00061<br>0157     | 0.01185<br>927  | 4.26151<br>9 | -<br>10.3083<br>473 | 13.3671<br>9703 | 847.93 | 0.08 | 2.09072 | 15 |
| 0.00187<br>003      | 0.00167<br>4375     | 0.01185<br>927  | 4.08947<br>1 | -<br>10.2585<br>744 | 13.9206<br>0551 | 848.27 | 0.08 | 2.09952 | 16 |
| -<br>0.00132<br>263 | 0.00114<br>2266     | 0.01106<br>111  | 4.00611<br>2 | -<br>10.2638<br>456 | 14.4687<br>1985 | 848.51 | 0.04 | 1.05736 | 16 |
| 0.00240<br>214      | 0.00140<br>8323     | 0.01239<br>138  | 3.92279<br>1 | -<br>10.2689<br>278 | 15.0034<br>7855 | 848.23 | 0.04 | 1.06576 | 17 |
| -<br>0.00079<br>052 | 0.00061<br>0157     | 0.01159<br>322  | 3.80120<br>5 | -<br>10.2319<br>662 | 15.5362<br>6054 | 848.36 | 0.04 | 1.06816 | 17 |
| 0.00133<br>792      | 0.00140<br>8323     | 0.01185<br>927  | 3.67907<br>5 | -<br>10.1383<br>736 | 16.0612<br>2739 | 848.18 | 0.08 | 2.13952 | 18 |
| 0.00053<br>975      | 0.00087<br>6213     | 0.01159<br>322  | 3.54234<br>9 | -<br>9.99468<br>724 | 16.5807<br>3396 | 848.05 | 0.08 | 2.14672 | 18 |
| 0.00027<br>37       | 0.00087<br>6213     | 0.01159<br>322  | 3.48026<br>6 | -<br>9.96864        | 17.0908<br>2109 | 847.94 | 0.03 | 0.80802 | 19 |

|                |                 |                |              |                     |                 |        |      |         |    |
|----------------|-----------------|----------------|--------------|---------------------|-----------------|--------|------|---------|----|
|                |                 |                |              | 057                 |                 |        |      |         |    |
| 0.00133<br>792 | 0.00167<br>4375 | 0.01185<br>927 | 3.42924<br>6 | -<br>9.96727<br>12  | 17.5891<br>6259 | 847.84 | 0.08 | 2.17312 | 19 |
| 0.00053<br>975 | 0.00061<br>0157 | 0.01132<br>716 | 3.33742<br>9 | -<br>9.95276<br>964 | 18.0865<br>1861 | 848.02 | 0.08 | 2.17552 | 20 |
| 0.00027<br>37  | 0.00140<br>8323 | 0.01185<br>927 | 3.27146<br>6 | -<br>9.89252<br>886 | 18.5674<br>3646 | 848.31 | 0.01 | 0.27454 | 20 |
| 0.00027<br>37  | 0.00114<br>2266 | 0.01185<br>927 | 3.22857<br>1 | -<br>9.79275<br>399 | 19.0385<br>3955 | 848.26 | 0.01 | 0.27572 | 21 |
| 0.00025<br>613 | 0.00136<br>6466 | 0.01208<br>347 | 3.12936<br>1 | -<br>9.77197<br>854 | 19.5258<br>5734 | 848    | 0.04 | 1.10568 | 21 |
| 0.00052<br>218 | 0.00163<br>2523 | 0.01208<br>347 | 3.01682<br>8 | -<br>9.75255<br>527 | 20.0027<br>1293 | 847.79 | 0.12 | 3.32184 | 22 |
| 0.00025<br>613 | 0.00136<br>6466 | 0.01261<br>558 | 2.90055<br>2 | -<br>9.64772<br>691 | 20.4761<br>1358 | 848.36 | 0.12 | 3.33624 | 22 |
| 0.00025<br>613 | 0.00136<br>6466 | 0.01208<br>347 | 2.81584<br>4 | -<br>9.57621<br>032 | 20.9325<br>1457 | 848.4  | 0.16 | 4.47232 | 22 |
| 0.00052<br>218 | 0.00243<br>0685 | 0.01208<br>347 | 2.78867<br>2 | -<br>9.56412<br>664 | 21.3729<br>816  | 847.82 | 0.16 | 4.49952 | 23 |
| 0.00025<br>613 | 0.00136<br>6466 | 0.01234<br>953 | 2.73270<br>7 | -<br>9.50883<br>048 | 21.8210<br>1741 | 847.93 | 0.04 | 1.12888 | 23 |
| 0.00105<br>429 | 0.00216<br>4632 | 0.01261<br>558 | 2.68225<br>5 | -<br>9.44649<br>268 | 22.2559<br>4967 | 848.36 | 0.04 | 1.13168 | 24 |
| 0.00025<br>613 | 0.00163<br>2523 | 0.01261<br>558 | 2.72977<br>9 | -<br>9.48768<br>261 | 22.6684<br>1626 | 847.87 | 0.04 | 1.13488 | 24 |
| 0.00025<br>613 | 0.00243<br>0685 | 0.01234<br>953 | 2.72173      | -<br>9.51017<br>693 | 23.0828<br>309  | 848.4  | 0.05 | 1.43015 | 24 |
| 0.00105<br>429 | 0.00243<br>0685 | 0.01181<br>742 | 2.60895<br>2 | -<br>9.50620<br>634 | 23.5039<br>6634 | 847.89 | 0.05 | 1.43315 | 25 |
| 0.00105<br>429 | 0.00216<br>4632 | 0.01261<br>558 | 2.56579<br>8 | -<br>9.39569<br>424 | 23.9168<br>34   | 847.83 | 0.06 | 1.72818 | 25 |
| 0.00052<br>218 | 0.00163<br>2523 | 0.01155<br>136 | 2.55832<br>4 | -<br>9.23234<br>397 | 24.3091<br>5539 | 848.38 | 0.06 | 1.73118 | 26 |
| 0.00052<br>218 | 0.00136<br>6466 | 0.01261<br>558 | 2.52368      | -<br>9.19493<br>556 | 24.7019<br>8098 | 848.39 | 0.09 | 2.61027 | 26 |
| 0.00078<br>824 | 0.00136<br>6466 | 0.01208<br>347 | 2.49171<br>6 | -<br>9.15463<br>37  | 25.0892<br>8899 | 848.46 | 0.04 | 1.17132 | 26 |
| 0.00025<br>613 | 0.00136<br>6466 | 0.01261<br>558 | 2.46506<br>8 | -<br>9.11166<br>76  | 25.4680<br>3701 | 847.89 | 0.04 | 1.17412 | 27 |

|                |                 |                |              |                     |                 |        |      |         |    |
|----------------|-----------------|----------------|--------------|---------------------|-----------------|--------|------|---------|----|
| 0.00105<br>429 | 0.00163<br>2523 | 0.01181<br>742 | 2.38409<br>1 | -<br>9.02539<br>734 | 25.8564<br>3937 | 848.39 | 0.06 | 1.76298 | 27 |
| 0.00052<br>218 | 0.00243<br>0685 | 0.01181<br>742 | 2.29300<br>6 | -<br>8.92420<br>154 | 26.2347<br>1757 | 848.5  | 0.06 | 1.76718 | 27 |
| 0.00132<br>035 | 0.00216<br>4632 | 0.01208<br>347 | 2.27697<br>4 | -<br>8.97114<br>97  | 26.5965<br>576  | 848.25 | 0.06 | 1.78398 | 28 |
| 0.00052<br>218 | 0.00163<br>2523 | 0.01261<br>558 | 2.25920<br>4 | -<br>8.97962<br>948 | 26.9513<br>6172 | 847.92 | 0.05 | 1.49165 | 28 |
| 0.00078<br>824 | 0.00136<br>6466 | 0.01181<br>742 | 2.23612<br>8 | -<br>8.90531<br>685 | 27.2971<br>5321 | 848.36 | 0.05 | 1.49365 | 28 |
| 0.00078<br>824 | 0.00189<br>8576 | 0.01208<br>347 | 2.19667<br>1 | -<br>8.84181<br>594 | 27.6492<br>8161 | 848.47 | 0.11 | 3.29373 | 29 |
| 0.00025<br>613 | 0.00136<br>6466 | 0.01261<br>558 | 2.14385<br>7 | -<br>8.78352<br>894 | 27.9935<br>6622 | 848.29 | 0.11 | 3.31573 | 29 |
| 0.00025<br>613 | 0.00243<br>0685 | 0.01208<br>347 | 2.13303<br>7 | -<br>8.76053<br>614 | 28.3241<br>686  | 847.94 | 0.03 | 0.90759 | 29 |
| 0.00132<br>035 | 0.00136<br>6466 | 0.01181<br>742 | 2.14457<br>2 | -<br>8.73487<br>337 | 28.6412<br>8928 | 848.04 | 0.02 | 0.60606 | 30 |

### A.3 TURNING FLIGHT

| Roll (rad)       | Pitch (rad)  | Yaw ()             | Roll_S speed (rad/s) | Pitch_Speed (rad/s)  | Yaw_Speed (rad/s)   | Time (s) | alt (m) | Ground speed (m/s) | Horizontal (m) | heading (deg) |
|------------------|--------------|--------------------|----------------------|----------------------|---------------------|----------|---------|--------------------|----------------|---------------|
| 0.0281<br>4      | 0.1204<br>76 | -<br>0.4557<br>315 | -<br>1.0149<br>97    | -<br>0.0706<br>3115  | 0.2355<br>731       | 0.214    | 923.61  | 7.89               | 1.6884<br>6    | 332           |
| -<br>0.1180<br>5 | 0.1057<br>25 | -<br>0.4287<br>874 | -<br>1.3555<br>47    | -<br>0.1326<br>219   | 0.0080<br>96121     | 0.234    | 924.35  | 8                  | 1.872          | 334           |
| -<br>0.2537<br>8 | 0.0830<br>36 | -<br>0.4036<br>788 | -<br>0.8628<br>131   | -<br>0.2321<br>265   | 0.0493<br>3463      | 0.344    | 923.52  | 7.74               | 2.6625<br>6    | 335           |
| -<br>0.2901<br>2 | 0.0743<br>04 | -<br>0.3807<br>518 | -<br>0.0449<br>6038  | -<br>0.0820<br>7152  | -<br>0.0158<br>4882 | 0.454    | 923.88  | 7.74               | 3.5139<br>6    | 337           |
| -<br>0.2865<br>2 | 0.0658<br>26 | -<br>0.3942<br>295 | 0.0329<br>937        | -<br>0.0086<br>40368 | -<br>0.1150<br>873  | 0.604    | 923.77  | 7.84               | 4.7353<br>6    | 338           |
| -<br>0.2893<br>7 | 0.0596<br>87 | -<br>0.4226<br>471 | 0.0513<br>5149       | -<br>0.0387<br>0457  | -<br>0.1773<br>441  | 0.704    | 924.27  | 7.84               | 5.5193<br>6    | 336           |
| -<br>0.2631<br>4 | 0.0484<br>07 | -<br>0.4443<br>317 | 0.4004<br>155        | 0.0317<br>9997       | -<br>0.1488<br>762  | 0.964    | 923.35  | 7.87               | 7.5866<br>8    | 335           |
| -<br>0.1942<br>9 | 0.0590<br>89 | -<br>0.4686<br>809 | 0.6983<br>97         | 0.1956<br>898        | -<br>0.0222<br>3413 | 0.994    | 923.27  | 7.89               | 7.8426<br>6    | 333           |

|          |          |            |             |              |             |       |        |      |          |     |
|----------|----------|------------|-------------|--------------|-------------|-------|--------|------|----------|-----|
| -0.12121 | 0.099453 | -0.4925432 | 0.5206723   | 0.3771392    | -0.08129832 | 1.214 | 923.47 | 7.89 | 9.57846  | 332 |
| -0.07291 | 0.127795 | -0.5155786 | 0.4025439   | 0.1565797    | -0.04325247 | 1.364 | 923.98 | 7.95 | 10.8438  | 331 |
| -0.01864 | 0.127542 | -0.5417443 | 0.5392962   | -0.1089431   | -0.1704267  | 1.444 | 923.85 | 7.93 | 11.45092 | 329 |
| 0.045194 | 0.102121 | -0.5739414 | 0.4682595   | -0.2600622   | -0.195968   | 1.504 | 923.98 | 7.93 | 11.92672 | 328 |
| 0.091509 | 0.079808 | -0.614001  | 0.3961586   | -0.1398054   | -0.200757   | 1.594 | 923.7  | 8.01 | 12.76794 | 325 |
| 0.109069 | 0.083652 | -0.6421301 | -0.01276774 | 0.1246531    | -0.1116286  | 1.744 | 924.88 | 8.01 | 13.96944 | 323 |
| 0.094517 | 0.09807  | -0.65079   | -0.1567034  | 0.09272654   | 0.1522979   | 1.894 | 924.05 | 7.96 | 15.07624 | 322 |
| 0.057856 | 0.106256 | -0.637468  | -0.4094556  | 0.0911302    | 0.2251969   | 1.934 | 924.65 | 7.85 | 15.1819  | 322 |
| -0.00607 | 0.109376 | -0.6126323 | -0.6890792  | -0.01422752  | 0.3497106   | 2.024 | 923.46 | 7.85 | 15.8884  | 324 |
| -0.09229 | 0.10313  | -0.5915303 | -0.6826939  | -0.0945761   | 0.2331786   | 2.295 | 924.95 | 7.88 | 18.0846  | 325 |
| -0.16097 | 0.079951 | -0.5803589 | -0.4906023  | -0.162154    | 0.0807291   | 2.325 | 924.24 | 7.88 | 18.321   | 326 |
| -0.21597 | 0.062653 | -0.6027073 | -0.2884006  | -0.0291266   | -0.1422249  | 2.445 | 923.72 | 7.87 | 19.24215 | 326 |
| -0.2386  | 0.058445 | -0.6107597 | -0.4097216  | -0.007310097 | -0.08236254 | 2.615 | 924.24 | 7.87 | 20.58005 | 325 |
| -0.26547 | 0.05381  | -0.6108809 | 0.01037904  | -0.09404399  | 0.1876832   | 2.645 | 924.81 | 7.87 | 20.81615 | 324 |
| -0.2136  | 0.047259 | -0.5982869 | 0.751874    | -0.05998896  | 0.1467107   | 2.755 | 923.59 | 7.93 | 21.84715 | 325 |
| -0.11697 | 0.041375 | -0.5995344 | 0.7247364   | -0.05573208  | 0.02671996  | 2.855 | 924.12 | 7.93 | 22.64015 | 325 |
| -0.0627  | 0.042498 | -0.6308725 | 0.3331036   | 0.1007082    | -0.1808028  | 3.115 | 924.17 | 8.02 | 24.9823  | 324 |
| -0.02549 | 0.054694 | -0.651653  | 0.4216999   | 0.148332     | 0.004637408 | 3.325 | 923.79 | 8.16 | 27.132   | 322 |
| 0.068107 | 0.074529 | -0.6473138 | 1.002764    | 0.1547173    | 0.153096    | 3.355 | 923.13 | 8.16 | 27.3768  | 322 |
| 0.179975 | 0.095891 | -0.6541    | 0.7851309   | 0.1613687    | -0.1842     | 3.385 | 924.02 | 8.09 | 27.38465 | 322 |

|                  |              |                    |                     |                     |                     |       |        |      |              |     |
|------------------|--------------|--------------------|---------------------|---------------------|---------------------|-------|--------|------|--------------|-----|
|                  |              | 491                |                     |                     | 615                 |       |        |      |              |     |
| 0.2269<br>72     | 0.1162<br>32 | -<br>0.7139<br>521 | -<br>0.0587<br>9522 | 0.0597<br>3573      | -<br>0.5181<br>605  | 3.535 | 923.45 | 8.01 | 28.315<br>35 | 320 |
| 0.1806<br>76     | 0.1292<br>59 | -<br>0.7647<br>652 | -<br>0.4847<br>491  | 0.0419<br>1006      | -<br>0.4665<br>458  | 3.605 | 924.08 | 8.01 | 28.876<br>05 | 317 |
| 0.1007<br>61     | 0.1302<br>32 | -<br>0.7890<br>325 | -<br>0.6667<br>306  | -<br>0.0589<br>2474 | -<br>0.1220<br>047  | 3.805 | 923.76 | 8.01 | 30.478<br>05 | 314 |
| 0.0188<br>1      | 0.0935<br>78 | -<br>0.7746<br>029 | -<br>0.7406<br>939  | -<br>0.4396<br>493  | 0.2073<br>712       | 3.925 | 924.35 | 8.01 | 31.439<br>25 | 315 |
| -<br>0.0736<br>3 | 0.0347<br>43 | -<br>0.7369<br>334 | -<br>0.7526<br>664  | -<br>0.4699<br>795  | 0.2028<br>483       | 3.975 | 924.17 | 7.99 | 31.760<br>25 | 317 |
| -<br>0.1632<br>3 | 0.0045<br>24 | -<br>0.6856<br>382 | -<br>0.6888<br>131  | -<br>0.0879<br>2473 | 0.4143<br>619       | 4.205 | 923.87 | 8.02 | 33.724<br>1  | 320 |
| -<br>0.2199<br>4 | 0.0389<br>52 | -<br>0.6247<br>487 | -<br>0.2546<br>116  | 0.3082<br>31        | 0.5064<br>169       | 4.385 | 923.33 | 8.02 | 35.167<br>7  | 323 |
| -<br>0.2289<br>5 | 0.0869<br>28 | -<br>0.5604<br>17  | -<br>0.1096<br>117  | 0.1970<br>201       | 0.3893<br>527       | 4.435 | 923.63 | 7.96 | 35.302<br>6  | 327 |
| -<br>0.2388<br>8 | 0.1004<br>4  | -<br>0.5216<br>592 | -<br>0.0949<br>787  | -<br>0.0522<br>7337 | 0.1640<br>043       | 4.455 | 923.12 | 7.96 | 35.461<br>8  | 329 |
| -<br>0.2069<br>9 | 0.1190<br>11 | -<br>0.5094<br>005 | 0.5653<br>695       | 0.3098<br>273       | -<br>0.0467<br>1118 | 4.635 | 923.8  | 7.84 | 36.338<br>4  | 330 |
| -<br>0.0958<br>1 | 0.1686<br>86 | -<br>0.5154<br>411 | 0.7124<br>979       | 0.3228<br>64        | -<br>0.1214<br>726  | 4.715 | 924.17 | 7.86 | 37.059<br>9  | 330 |
| -<br>0.0111<br>5 | 0.1840<br>97 | -<br>0.5297<br>822 | 0.7510<br>759       | -<br>0.0919<br>1556 | -<br>0.2329<br>496  | 4.835 | 923.73 | 7.86 | 38.003<br>1  | 329 |
| 0.0950<br>12     | 0.1562<br>12 | -<br>0.5633<br>965 | 0.9474<br>244       | -<br>0.1829<br>063  | -<br>0.3710<br>321  | 4.985 | 924.71 | 7.52 | 37.487<br>2  | 328 |
| 0.2057<br>03     | 0.1486<br>33 | -<br>0.5888<br>592 | 0.8332<br>868       | 0.0485<br>6143      | -<br>0.2002<br>248  | 5.075 | 923.84 | 7.55 | 38.316<br>25 | 326 |
| 0.3135           | 0.1585<br>19 | -<br>0.5776<br>109 | 0.6316<br>172       | 0.1794<br>604       | 0.2294<br>538       | 5.245 | 924.52 | 7.55 | 39.599<br>75 | 326 |
| 0.3755<br>83     | 0.1503<br>22 | -<br>0.5149<br>143 | 0.2801<br>587       | 0.1238<br>55        | 0.6218<br>847       | 5.565 | 924.51 | 7.29 | 40.568<br>85 | 329 |
| 0.4254           | 0.1174<br>25 | -<br>0.4138<br>428 | 0.3921<br>678       | 0.1501<br>944       | 0.9086<br>919       | 5.605 | 924.35 | 7.19 | 40.299<br>95 | 335 |
| 0.5102<br>23     | 0.0786<br>68 | -<br>0.2992<br>465 | 0.4365<br>99        | 0.1847<br>815       | 0.6905<br>269       | 5.665 | 924.23 | 7.19 | 40.731<br>35 | 342 |
| 0.4854<br>82     | 0.0718<br>53 | -<br>0.2455<br>837 | -<br>0.7457<br>489  | 0.2084<br>604       | 0.1562<br>887       | 5.745 | 923.75 | 7.07 | 40.617<br>15 | 345 |



|                  |                  |                     |                     |                      |                     |       |        |      |              |     |
|------------------|------------------|---------------------|---------------------|----------------------|---------------------|-------|--------|------|--------------|-----|
| 0.3170<br>02     | 0.0627<br>54     | -<br>0.2281<br>255  | -<br>1.7469<br>13   | -<br>0.0791<br>4492  | 0.0474<br>7224      | 5.895 | 925.19 | 7.07 | 41.677<br>65 | 346 |
| 0.0934<br>84     | 0.0057<br>7      | -<br>0.2022<br>291  | -<br>1.1932<br>53   | -<br>0.3771<br>264   | 0.1517<br>658       | 6.195 | 924.66 | 7.15 | 44.294<br>25 | 348 |
| 0.0080<br>36     | -<br>0.0404<br>8 | -<br>0.1727<br>907  | -<br>0.3631<br>62   | -<br>0.1738<br>604   | 0.1719<br>859       | 6.235 | 925.13 | 7.32 | 45.640<br>2  | 349 |
| -<br>0.1189<br>1 | -<br>0.0435<br>8 | -<br>0.1362<br>073  | -<br>0.7486<br>755  | 0.0405<br>7978       | 0.2185<br>455       | 6.425 | 924.67 | 7.31 | 46.966<br>75 | 351 |
| -<br>0.1538      | -<br>0.0471<br>4 | -<br>0.1158<br>141  | 0.1630<br>946       | -<br>0.0924<br>4766  | 0.3547<br>656       | 6.455 | 924.72 | 7.31 | 47.186<br>05 | 353 |
| -<br>0.0874<br>9 | -<br>0.0658<br>2 | -<br>0.0883<br>9322 | 0.5712<br>227       | -<br>0.1874<br>292   | 0.1749<br>125       | 6.595 | 924.65 | 7.31 | 48.209<br>45 | 354 |
| -<br>0.0649<br>4 | -<br>0.0740<br>9 | -<br>0.0906<br>3776 | -<br>0.0361<br>8057 | 0.0605<br>339        | -<br>0.0416<br>5614 | 6.745 | 924.14 | 7.56 | 50.992<br>2  | 355 |
| -<br>0.0625<br>2 | -<br>0.0566<br>2 | -<br>0.1049<br>792  | 0.2022<br>046       | 0.2113<br>87         | 0.1068<br>025       | 6.915 | 924.58 | 7.56 | 52.277<br>4  | 354 |
| 0.0116<br>28     | -<br>0.0245<br>5 | -<br>0.0942<br>1061 | 0.7917<br>823       | 0.1451<br>394        | 0.2033<br>804       | 6.925 | 924.38 | 7.52 | 52.076       | 354 |
| 0.1079<br>16     | -<br>0.0187<br>2 | -<br>0.0823<br>6877 | 0.6888<br>19        | -<br>0.0126<br>3119  | 0.0280<br>5024      | 7.197 | 924.79 | 7.52 | 54.121<br>44 | 355 |
| 0.1609<br>93     | -<br>0.0337<br>2 | -<br>0.0942<br>2337 | 0.1050<br>946       | -<br>0.1036<br>22    | -<br>0.1597<br>845  | 7.387 | 924.78 | 7.64 | 56.436<br>68 | 354 |
| 0.1890<br>46     | -<br>0.0426<br>6 | -<br>0.0928<br>267  | 0.3599<br>751       | -<br>0.0083<br>74316 | 0.1507<br>015       | 7.457 | 923.88 | 7.82 | 58.313<br>74 | 354 |
| 0.2531<br>78     | -<br>0.0469<br>4 | -<br>0.0561<br>9285 | 0.7247<br>364       | 0.0887<br>3571       | 0.3507<br>748       | 7.467 | 924.55 | 7.82 | 58.391<br>94 | 356 |
| 0.3522<br>55     | -<br>0.0488<br>7 | 0.0138<br>524       | 0.6284<br>245       | 0.2457<br>081        | 0.3858<br>94        | 7.727 | 924.82 | 7.89 | 60.966<br>03 | 0   |
| 0.3910<br>73     | -<br>0.0456<br>7 | 0.0771<br>2423      | -<br>0.0300<br>613  | 0.2265<br>521        | 0.3098<br>024       | 7.747 | 924.72 | 8.13 | 62.983<br>11 | 3   |
| 0.3394<br>56     | -<br>0.0498<br>8 | 0.1356<br>741       | -<br>0.5057<br>674  | 0.1648<br>274        | 0.2414<br>263       | 7.977 | 923.7  | 8.13 | 64.853<br>01 | 6   |
| 0.2753<br>42     | -<br>0.0515<br>3 | 0.1701<br>422       | -<br>0.6648<br>682  | 0.0791<br>5774       | 0.3457<br>198       | 7.997 | 924.19 | 8.2  | 65.575<br>4  | 9   |
| 0.1597<br>58     | -<br>0.0663<br>8 | 0.2277<br>133       | -<br>0.7920<br>424  | -<br>0.0413<br>6512  | 0.3425<br>271       | 8.197 | 924.56 | 8.42 | 69.018<br>74 | 13  |
| 0.0340<br>3      | -<br>0.0928<br>3 | 0.2875<br>325       | -<br>0.5757<br>399  | -<br>0.0921<br>816   | 0.3018<br>207       | 8.347 | 924.17 | 8.69 | 72.535<br>43 | 16  |
| -<br>0.0181      | -<br>0.1073      | 0.3209<br>488       | -<br>0.3256         | -<br>0.0860          | 0.2243<br>987       | 8.497 | 924.36 | 8.69 | 73.838<br>93 | 18  |

|          |          |           |            |             |            |        |        |          |             |    |
|----------|----------|-----------|------------|-------------|------------|--------|--------|----------|-------------|----|
| 5        |          |           | 483        | 6233        |            |        |        |          |             |    |
| -0.09207 | -0.1344  | 0.3402644 | -0.7321801 | -0.1823742  | 0.1459126  | 8.577  | 924.18 | 8.95     | 76.76415    | 19 |
| -0.16036 | -0.14278 | 0.3702455 | -0.0678411 | 0.04004767  | 0.4300591  | 8.757  | 924.24 | 9.08     | 79.51356    | 21 |
| -0.12498 | -0.10941 | 0.4270379 | 0.5757457  | 0.2462402   | 0.6048572  | 8.817  | 924.53 | 9.08     | 80.05836    | 24 |
| -0.08568 | -0.09122 | 0.5059074 | 0.08886523 | -0.0320532  | 0.4814077  | 9.077  | 924.53 | 9.26     | 84.05302    | 28 |
| -0.03461 | -0.09464 | 0.542439  | 0.7875254  | 0.07064398  | 0.02751813 | 9.287  | 923.33 | 9.429999 | 87.57640071 | 31 |
| 0.083322 | -0.08978 | 0.5227079 | 0.6635438  | -0.05945685 | -0.2276285 | 9.327  | 923.78 | 9.429999 | 87.95360067 | 29 |
| 0.063464 | -0.11018 | 0.4703385 | -0.6616756 | -0.1991356  | -0.1746836 | 9.397  | 923.53 | 9.58     | 90.02326    | 26 |
| 0.027154 | -0.11866 | 0.5089482 | 0.5009843  | 0.04031373  | 0.7799213  | 9.597  | 923.6  | 9.84     | 94.43448    | 29 |
| 0.1662   | -0.11944 | 0.6360769 | 1.640497   | 0.119332    | 1.088545   | 9.657  | 924.38 | 9.84     | 95.02488    | 36 |
| 0.334844 | -0.13126 | 0.7332773 | 0.5291861  | 0.2603411   | 0.468105   | 9.787  | 923.42 | 9.929999 | 97.18490021 | 42 |
| 0.324591 | -0.1151  | 0.7680477 | -0.3006391 | 0.2989191   | 0.2408941  | 9.987  | 923.62 | 10.28    | 102.66636   | 44 |
| 0.304609 | -0.09814 | 0.8025115 | 0.1745349  | 0.2289466   | 0.245151   | 10.197 | 923.18 | 10.28    | 104.82516   | 45 |
| 0.349225 | -0.09368 | 0.8412493 | 0.2955899  | 0.1714788   | 0.1403254  | 10.267 | 922.91 | 10.74    | 110.26758   | 48 |
| 0.281493 | -0.08258 | 0.8531324 | -0.8580241 | 0.1211944   | 0.03869243 | 10.357 | 923.42 | 11.12    | 115.16984   | 48 |
| 0.170515 | -0.08207 | 0.8803326 | -0.7308498 | 0.1360935   | 0.4226096  | 10.497 | 923.93 | 11.24    | 117.98628   | 50 |
| 0.135461 | -0.0769  | 0.9636254 | 0.07210377 | 0.1039008   | 0.7102149  | 10.667 | 923.24 | 11.24    | 119.89708   | 55 |
| 0.111275 | -0.07804 | 1.037213  | -0.3589051 | 0.05920362  | 0.5742609  | 10.817 | 922.8  | 11.55    | 124.93635   | 59 |
| 0.042884 | -0.07583 | 1.090022  | -0.5007124 | 0.1709467   | 0.4811417  | 10.867 | 923.26 | 11.84    | 128.66528   | 62 |
| 0.049641 | -0.05282 | 1.163938  | 0.52892    | 0.2728457   | 0.5303618  | 11.147 | 922.32 | 11.84    | 131.98048   | 66 |
| 0.153089 | -0.0325  | 1.203956  | 0.5866539  | 0.1810568   | 0.1584171  | 11.267 | 923.42 | 11.81    | 133.06327   | 68 |

|          |          |          |              |             |            |        |        |       |           |     |
|----------|----------|----------|--------------|-------------|------------|--------|--------|-------|-----------|-----|
|          | 7        |          |              |             |            |        |        |       |           |     |
| 0.17345  | -0.01486 | 1.184818 | -0.1670796   | 0.1331669   | -0.1467478 | 11.297 | 923.03 | 12.33 | 139.29201 | 67  |
| 0.136287 | -0.00636 | 1.172025 | 0.02820471   | 0.1571118   | 0.1698575  | 11.547 | 922.71 | 12.33 | 142.37451 | 67  |
| 0.216019 | 0.002302 | 1.236995 | 0.6912135    | 0.2459742   | 0.5314261  | 11.577 | 923.79 | 12.33 | 142.74441 | 70  |
| 0.259151 | 0.011314 | 1.288352 | -0.04096955  | 0.177332    | 0.4037197  | 11.757 | 922.36 | 12.63 | 148.49091 | 73  |
| 0.195581 | 0.019636 | 1.322723 | -0.4235565   | 0.1124146   | 0.3252335  | 11.797 | 923.08 | 12.63 | 148.99611 | 75  |
| 0.18807  | 0.014595 | 1.377421 | 0.1995441    | 0.07144215  | 0.4013252  | 11.987 | 923.43 | 12.53 | 150.19711 | 78  |
| 0.176731 | 0.020099 | 1.404884 | -0.4381895   | 0.1669559   | 0.3039491  | 12.037 | 922.5  | 12.7  | 152.8699  | 80  |
| 0.097684 | 0.039898 | 1.433959 | -0.547272    | 0.3095613   | 0.3619491  | 12.216 | 922.94 | 12.7  | 155.1432  | 82  |
| 0.066436 | 0.089151 | 1.489627 | -0.1024282   | 0.4266254   | 0.4625179  | 12.316 | 922.87 | 12.83 | 158.01428 | 85  |
| 0.053159 | 0.12139  | 1.529291 | -0.2365199   | 0.2539558   | 0.2730868  | 12.486 | 923.9  | 12.78 | 159.57108 | 88  |
| 0.02068  | 0.131923 | 1.543439 | -0.31474     | 0.09405681  | 0.05784838 | 12.576 | 923.38 | 12.78 | 160.72128 | 88  |
| -0.00948 | 0.137579 | 1.541948 | -0.3115474   | 0.02647888  | 0.1086649  | 12.776 | 924.53 | 12.71 | 162.38296 | 88  |
| -0.04176 | 0.124184 | 1.553253 | -0.2532814   | -0.1807779  | 0.1791694  | 12.876 | 923.47 | 12.59 | 162.10884 | 89  |
| -0.0485  | 0.075216 | 1.58794  | 0.126645     | -0.3279062  | 0.2526006  | 12.976 | 924.79 | 12.59 | 163.36784 | 91  |
| 0.011751 | 0.041861 | 1.626635 | 0.3437458    | 0.06824949  | 0.1855547  | 13.146 | 924.51 | 12.5  | 164.325   | 93  |
| 0.042176 | 0.073313 | 1.65844  | -0.002391596 | 0.3603777   | 0.2486097  | 13.296 | 923.63 | 12.42 | 165.13632 | 95  |
| 0.022739 | 0.099787 | 1.697128 | -0.3618318   | 0.1709467   | 0.409839   | 13.486 | 923.68 | 12.42 | 167.49612 | 97  |
| -0.00169 | 0.102729 | 1.747699 | -0.05799707  | -0.04695227 | 0.3819032  | 13.706 | 924.04 | 12.25 | 167.8985  | 100 |
| 0.004312 | 0.090072 | 1.780655 | -0.005584254 | -0.0567963  | 0.1546924  | 13.796 | 924.46 | 12.35 | 170.3806  | 102 |
| -0.01908 | 0.086741 | 1.79328  | -0.377529    | 0.07889169  | 0.04374747 | 13.906 | 923.99 | 12.35 | 171.7391  | 102 |

|          |          |          |            |              |             |        |        |       |           |     |
|----------|----------|----------|------------|--------------|-------------|--------|--------|-------|-----------|-----|
| -0.06312 | 0.092477 | 1.809793 | -0.2868043 | 0.03313025   | 0.1645364   | 13.936 | 924.04 | 12.36 | 172.24896 | 103 |
| -0.09025 | 0.086037 | 1.833644 | -0.2777584 | -0.1302274   | 0.1839584   | 14.176 | 924.12 | 12.25 | 173.656   | 105 |
| -0.1238  | 0.065252 | 1.853004 | -0.3064923 | -0.1485852   | 0.09296762  | 14.256 | 924.08 | 12.23 | 174.35088 | 107 |
| -0.13899 | 0.05794  | 1.884581 | 0.0111772  | 0.06691922   | 0.2084354   | 14.436 | 924.08 | 12.23 | 176.55228 | 108 |
| -0.10857 | 0.084767 | 1.918038 | 0.2697825  | 0.2800292    | 0.3292243   | 14.456 | 923.62 | 12.15 | 175.6404  | 110 |
| -0.0798  | 0.111509 | 1.946246 | 0.0548102  | 0.03206603   | 0.1163805   | 14.606 | 924.16 | 12.15 | 177.4629  | 111 |
| -0.10921 | 0.100544 | 1.945965 | -0.3487951 | -0.08952106  | -0.07039007 | 14.776 | 925.23 | 11.95 | 176.5732  | 111 |
| -0.17008 | 0.094863 | 1.95156  | -0.3150061 | -0.007044037 | 0.02938051  | 14.936 | 924.44 | 12.05 | 179.9788  | 112 |
| -0.15903 | 0.091391 | 1.977606 | 0.2979844  | -0.08473206  | 0.1882153   | 15.046 | 925.62 | 12.05 | 181.3043  | 113 |
| -0.07291 | 0.075907 | 2.016352 | 0.5877181  | -0.132888    | 0.2273254   | 15.166 | 925.26 | 11.92 | 180.77872 | 115 |
| 0.003502 | 0.065819 | 2.044145 | 0.1859753  | 0.01450641   | 0.1230318   | 15.366 | 925.16 | 11.95 | 183.6237  | 117 |
| 0.025875 | 0.06264  | 2.065435 | 0.2155074  | -0.03391558  | 0.1629401   | 15.456 | 924.83 | 11.94 | 184.54464 | 118 |
| 0.073074 | 0.051085 | 2.103502 | 0.4475072  | -0.0562642   | 0.2794721   | 15.576 | 926.07 | 11.94 | 185.97744 | 120 |
| 0.134537 | 0.035219 | 2.150787 | 0.4879475  | -0.03604402  | 0.3983986   | 15.676 | 925.37 | 12.08 | 189.36608 | 123 |
| 0.201188 | 0.021647 | 2.20899  | 0.5169476  | 0.04191006   | 0.5090774   | 15.966 | 925.77 | 12.08 | 192.86928 | 127 |
| 0.261849 | 0.007821 | 2.280369 | 0.4179751  | 0.02860731   | 0.448949    | 16.036 | 924.62 | 12.08 | 193.71488 | 131 |
| 0.304062 | -0.01591 | 2.334972 | 0.2474339  | -0.02087889  | 0.2709583   | 16.116 | 925.54 | 12.1  | 195.0036  | 134 |
| 0.296539 | -0.0343  | 2.375643 | -0.2993088 | 0.0576073    | 0.3185821   | 16.386 | 925.29 | 12.1  | 198.2706  | 136 |
| 0.257196 | -0.03196 | 2.451257 | -0.0949787 | 0.3329741    | 0.6173618   | 16.416 | 923.48 | 12.27 | 201.42432 | 141 |
| 0.260557 | -0.00531 | 2.56334  | 0.08753495 | 0.385919     | 0.720325    | 16.586 | 924.37 | 12.29 | 203.84194 | 147 |
| 0.228203 | -0.00574 | 2.650241 | -0.4778317 | 0.02541466   | 0.3643436   | 16.736 | 925    | 12.45 | 208.3632  | 152 |

|              |                  |                   |                     |                      |                |        |        |       |               |     |
|--------------|------------------|-------------------|---------------------|----------------------|----------------|--------|--------|-------|---------------|-----|
| 0.1475<br>39 | -<br>0.0290<br>4 | 2.6860<br>48      | -<br>0.4054<br>647  | -<br>0.0344<br>4769  | 0.0905<br>7313 | 16.806 | 925.24 | 12.45 | 209.23<br>47  | 154 |
| 0.1199<br>45 | -<br>0.0302      | 2.7170<br>01      | -<br>0.0335<br>2002 | 0.1946<br>256        | 0.1953<br>988  | 16.996 | 924.97 | 12.81 | 217.71<br>876 | 156 |
| 0.1104<br>25 | -<br>0.0167<br>7 | 2.7689<br>77      | -<br>0.0923<br>1815 | 0.1709<br>467        | 0.4199<br>491  | 17.106 | 924.23 | 12.84 | 219.64<br>104 | 160 |
| 0.1271       | -<br>0.0135<br>5 | 2.8394<br>56      | 0.2019<br>386       | 0.0610<br>6601       | 0.3781<br>784  | 17.298 | 924.74 | 12.84 | 222.10<br>632 | 163 |
| 0.1217       | -<br>0.0260<br>9 | 2.8965<br>39      | -<br>0.2351<br>896  | -<br>0.0019<br>88997 | 0.3239<br>033  | 17.408 | 924.05 | 12.75 | 221.95<br>2   | 166 |
| 0.1080<br>75 | -<br>0.0302<br>1 | 2.9462<br>98      | 0.0633<br>2395      | 0.1023<br>045        | 0.3968<br>023  | 17.458 | 923.72 | 12.78 | 223.11<br>324 | 170 |
| 0.1497<br>78 | -<br>0.0274<br>7 | 3.0274<br>5       | 0.4288<br>833       | 0.1571<br>118        | 0.5000<br>316  | 17.618 | 924.21 | 12.78 | 225.15<br>804 | 177 |
| 0.1969<br>64 | -<br>0.0218<br>4 | 3.0987<br>41      | 0.2351<br>954       | 0.2100<br>568        | 0.3590<br>225  | 17.818 | 923.05 | 12.78 | 227.71<br>404 | 178 |
| 0.2333<br>37 | -<br>0.0088<br>3 | -<br>3.1261<br>66 | 0.2181<br>679       | 0.2491<br>668        | 0.2044<br>446  | 17.988 | 924.26 | 12.49 | 224.67<br>012 | 181 |
| 0.2520<br>34 | -<br>0.0057<br>1 | -<br>3.0975<br>75 | 0.0013<br>33173     | -<br>0.0089<br>06421 | 0.1991<br>235  | 18.028 | 923.63 | 12.46 | 224.62<br>888 | 182 |
| 0.2431<br>16 | -<br>0.0224<br>9 | -<br>3.0770<br>68 | 0.0593<br>3313      | -<br>0.0019<br>88997 | 0.2049<br>767  | 18.138 | 923.91 | 12.46 | 225.99<br>948 | 184 |
| 0.2343<br>32 | -<br>0.0182<br>1 | -<br>3.0232<br>9  | -<br>0.1167<br>952  | 0.2355<br>98         | 0.4635<br>821  | 18.488 | 923.52 | 12.7  | 234.79<br>76  | 188 |
| 0.1676<br>58 | -<br>0.0054<br>7 | -<br>2.8823<br>97 | -<br>0.2950<br>52   | 0.1467<br>357        | 0.4992<br>334  | 18.658 | 923.5  | 12.53 | 233.78<br>474 | 195 |
| 0.1502<br>64 | -<br>0.0068<br>2 | -<br>2.8202<br>79 | -<br>0.0968<br>4108 | 0.1709<br>467        | 0.4816<br>738  | 18.698 | 923.34 | 12.53 | 234.28<br>594 | 199 |
| 0.1407<br>11 | 0.0097<br>54     | -<br>2.7691<br>96 | -<br>0.0800<br>7962 | 0.2869<br>466        | 0.4665<br>087  | 19.168 | 923.74 | 12.52 | 239.98<br>336 | 202 |
| 0.1096<br>59 | 0.0563<br>55     | -<br>2.6954<br>14 | -<br>0.1449<br>97   | 0.5569<br>923        | 0.5966<br>095  | 19.238 | 922.44 | 11.79 | 226.81<br>602 | 149 |
| 0.1478<br>02 | 0.1148<br>07     | 2.6369<br>56      | 0.0920<br>5788      | 0.3223<br>319        | 0.3805<br>729  | 20.018 | 923    | 11.44 | 229.00<br>592 | 152 |
| 0.2254<br>08 | 0.1203<br>76     | 2.7274<br>55      | 0.7135<br>621       | 0.0538<br>8253       | 0.8663<br>892  | 20.058 | 923.31 | 11.44 | 229.46<br>352 | 158 |
| 0.3167<br>67 | 0.0903<br>93     | 2.8215<br>3       | 0.6286<br>906       | -<br>0.0379<br>064   | 0.7115<br>452  | 20.148 | 923.08 | 11.05 | 222.63<br>54  | 163 |
| 0.3834<br>74 | 0.0811<br>56     | 2.8977<br>63      | 0.2796<br>266       | 0.2571<br>484        | 0.5614<br>902  | 20.188 | 923.01 | 11.05 | 223.07<br>74  | 167 |
| 0.4146<br>16 | 0.1106<br>57     | 2.9744<br>41      | 0.1295<br>716       | 0.5184<br>144        | 0.4888<br>573  | 20.328 | 922.77 | 10.69 | 217.30<br>632 | 171 |

|                  |              |                   |                     |                      |                      |        |        |              |                 |     |
|------------------|--------------|-------------------|---------------------|----------------------|----------------------|--------|--------|--------------|-----------------|-----|
| 0.4233<br>98     | 0.1393<br>51 | 3.0478<br>6       | -<br>0.1880<br>979  | 0.3401<br>576        | 0.3683<br>344        | 20.328 | 922.68 | 10.58        | 215.07<br>024   | 180 |
| 0.2100<br>61     | 0.1822<br>25 | 3.1400<br>29      | -<br>0.9285<br>286  | 0.2728<br>457        | 0.2954<br>354        | 20.818 | 922.16 | 9.71         | 202.14<br>278   | 185 |
| 0.1119<br>39     | 0.2014<br>97 | -<br>3.0992<br>62 | -<br>0.8660<br>057  | 0.1219<br>926        | 0.3747<br>197        | 20.818 | 921.89 | 9.71         | 202.14<br>278   | 186 |
| -<br>0.0273<br>7 | 0.1849<br>27 | -<br>3.0322<br>53 | -<br>0.4262<br>17   | -<br>0.0841<br>9996  | 0.1749<br>125        | 21.028 | 921.43 | 9.6399<br>99 | 202.70<br>9899  | 187 |
| -<br>0.0896<br>7 | 0.1925<br>93 | -<br>3.0143<br>45 | -<br>0.6020<br>793  | 0.1238<br>55         | 0.1605<br>456        | 21.068 | 921.6  | 9.6399<br>99 | 203.09<br>54989 | 189 |
| -<br>0.1312<br>4 | 0.2065<br>18 | -<br>2.9853<br>4  | -<br>0.1625<br>566  | 0.0780<br>9352       | 0.3489<br>124        | 21.238 | 921.39 | 9.37         | 199.00<br>006   | 191 |
| -<br>0.0953<br>5 | 0.2116<br>52 | -<br>2.9556<br>72 | 0.5092<br>319       | -<br>0.0011<br>90835 | 0.1826<br>281        | 21.298 | 922.02 | 9.38         | 199.77<br>524   | 190 |
| -<br>0.0275<br>9 | 0.2165<br>27 | -<br>2.9516<br>1  | 0.4927<br>365       | 0.1438<br>091        | -<br>0.0515<br>0017  | 21.438 | 921.08 | 9.38         | 201.08<br>844   | 189 |
| 0.0074<br>63     | 0.2361<br>28 | -<br>2.9708<br>8  | 0.1436<br>725       | 0.1438<br>091        | -<br>0.1007<br>203   | 21.698 | 921.29 | 8.99         | 195.06<br>502   | 189 |
| 0.0095<br>1      | 0.2353<br>06 | -<br>2.9807<br>84 | 0.1130<br>762       | -<br>0.0740<br>8988  | -<br>0.0017<br>47909 | 21.848 | 921.69 | 8.99         | 196.41<br>352   | 189 |
| 0.0771<br>74     | 0.2004<br>22 | -<br>2.9729<br>96 | 0.7941<br>768       | -<br>0.3875<br>025   | 0.1158<br>483        | 21.878 | 921.4  | 8.96         | 196.02<br>688   | 188 |
| 0.1865<br>96     | 0.1648<br>36 | -<br>2.9875<br>63 | 0.8859<br>656       | -<br>0.2087<br>136   | -<br>0.1499<br>405   | 21.938 | 921.19 | 8.88         | 194.80<br>944   | 186 |
| 0.2345<br>07     | 0.1637<br>15 | -<br>3.0196<br>72 | -<br>0.0140<br>9801 | 0.0568<br>0913       | -<br>0.2656<br>744   | 22.158 | 921.79 | 8.88         | 196.76<br>304   | 185 |
| 0.1752<br>47     | 0.1804<br>84 | -<br>3.0409<br>32 | -<br>0.7188<br>774  | 0.1041<br>669        | 0.0078<br>30067      | 22.3   | 920.87 | 8.76         | 195.34<br>8     | 188 |
| 0.0893<br>83     | 0.1853<br>35 | -<br>3.0154<br>22 | -<br>0.6129<br>875  | -<br>0.0123<br>6514  | 0.3819<br>032        | 22.3   | 922.3  | 8.76         | 195.34<br>8     | 190 |
| 0.0703<br>83     | 0.1445<br>99 | -<br>2.9614<br>55 | -<br>0.1064<br>191  | -<br>0.4811<br>538   | 0.4476<br>188        | 22.47  | 921.37 | 8.95         | 201.10<br>65    | 190 |
| 0.0358<br>61     | 0.0840<br>78 | -<br>2.9542<br>01 | -<br>0.5901<br>068  | -<br>0.3821<br>814   | 0.0120<br>8694       | 22.48  | 921.12 | 8.99         | 202.09<br>52    | 190 |
| -<br>0.0833<br>2 | 0.0634<br>07 | -<br>2.9620<br>3  | -<br>1.2137<br>4    | 0.0131<br>7613       | 0.0331<br>0528       | 22.61  | 921.46 | 8.99         | 203.26<br>39    | 192 |
| -<br>0.2006<br>6 | 0.0713<br>68 | -<br>2.9388<br>55 | -<br>0.7635<br>746  | 0.0182<br>3117       | 0.4699<br>674        | 22.75  | 921.23 | 9.03         | 205.43<br>25    | 196 |
| -<br>0.2392      | 0.0824<br>22 | -<br>2.8788       | -<br>0.0369         | -<br>0.0533          | 0.5694<br>719        | 22.88  | 921.42 | 9.03         | 206.60<br>64    | 199 |

|                  |              |                   |                    |                      |                      |       |        |              |                 |     |
|------------------|--------------|-------------------|--------------------|----------------------|----------------------|-------|--------|--------------|-----------------|-----|
| 7                |              | 06                | 7873               | 3759                 |                      |       |        |              |                 |     |
| -<br>0.2131<br>1 | 0.0881<br>09 | -<br>2.8181<br>63 | 0.1098<br>836      | -<br>0.0009<br>24778 | 0.4667<br>747        | 23.09 | 920.7  | 9.15         | 211.27<br>35    | 200 |
| -<br>0.2126<br>7 | 0.1023<br>68 | -<br>2.7933<br>89 | -<br>0.1061<br>53  | 0.1134<br>788        | 0.1828<br>942        | 23.16 | 920.94 | 9.22         | 213.53<br>52    | 200 |
| -<br>0.2052<br>7 | 0.1179<br>75 | -<br>2.7885<br>28 | 0.2958<br>559      | 0.1951<br>577        | 0.0940<br>3185       | 23.35 | 920.35 | 9.22         | 215.28<br>7     | 200 |
| -<br>0.1231<br>9 | 0.1481<br>69 | -<br>2.7884<br>35 | 0.8356<br>813      | 0.3037<br>081        | 0.1166<br>465        | 23.35 | 921.42 | 9.11         | 212.71<br>85    | 199 |
| -<br>0.0395<br>9 | 0.1826<br>08 | -<br>2.8003<br>66 | 0.5781<br>401      | 0.2797<br>631        | -<br>0.1190<br>781   | 23.48 | 920.89 | 9.11         | 213.90<br>28    | 197 |
| -<br>0.0002<br>5 | 0.1916<br>89 | -<br>2.8275<br>56 | 0.1920<br>945      | -<br>0.0283<br>2843  | -<br>0.1680<br>322   | 23.7  | 920.34 | 9.01         | 213.53<br>7     | 195 |
| 0.0101<br>52     | 0.1879<br>79 | -<br>2.8610<br>92 | 0.1615<br>724      | -<br>0.0014<br>03395 | -<br>0.1780<br>888   | 23.77 | 921.28 | 8.99         | 213.69<br>23    | 195 |
| 0.0370<br>97     | 0.1913<br>23 | -<br>2.8734<br>68 | 0.2493<br>705      | 0.1114<br>039        | 0.0105<br>4411       | 23.91 | 920.16 | 8.99         | 214.95<br>09    | 196 |
| 0.0685<br>96     | 0.2031<br>21 | -<br>2.8638<br>91 | 0.1879<br>119      | 0.0858<br>626        | 0.1935<br>899        | 23.94 | 921.04 | 8.7          | 208.27<br>8     | 197 |
| 0.0687<br>27     | 0.2063<br>74 | -<br>2.8475<br>89 | -<br>0.1435<br>925 | 0.0233<br>3971       | 0.1637<br>917        | 24.12 | 920.38 | 8.7          | 209.84<br>4     | 198 |
| 0.0366<br>93     | 0.1951<br>18 | -<br>2.8303<br>86 | -<br>0.4793<br>538 | -<br>0.1056<br>969   | 0.2300<br>394        | 24.26 | 920.45 | 8.65         | 209.84<br>9     | 199 |
| -<br>0.0234<br>4 | 0.1925<br>5  | -<br>2.8073<br>82 | -<br>0.5389<br>501 | 0.0222<br>7549       | 0.3034<br>705        | 24.3  | 920.84 | 8.52         | 207.03<br>6     | 201 |
| -<br>0.0800<br>7 | 0.1897<br>63 | -<br>2.7720<br>26 | -<br>0.5511<br>886 | -<br>0.0394<br>4924  | 0.3282<br>136        | 24.43 | 920.63 | 8.52         | 208.14<br>36    | 202 |
| -<br>0.1264<br>5 | 0.1781<br>74 | -<br>2.7455<br>24 | -<br>0.3420<br>695 | -<br>0.1397<br>519   | 0.2475<br>99         | 24.62 | 920.59 | 8.38         | 206.31<br>56    | 202 |
| -<br>0.1602<br>1 | 0.1747<br>36 | -<br>2.7498<br>07 | -<br>0.2287<br>301 | 0.1068<br>809        | -<br>0.0836<br>3932  | 24.68 | 920.38 | 8.38         | 206.81<br>84    | 200 |
| -<br>0.2068      | 0.1884<br>54 | -<br>2.7730<br>54 | -<br>0.5011<br>703 | 0.1616<br>882        | -<br>0.0575<br>6595  | 24.78 | 921.14 | 8.26         | 204.68<br>28    | 200 |
| -<br>0.2591<br>7 | 0.1959<br>05 | -<br>2.7851<br>55 | -<br>0.2383<br>081 | 0.0150<br>92         | -<br>0.0048<br>87076 | 24.94 | 920.27 | 8.3499<br>99 | 208.24<br>89751 | 200 |
| -<br>0.2428<br>8 | 0.1807<br>8  | -<br>2.7857<br>81 | 0.3946<br>365      | -<br>0.1293<br>758   | -<br>0.0128<br>6872  | 25.02 | 921.2  | 8.3499<br>99 | 208.91<br>6975  | 198 |
| -<br>0.1726      | 0.1571<br>22 | -<br>2.8027<br>82 | 0.5816<br>731      | -<br>0.1291<br>097   | -<br>0.1679<br>787   | 25.2  | 920.26 | 8.16         | 205.63<br>2     | 196 |

|                  |              |                   |                      |                    |                    |       |        |      |              |     |
|------------------|--------------|-------------------|----------------------|--------------------|--------------------|-------|--------|------|--------------|-----|
| -<br>0.1436<br>4 | 0.1439<br>87 | -<br>2.8426<br>73 | 0.1158<br>11         | 0.0802<br>7545     | -<br>0.2970<br>153 | 25.35 | 921.09 | 8.16 | 206.85<br>6  | 196 |
| -<br>0.1245<br>4 | 0.1649<br>16 | -<br>2.8604<br>4  | 0.2727<br>833        | 0.2580<br>001      | 0.1084<br>523      | 25.38 | 921.42 | 8    | 203.04       | 197 |
| -<br>0.0581      | 0.1895<br>49 | -<br>2.8467<br>39 | 0.7139<br>024        | 0.1036<br>883      | 0.2417<br>458      | 25.5  | 921.5  | 7.92 | 201.96       | 197 |
| 0.0322<br>58     | 0.1838<br>45 | -<br>2.8369<br>18 | 0.6391<br>41         | -<br>0.1166<br>052 | 0.0283<br>6978     | 25.65 | 920.15 | 7.92 | 203.14<br>8  | 195 |
| 0.0673<br>25     | 0.1566<br>01 | -<br>2.8563<br>8  | -<br>0.0055<br>10043 | -<br>0.2669<br>261 | -<br>0.1025<br>292 | 25.73 | 921.35 | 7.81 | 200.95<br>13 | 194 |
| 0.0292<br>64     | 0.1318<br>37 | -<br>2.8874<br>36 | -<br>0.3471<br>245   | -<br>0.1913<br>666 | -<br>0.1405<br>751 | 25.86 | 920.74 | 7.81 | 201.96<br>66 | 194 |